



**TEXAS A&M**  
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## Application of Standard 87T Differential Protection on Phase-Shifting Transformers

Z. Gajić, G. Neise, K. de la Porte, M. Kockott, B. Vasudevan; Hitachi Energy

D. Seifert; J. Neuhaus, TenneT TSO GmbH, Germany

E. Chen; Consolidated Edison Inc., NY, USA

# Introduction

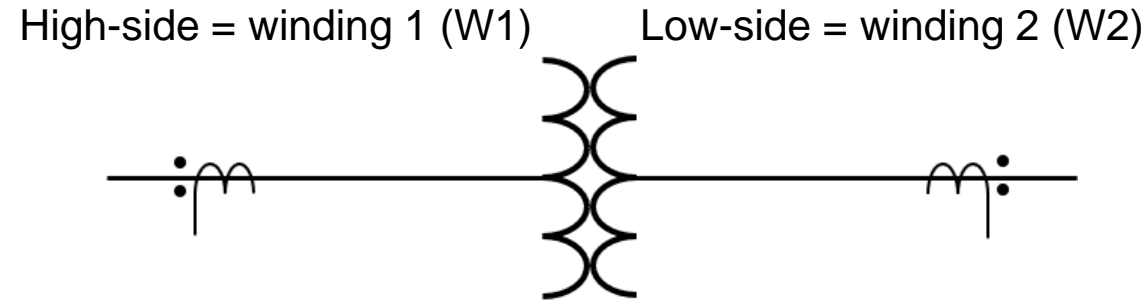
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- Standard two-winding 87T protection
  - principle of operation, typical settings
- Self-adapting differential protection for PSTs
  - principle of operation, typical settings
- Customer TenneT: testing and pilot installation
- Customer ConEd: selection requirements and commissioning recording
- Conclusions

# Phase-angle shift across a transformer

- A phase-angle shift  $\Theta$  occurs between the no-load voltages and between the through-going currents on the two sides of the transformer
  - standard two-winding three-phase power transformers introduce a fixed phase-angle shift  $\Theta$  of  $n \cdot 30^\circ$  ( $n=0, 1, 2, \dots, 11$ ) –  $n$  is defined by the transformer vector group at manufacture
  - phase shifting transformers introduce a variable phase-angle shift  $\Theta$ , for example  $\pm 24^\circ$  in total, having  $\pm 32$  OLTC steps of approximately  $0.75^\circ$  per step

# Standard transformer differential 87T principle of operation



- 87T transformer differential protection – factors to consider
  - transformation (turns) ratio; winding type; vector group; flow of zero sequence current
- Solution
  - bring all current magnitudes to the same magnitude reference (magnitude compensation)
  - align all current phase angles to the same phase reference (phase-angle compensation)
    - phase reference side – no rotation of currents
    - non phase reference side – rotate currents to align with the phase reference side currents
  - eliminate the zero-sequence currents (that can flow on only one side)

# Standard transformer differential 87T principle of operation

- Microprocessor relays – matrix equation

- all currents/voltages shown below are in primary values

$$\begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = A * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + \frac{V_{rated\_W2}}{V_{rated\_W1}} * B * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix}$$

Ratio (magnitude compensation)

$$= \begin{bmatrix} DCCA\_W1 \\ DCCB\_W1 \\ DCCC\_W1 \end{bmatrix} + \begin{bmatrix} DCCA\_W2 \\ DCCB\_W2 \\ DCCC\_W2 \end{bmatrix}$$

Commonly termed the compensated currents

- where

$$|ID\_A| = |DCCA\_W1 + DCCA\_W2|$$

$$|ID\_B| = |DCCB\_W1 + DCCB\_W2|$$

$$|ID\_C| = |DCCC\_W1 + DCCC\_W2|$$

- A and B are 3X3 matrices

- the elements of A and B depend on

- winding connection type, i.e. wye or delta

- transformer vector group, DABY (Dyn1), DACY (Dyn11), etc.

- whether the subtraction (elimination) of zero-sequence current is enabled or not

- the selected phase reference side

- matrix multiplication

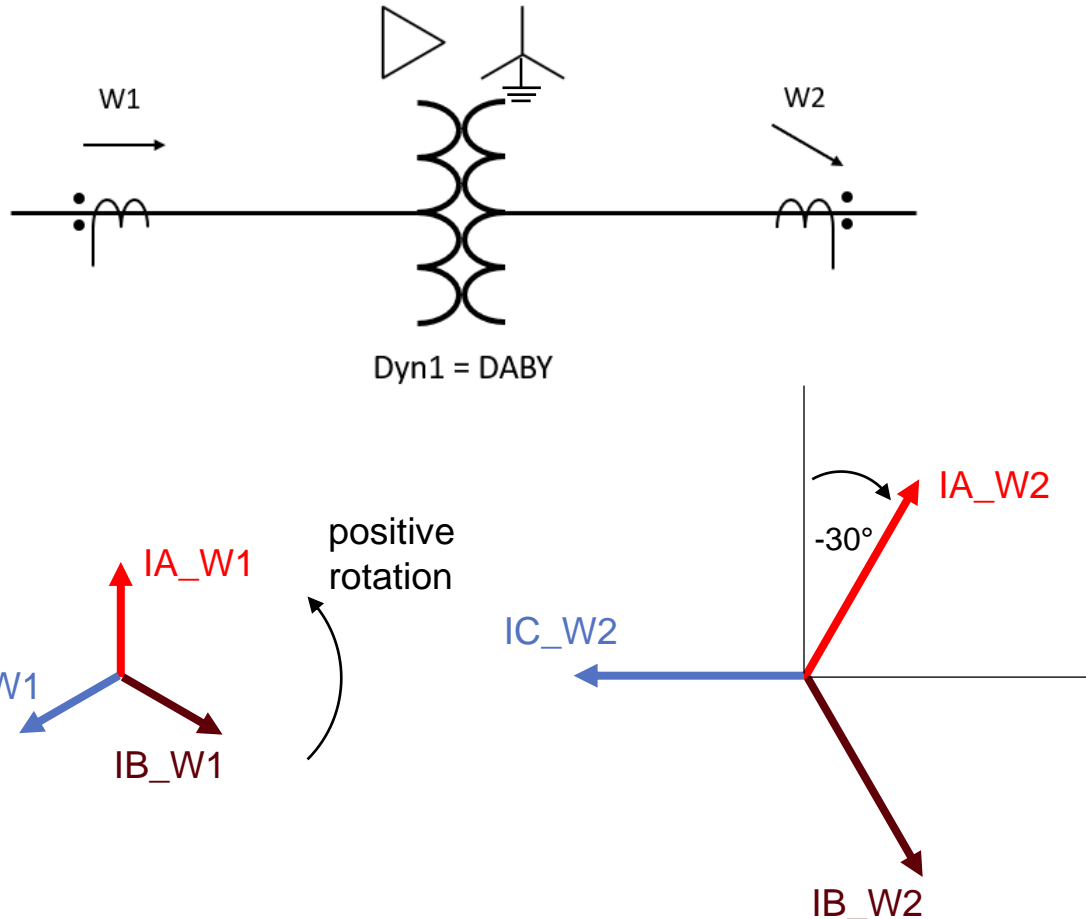
- phase reference side – introduces no phase shift in the currents

