



Transmission Line Parameter Estimation Using Traveling-Wave Fault Location Data

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Outline

- Necessity of accurate line parameters
- Available line parameter estimation methods
- Double-ended traveling-wave fault location
- Incremental quantities
- Proposed line parameter estimation method
- Simulation and field event results
- Phenomena that impacts accuracy
- Conclusion

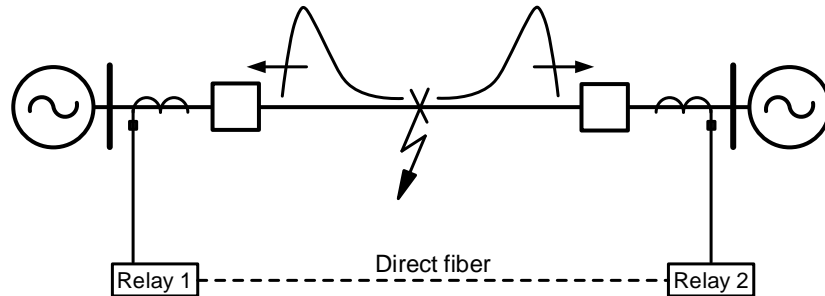
Necessity of accurate line parameters

- Phasor-based distance protection
- Impedance-based fault location
- Short circuit analysis
- Relay testing
- Power flow and stability studies

Available line parameter estimation methods

- Offline methods
 - Line constant tools
 - Signal injection methods
 - Event analysis using known fault location
- Online methods
 - Synchrophasor measurements
 - SPO method

Double-ended traveling-wave fault location



$$m = \frac{1}{2} [l + (t_L - t_R) \cdot v]$$

m = fault location estimation using DETWFL
 l = line length setting
 t_L = first TW arrival time at local relay
 t_R = first TW arrival time at remote relay
 v = TW propagation velocity

Double-ended traveling-wave fault location

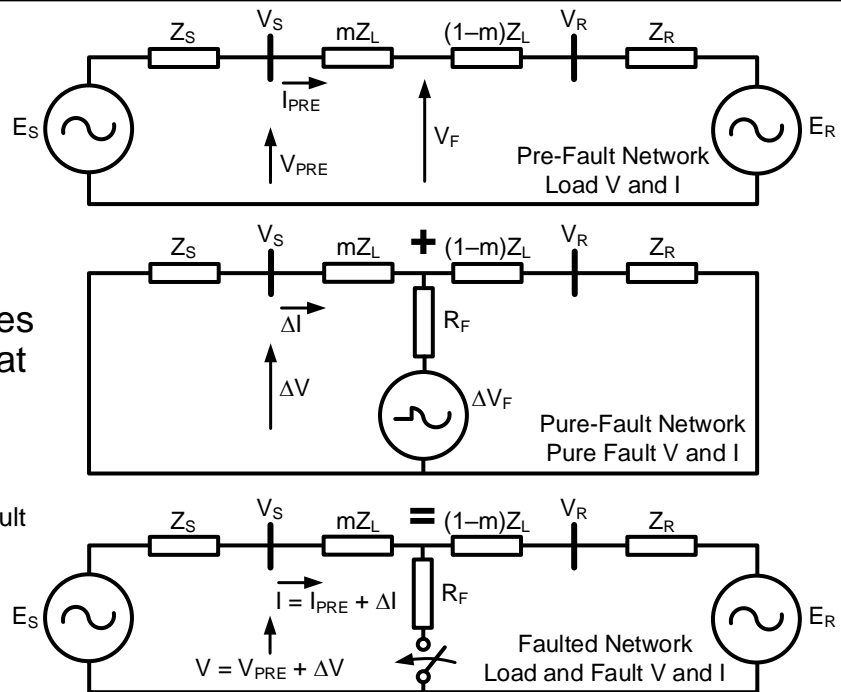
- DETWFL method does not use Z_1 and Z_0 parameters; errors in line parameter settings have no impact on fault location estimates
- DETWFL method provides accuracy as low as 300 m or close to one tower span in real-world fault events

Incremental quantities

- Superposition principle is applied
- Incremental quantities represent signals that appear in the pure-fault network