- non phase reference side – phase shifts the currents to align with the phase reference side

- subtract zero-sequence if required

# Standard transformer differential 87T principle of operation

- Settings example (microprocessor relay): Dyn1 (DABY) transformer

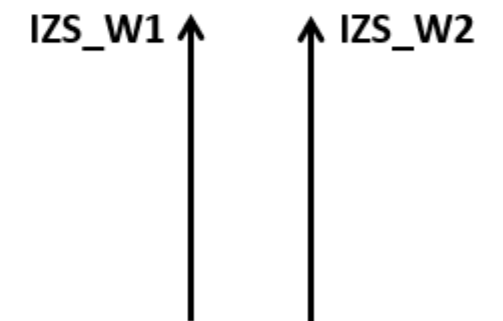
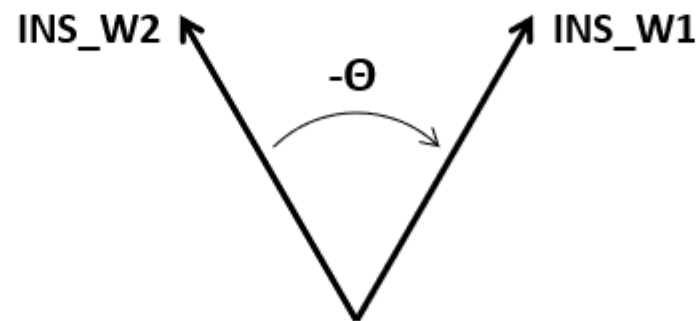
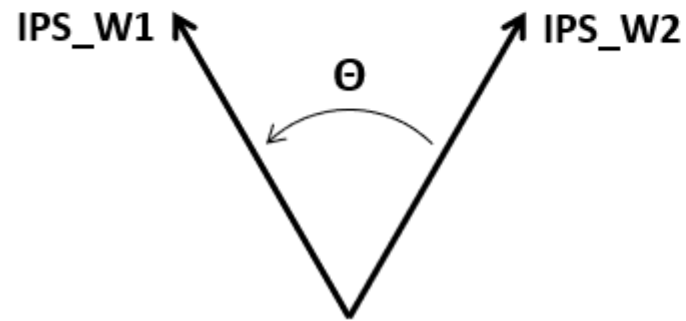
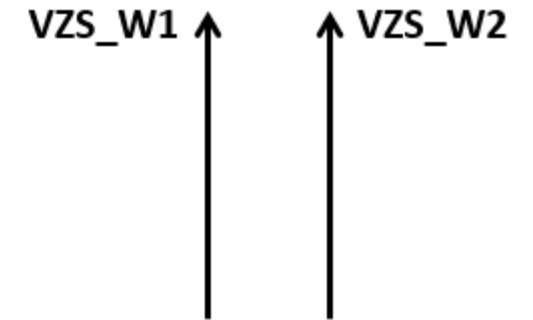
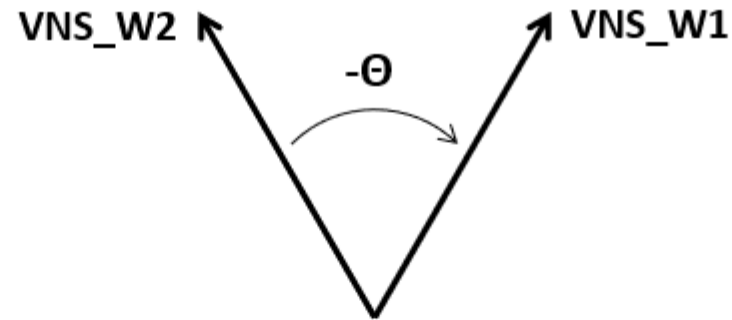
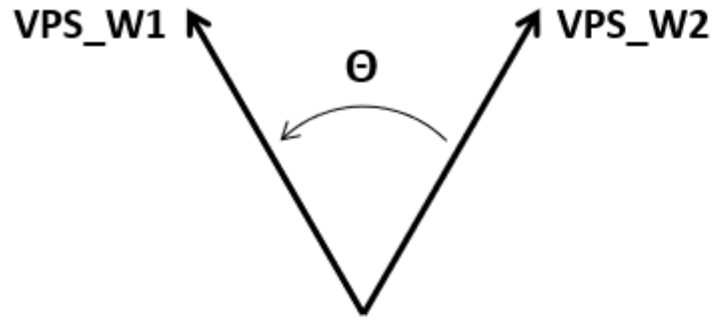


- typical 87T function settings to set the transformer details

- $V_{rated\_W1}$
- $I_{rated\_W1}$
- $V_{rated\_W2}$
- $I_{rated\_W2}$
- W1 connection DELTA
- W2 connection WYE
- W2 clock position 1 'o clock with respect to W1
- W1 zero-sequence Off/On subtraction
- W2 zero-sequence Off/On subtraction

# Transformer differential 87T theoretical overview

- Strict rules exist only for the phase-angle shift between the sequence components, and not the individual phase quantities

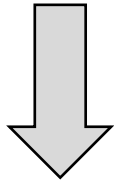


# Transformer differential 87T theoretical overview

$$ID\_PS = IPS\_W1 + Ratio * e^{j\theta} * IPS\_W2$$

$$ID\_NS = INS\_W1 + Ratio * e^{-j\theta} * INS\_W2$$

$$ID\_ZS = IZS\_W1 + Ratio * IZS\_W2$$



$$\begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = M(0^\circ) * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + Ratio * M(\theta) * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix} \quad \text{OR} \quad \begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = M(-\theta) * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + Ratio * M(0^\circ) * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix}$$



# Transformer differential 87T theoretical overview

$$M(\Theta) = \frac{1}{3} \begin{bmatrix} 1+2*\cos(\Theta) & 1+2*\cos(\Theta+120^\circ) & 1+2*\cos(\Theta-120^\circ) \\ 1+2*\cos(\Theta-120^\circ) & 1+2*\cos(\Theta) & 1+2*\cos(\Theta+120^\circ) \\ 1+2*\cos(\Theta+120^\circ) & 1+2*\cos(\Theta-120^\circ) & 1+2*\cos(\Theta) \end{bmatrix}$$

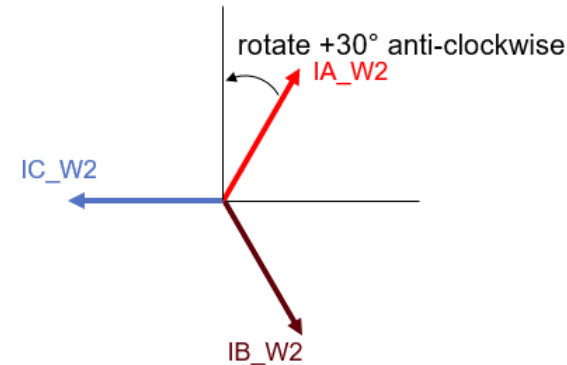
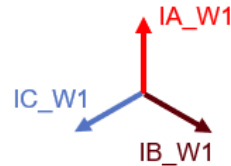
- $M(\Theta)$  matrix does not subtract the zero sequence currents
- $M0(\Theta)$  matrix to be used when the zero sequence currents must be subtracted

$$M0(\Theta) = \frac{2}{3} \begin{bmatrix} \cos(\Theta) & \cos(\Theta+120^\circ) & \cos(\Theta-120^\circ) \\ \cos(\Theta-120^\circ) & \cos(\Theta) & \cos(\Theta+120^\circ) \\ \cos(\Theta+120^\circ) & \cos(\Theta-120^\circ) & \cos(\Theta) \end{bmatrix}$$

# Standard transformer differential 87T principle of operation

- Dyn1 (DABY) transformer
  - delta-winding (W1) as the phase reference

$$\begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + \frac{V_{rated\_W2}}{V_{rated\_W1}} * \frac{1}{\sqrt{3}} \begin{bmatrix} 1 & -1 & 0 \\ 0 & 1 & -1 \\ -1 & 0 & 1 \end{bmatrix} * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix}$$



no zero-sequence subtraction is required, so use the M(0°) matrix

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

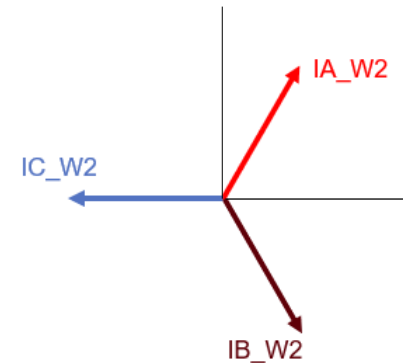
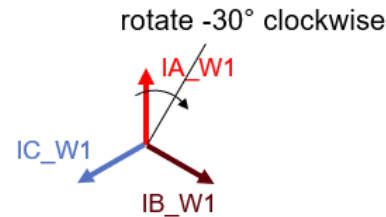
use matrix M0(30°) as it is necessary to subtract the zero-sequence

$$\begin{bmatrix} 0.577 & -0.577 & 0.000 \\ 0.000 & 0.577 & -0.577 \\ -0.577 & 0.000 & 0.577 \end{bmatrix}$$

# Standard transformer differential 87T principle of operation

- Dyn1 (DABY) transformer
  - wye-winding (W2) as the phase reference

$$\begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = \frac{1}{\sqrt{3}} \begin{bmatrix} 1 & 0 & -1 \\ -1 & 1 & 0 \\ 0 & -1 & 1 \end{bmatrix} * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + \frac{V_{rated\_W2}}{V_{rated\_W1}} * \frac{1}{3} \begin{bmatrix} 2 & -1 & -1 \\ -1 & 2 & -1 \\ -1 & -1 & 2 \end{bmatrix} * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix}$$



there is no zero-sequence in the measured currents, but anyway can use the M0(-30°) matrix

$$\begin{bmatrix} 0.577 & 0.000 & -0.577 \\ -0.577 & 0.577 & 0.000 \\ 0.000 & -0.577 & 0.577 \end{bmatrix}$$

use matrix M0(0°) as it is necessary to subtract the zero-sequence

$$\begin{bmatrix} 0.667 & -0.333 & -0.333 \\ -0.333 & 0.667 & -0.333 \\ -0.333 & 0.667 & -0.333 \end{bmatrix}$$

# Phase shifting transformer differential protection

- 87T for PST
  - 87T protection that requires voltage measurement (needs VTs on the S- and L-sides – single-phase or three-phase)
  - has on-line measurement of phase-angle shift and transformation ratio (PSTs have varying phase-angle shift and maybe also varying ratio)
  - is suitable for any PST regardless of its construction (symmetrical or asymmetrical; single-core or double-core)
  - does not require OLTC position
  - is similar to the standard 87T function for two-winding transformers