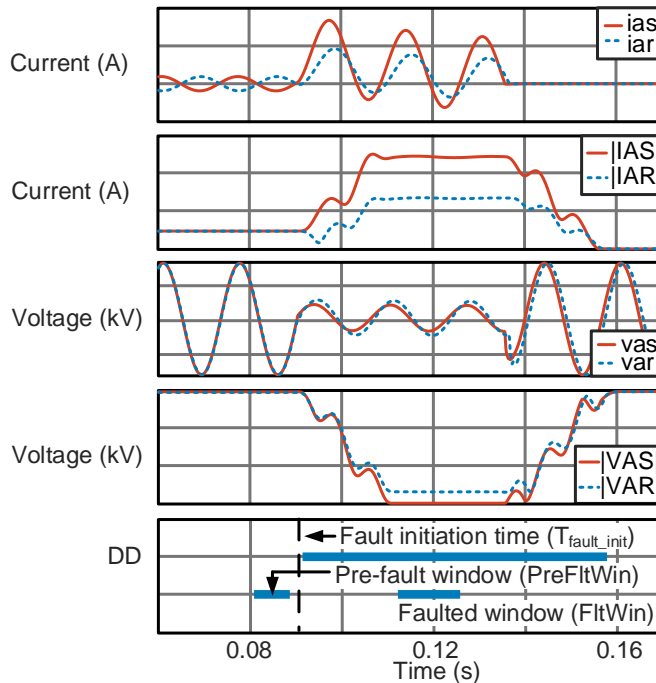
$$\Delta V = V_{\text{Faulted}} - V_{\text{Pre-fault}}$$

$$\Delta I = I_{\text{Faulted}} - I_{\text{Pre-fault}}$$



Proposed method

DD – disturbance detector is used to identify fault initiation time



Proposed method

- Z_1 is estimated using phasors from pre-fault window and solving positive-sequence network
- Incremental phasors (ΔV , ΔI) are computed by subtracting pre-fault phasors from faulted phasors
- Z_0 is estimated using incremental phasors and solving pure-fault zero-sequence network
- Only Z_0 estimation method uses TW fault location data

Proposed Z_1 estimation method

Time synchronized voltage and current phasors from pre-fault data window from both ends are used; PI equivalent model is used

$$I_{C1} = I_{1S} + I_{1R} \quad |Y_{C1}| = \left| \frac{2 \cdot I_{C1}}{V_{1S} + V_{1R}} \right| \quad |Y_{C0}| = \frac{|Y_{C1}|}{1.7} \quad B_S = \frac{2 \cdot Y_{C1} + Y_{C0}}{3} \quad B_M = \frac{Y_{C0} + Y_{C1}}{3}$$

Line charging current supplied from local end

$$\begin{bmatrix} I_{AS_CC'} \\ I_{BS_CC'} \\ I_{CS_CC'} \end{bmatrix} = 0.5 \cdot \begin{bmatrix} B_S & B_M & B_M \\ B_M & B_S & B_M \\ B_M & B_M & B_S \end{bmatrix} \cdot \begin{bmatrix} V_{AS} \\ V_{BS} \\ V_{CS} \end{bmatrix}$$

Proposed Z_1 estimation method

Current flowing through local end

$$\begin{bmatrix} I_{AS'} \\ I_{BS'} \\ I_{CS'} \end{bmatrix} = \begin{bmatrix} I_{AS} \\ I_{BS} \\ I_{CS} \end{bmatrix} - \begin{bmatrix} I_{AS_CC'} \\ I_{BS_CC'} \\ I_{CS_CC'} \end{bmatrix}$$

Positive-sequence current through line is calculated ($I_{1S'_{Pre-fault}}$), and Z_1 is estimated

$$Z_1 = \frac{V_{1S_Pre-fault} - V_{1R_Pre-fault}}{I_{1S'_{Pre-fault}}}$$

Proposed Z_0 estimation method

m_{TW} – TWFL data in per unit; B-susceptance matrix

Current flowing through local end

$$\begin{bmatrix} I_{AS_CC''} \\ I_{BS_CC''} \\ I_{CS_CC''} \end{bmatrix} = m_{TW} \cdot \begin{bmatrix} B_S & B_M & B_M \\ B_M & B_S & B_M \\ B_M & B_M & B_S \end{bmatrix} \cdot \begin{bmatrix} V_{AS} \\ V_{BS} \\ V_{CS} \end{bmatrix}$$

$$\begin{bmatrix} I_{AS''} \\ I_{BS''} \\ I_{CS''} \end{bmatrix} = \begin{bmatrix} I_{AS} \\ I_{BS} \\ I_{CS} \end{bmatrix} - \begin{bmatrix} I_{AS_CC''} \\ I_{BS_CC''} \\ I_{CS_CC''} \end{bmatrix}$$