# Phase shifting transformer differential protection

- 87T for PST

- continuously performs on-line estimation of transformation ratio and phase-angle shift

$$\begin{aligned}\text{Complex Current Ratio (CCR)} &= \frac{-I_{W2}}{I_{W1}} = \frac{|I_{W2}|}{|I_{W1}|} e^{j(\angle I_{W2} + 180^\circ - \angle I_{W1})} \\ &= |\text{CCR}| e^{jI\_Angle}\end{aligned}$$

- $I_{W1}$  and  $I_{W2}$  are the positive-sequence current phasors from the two transformer sides

$$I\_Ratio = \frac{1}{|\text{CCR}|}$$

$$\begin{aligned}\text{Complex Voltage Ratio (CVR)} &= \frac{V_{W2}}{V_{W1}} = \frac{|V_{W2}|}{|V_{W1}|} e^{j(\angle V_{W2} - \angle V_{W1})} \\ &= |\text{CVR}| e^{jV\_Angle}\end{aligned}$$

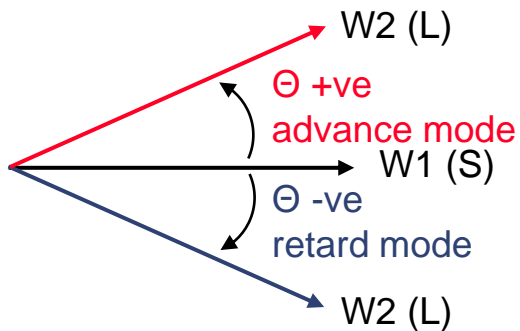
- $V_{W1}$  and  $V_{W2}$  are the selected voltage phasors (one from each side)

$$V\_Ratio = |\text{CVR}|$$

# Phase shifting transformer differential protection

- 87T for PST

$$\begin{bmatrix} ID\_A \\ ID\_B \\ ID\_C \end{bmatrix} = M0(0^\circ) * \begin{bmatrix} IA\_W1 \\ IB\_W1 \\ IC\_W1 \end{bmatrix} + DIFRATIO * M0(DIFANGLE) * \begin{bmatrix} IA\_W2 \\ IB\_W2 \\ IC\_W2 \end{bmatrix}$$



I\_Ratio or V\_Ratio

I\_Angle or V\_Angle (mult by -1) → DIFANGLE

$$M0(\Theta) = \frac{2}{3} \begin{bmatrix} \cos(\Theta) & \cos(\Theta+120^\circ) & \cos(\Theta-120^\circ) \\ \cos(\Theta-120^\circ) & \cos(\Theta) & \cos(\Theta+120^\circ) \\ \cos(\Theta+120^\circ) & \cos(\Theta-120^\circ) & \cos(\Theta) \end{bmatrix}$$

- pre-programmed rules determine which of the on-line estimated values are used
  - if both W1 and W2 positive-sequence current magnitudes  $\geq 10\%$  of  $I_{rated}$ , the values from the current calculation are used
  - if either positive-sequence current magnitude  $< 10\%$  of  $I_{rated}$ , only then are values from the voltage calculation used

# Phase shifting transformer differential protection

- 87T for PST

- negative-sequence differential function

$$ID\_NS = INS\_W1 + Ratio * INS\_W2 * e^{-j\theta}$$

- where

- $ID\_NS$  is the negative-sequence differential current phasor, and  $INS\_W1$  and  $INS\_W2$  are the  $W1$  and  $W2$  negative-sequence current phasors
- the provided features are equally applicable to the 87T for PST as for the standard transformer 87T



# Phase shifting transformer differential protection

- Settings

- Typical settings for standard 87T

- $V_{rated\_W1}$
- $I_{rated\_W1}$
- $V_{rated\_W2}$
- $I_{rated\_W2}$
- W1 connection            DELTA
- W2 connection            WYE
- W2 clock position        1 'o clock
- W1 zero-sequence subtraction    Off/On
- W2 zero-sequence subtraction    Off/On

- Typical settings for 87T for PST

- $V_{rated\_W1}$
- $I_{rated\_W1}$
- $V_{rated\_W2}$
- $I_{rated\_W2}$
- W1 zero-sequence subtraction    Off/On
- W2 zero-sequence subtraction    Off/On
- W1 and W1 voltage input selection

# Phase-shifting transformer differential protection

- Settings

- Typical settings for standard 87T

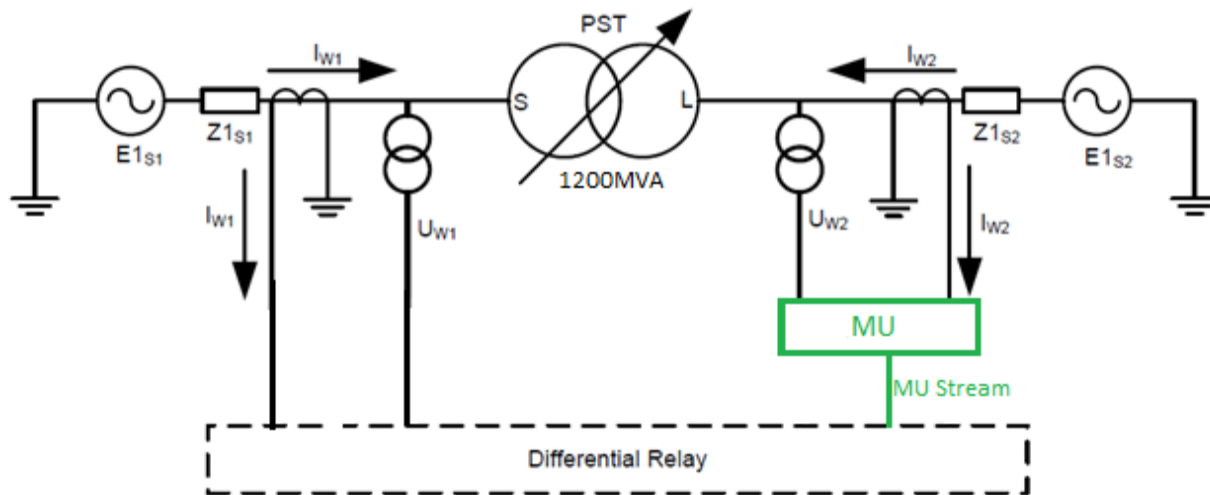
- minimum pickup sensitivity
- restrained characteristic
- high-set unrestrained trip level
- 2nd / 5th harmonic block / restrain levels
- cross block On / Off
- negative-sequence function settings