Current flowing through remote end

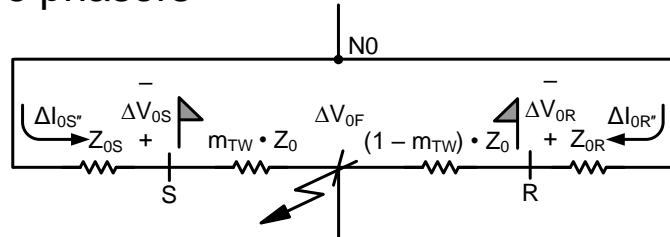
$$\begin{bmatrix} I_{AR_CC''} \\ I_{BR_CC''} \\ I_{RS_CC''} \end{bmatrix} = (1 - m_{TW}) \cdot \begin{bmatrix} B_S & B_M & B_M \\ B_M & B_S & B_M \\ B_M & B_M & B_S \end{bmatrix} \cdot \begin{bmatrix} V_{AR} \\ V_{BR} \\ V_{CR} \end{bmatrix}$$

$$\begin{bmatrix} I_{AR''} \\ I_{BR''} \\ I_{CR''} \end{bmatrix} = \begin{bmatrix} I_{AR} \\ I_{BR} \\ I_{CR} \end{bmatrix} - \begin{bmatrix} I_{AR_CC''} \\ I_{BR_CC''} \\ I_{CR_CC''} \end{bmatrix}$$

Proposed Z_0 estimation method

Incremental zero-sequence phasors

$$\begin{aligned}\Delta V_{0S} &= V_{0S_Faulted} - V_{0S_Pre-fault} \\ \Delta I_{0S''} &= I_{0S''_Faulted} - I_{0S''_Pre-fault} \\ \Delta V_{0R} &= V_{0R_Faulted} - V_{0R_Pre-fault} \\ \Delta I_{0R''} &= I_{0R''_Faulted} - I_{0R''_Pre-fault}\end{aligned}$$

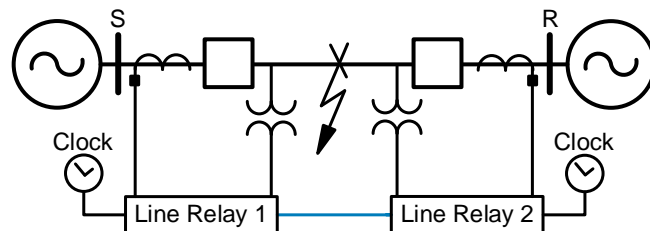


Pure-fault network is used to estimate Z_0

$$Z_0 = \frac{\Delta V_{0S} - \Delta V_{0R}}{m_{TW} \cdot \Delta I_{0S''} - (1 - m_{TW}) \cdot \Delta I_{0R''}}$$

Test setup

- System nominal voltage is 400 kV, and line length is 100 km
- Modeled with CT, CCVT, and 2-cycle circuit breakers
- 81 fault cases using following combinations
 - Load angle (δ): 20° , 1° , -20°
 - Fault resistance (R_f): 0, 10, 40 ohms
 - Fault type: AG, BC, CAG
 - Fault location (m_{TW}): 30, 50, 80 km



Faulted network method

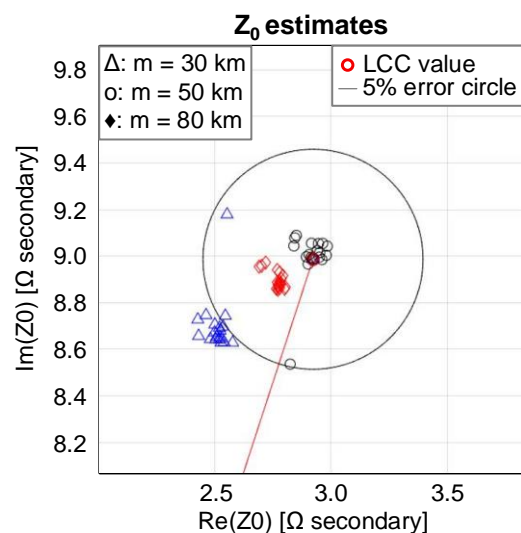
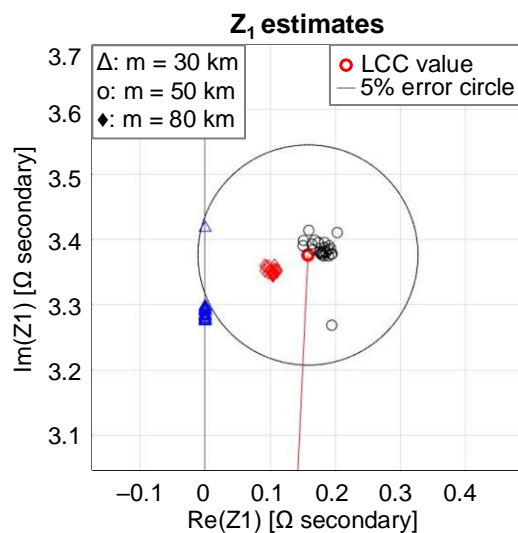
Faulted negative-sequence network is used to estimate Z_1

$$Z_1 = \frac{V_{2S} - V_{2R}}{m_{TW} \cdot I_{2S} - (1 - m_{TW}) \cdot I_{2R}}$$

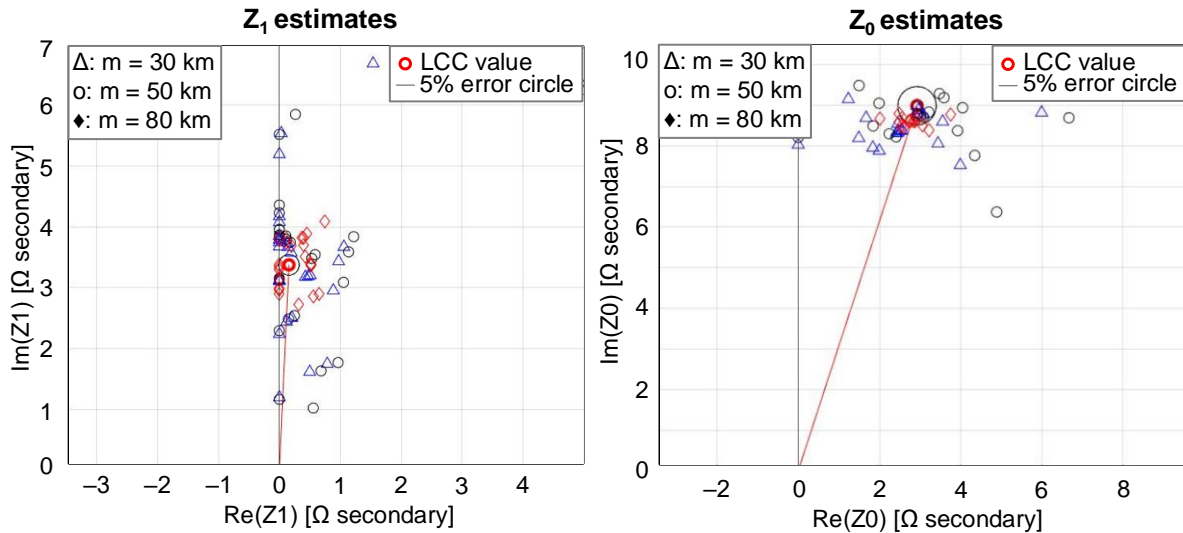
Faulted zero-sequence network is used to estimate Z_0

$$Z_0 = \frac{V_{0S} - V_{0R}}{m_{TW} \cdot I_{0S} - (1 - m_{TW}) \cdot I_{0R}}$$