- Typical settings for 87T for PST

- minimum pickup sensitivity
- restrained characteristic
- high-set unrestrained trip level
- 2nd / 5th harmonic block / restrain levels
- cross block On / Off
- negative-sequence function settings

# Customer: TenneT TSO GmbH, Germany

- Secondary injection testing using a test set
- Secondary injection of simulated external and internal fault conditions
- Pilot installation of the 87T-PST (since March 2021)
  - existing dual-core, symmetrical PST having the following rated data:
    - 1200MVA; 400/400kV; 50Hz;  $\pm 24^\circ$  (32 OLTC positions in advance direction, and 32 OLTC positions in retard direction, with an advance-retard switch due to the large number of taps)



- PST has operated at various loads and OLTC positions, as well as different positions of the advanced-retard switch
- several primary faults have happened during this time in the vicinity of the PST
- the 87T-PST differential protection has remained stable

# Customer: TenneT TSO GmbH, Germany

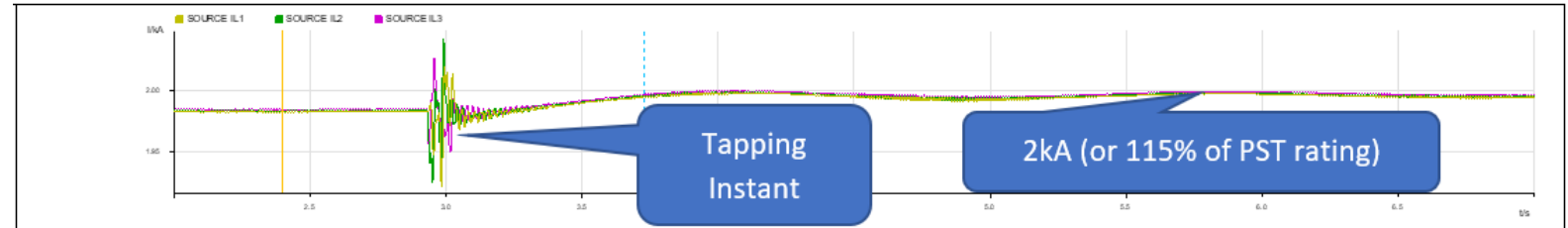
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- 87T-PST testing during new PST FAT at the transformer factory
  - same PST type as where pilot was installed
  - same analog input arrangement as for pilot
  - all 65 tap positions were checked under load by tapping from position 32A to position 32R – every tap transition was recorded

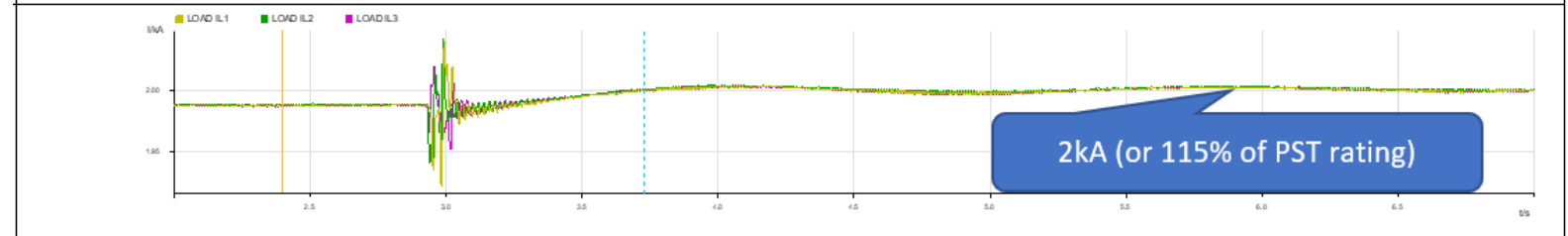
# Customer: TenneT TSO GmbH, Germany

- 87T\_PST testing during new PST FAT at the transformer factory – tap change under full load

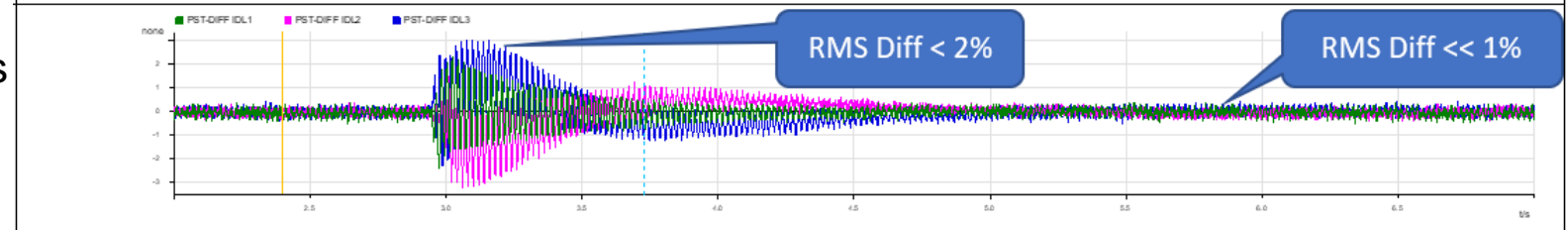
RMS values of the measured S-side currents in kA (W1)



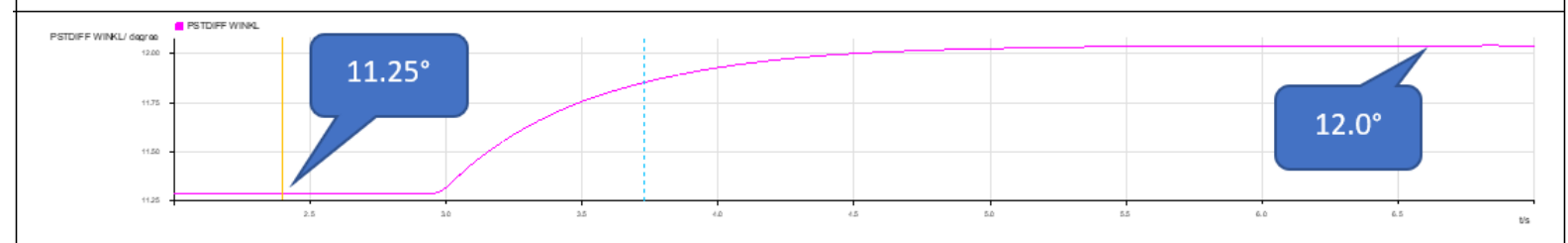
RMS values of the measured L-side currents in kA (W2)



Internally calculated instantaneous differential currents in percent of PST rating



Internally calculated phase-angle shift across the PST in degrees



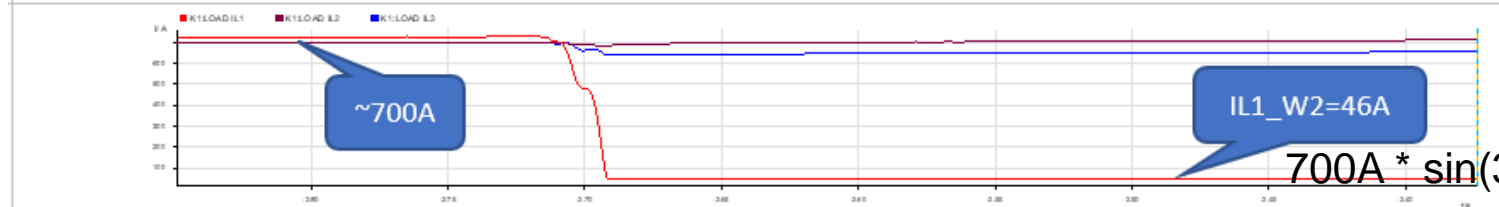
# Customer: TenneT TSO GmbH, Germany

- 87T\_PST testing – in-service PST, single-pole opened on S-side (PST on tap 5 advance = 3.75°)

RMS values of the measured S-side currents in kA (W1)

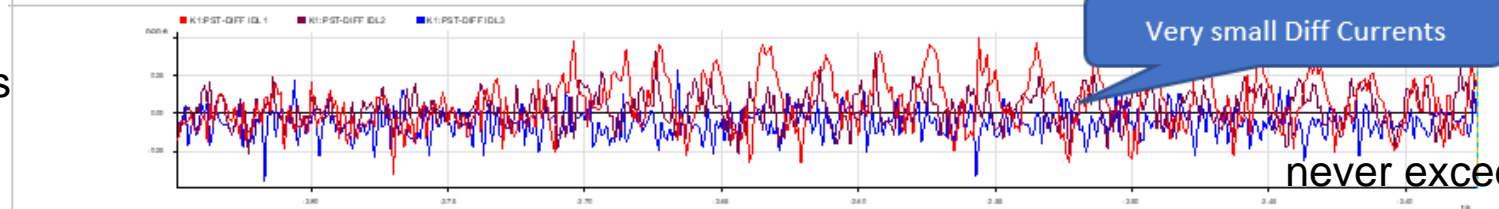


RMS values of the measured L-side currents in kA (W2)



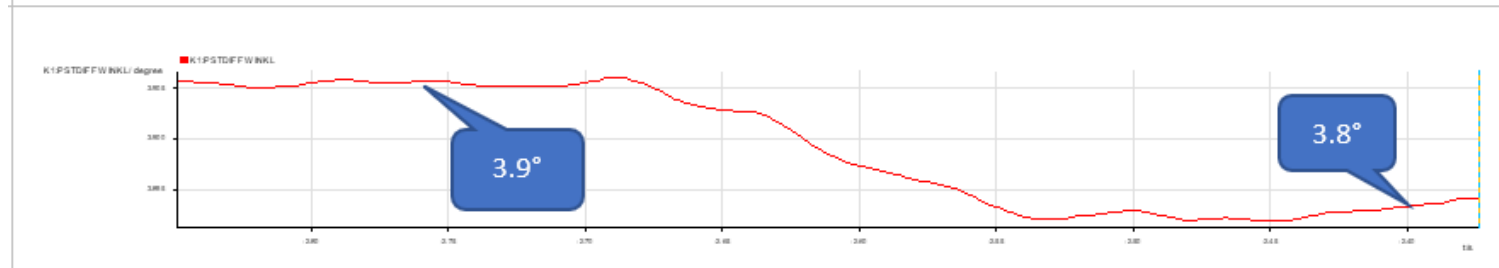
$$700A * \sin(3.75^\circ) = 46A$$

Internally calculated instantaneous differential currents in percent of PST rating



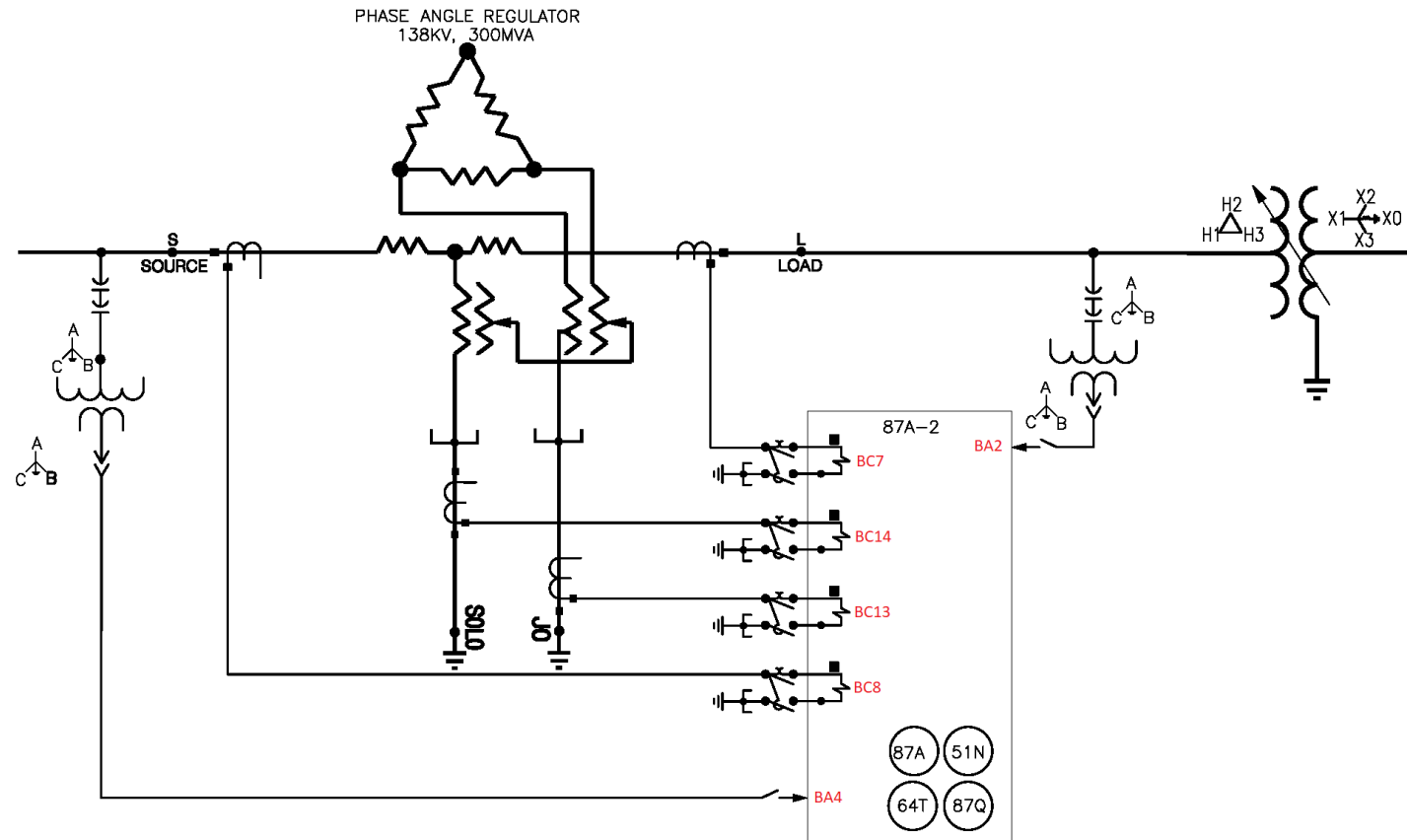
never exceeded 0.5%

Internally calculated phase-angle shift across the PST in degrees



# Customer: ConEd, NY, USA

- PSTs are used to control active power flow
- Commissioned a new 300MVA; 60Hz; 138kV;  $\pm 25^\circ$ ; symmetrical double-core PST in 2022
- Protected by two different systems, one incorporating the 87T for PST function



# Customer: ConEd, NY, USA

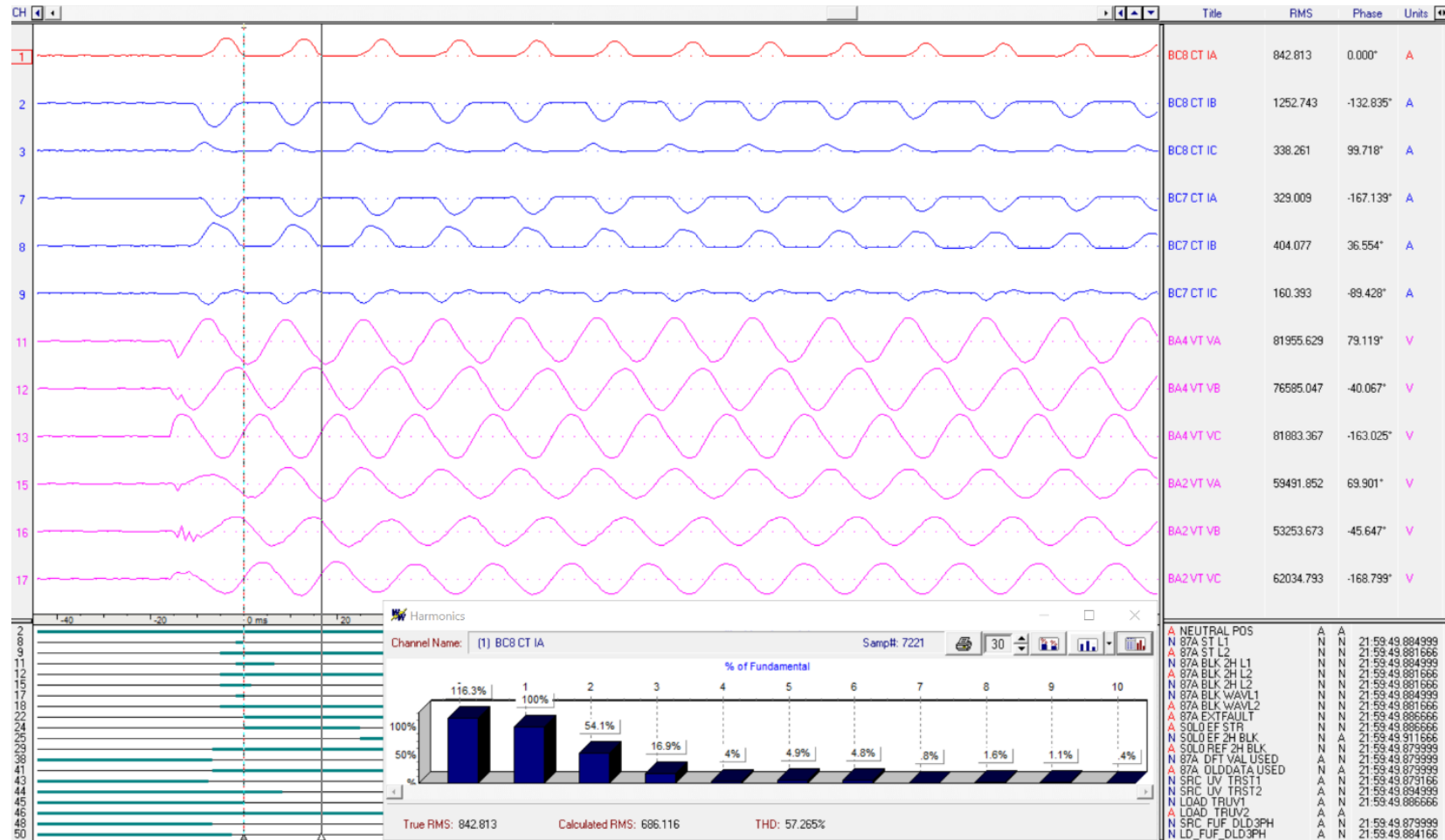
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- Customer: ConEd, NY, USA
  - protection system must provide complete PST protection for all high- and low-level internal faults, as well as backup protection for all external ground faults
  - new solution, with 87T for PST
    - one relay, where traditionally many were required
    - low-level internal faults (turn-to-turn) covered, where traditionally had to rely on sudden pressure and/or Buchholz devices (overcurrent supervised)



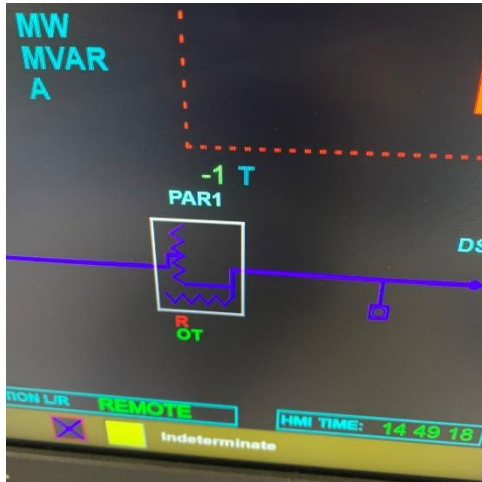
# Customer: ConEd, NY, USA

- Energization of the PST - phase quantities
  - high DC offset and 2nd harmonic content in the source-side inrush currents – remained stable (no operation)



# Customer: ConEd, NY, USA

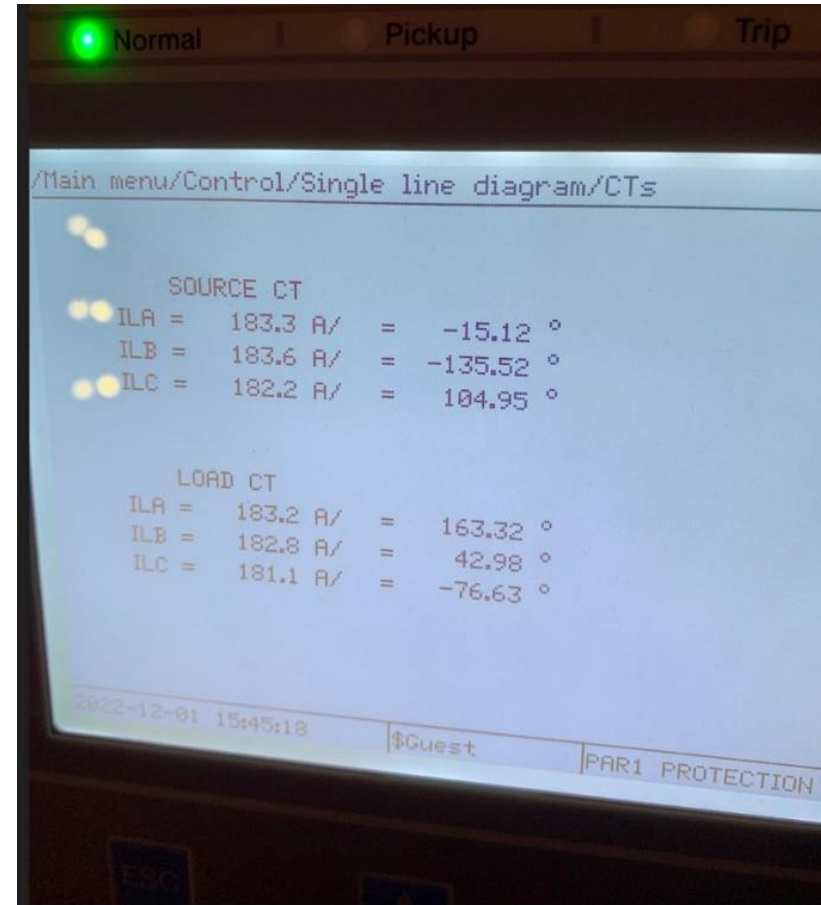
PST's OLTC tap position on the substation HMI screen (tap 1 retard)



PST nameplate

Retard	NA	NR	17
	N	N	0.0
	NR	NA	1
	1R	1A	-1.6
	2R	2A	-3.2
	3R	3A	-4.8
	4R	4A	-6.3
	5R	5A	-7.9
	6R	6A	-9.5
	7R	7A	-11.1
Advance	8R	8A	-12.6
	9R	9A	-14.2
			10

L-side current will lag S-side current by 1.6°  
 S-side current into PST; L-side current from PST  
 Therefore IED perceived angle difference = 178.4° lead



PhaseA: 178.44°

PhaseB: 178.50°

PhaseC: 178.42°

# Conclusions

- 87T for PST only requires one three-phase current set and at least one phase-to-ground voltage from each side of the protected PST – internally buried CTs within the protected PST tank are not required
- Position of any internal OLTC is not required
- 87T for PST is suitable for any PST regardless of its construction (symmetrical or asymmetrical; single-core or double-core) – protects the complete PST against all internal faults
- Transformation ratio and phase-angle shift are estimated on-line
- Typically, a minimum pickup of 20%, based on the PST rating, can be achieved for the differential protection
- Negative-sequence based differential protection provides additional sensitivity for low level turn-to-turn faults
- Possible to use 87T for PST on standard two-winding transformer with OLTC where compensation for tap position is required (traditionally accomplished by connecting tap position to the 87T function) – 87T for PST continuously calculates on-line the “Ratio” without requiring connection of tap position