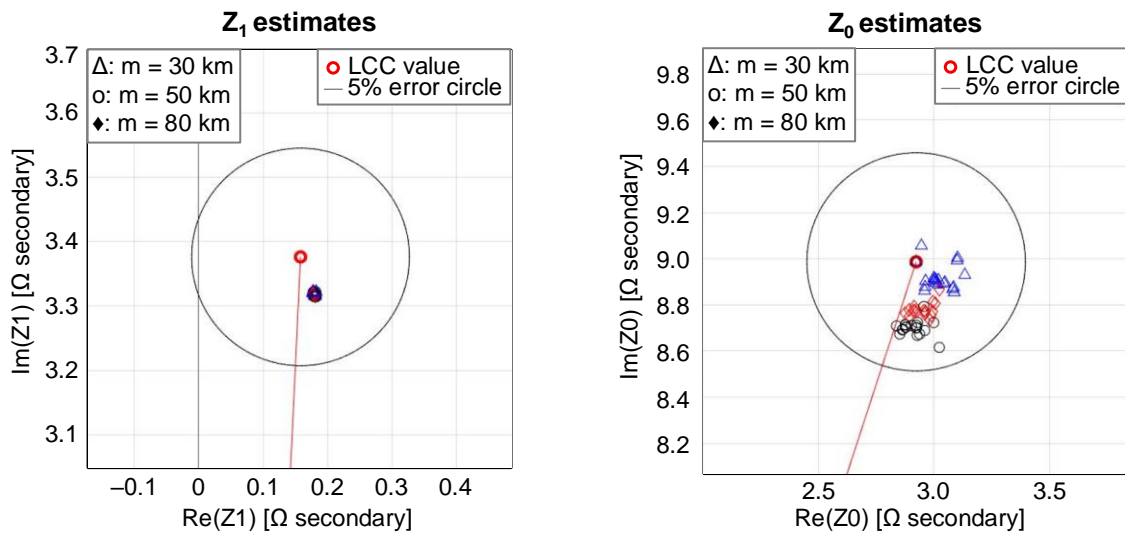
Transposed line model – faulted network method



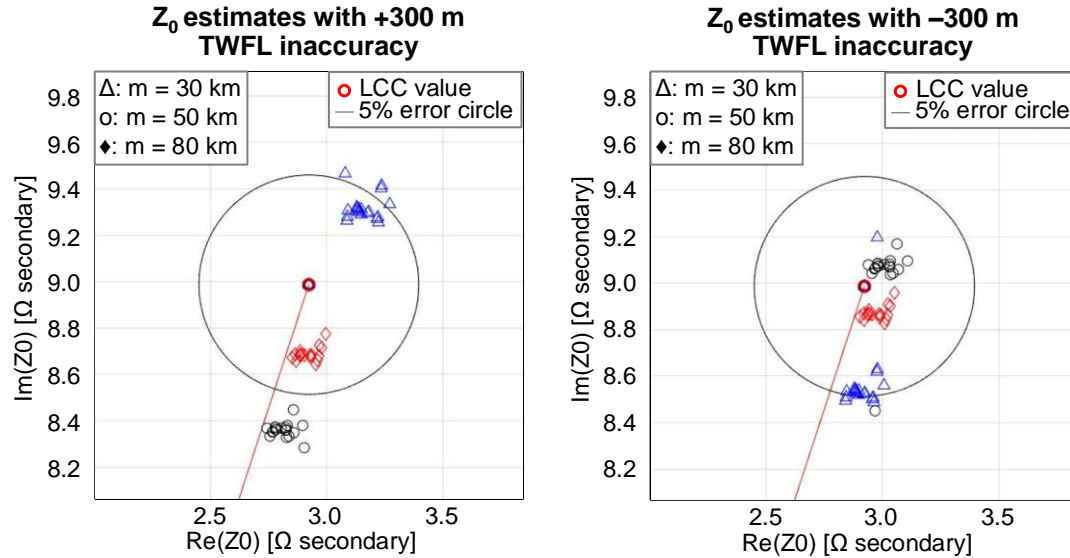
Untransposed line model – faulted network method



Untransposed line model – proposed method



Impact of TWFL inaccuracy



Field event results

Event	Line voltage (kV)	Fault type	Fault location (miles)		Z_1/Z_0 estimates		[Mag error, phase error]
			Actual	DETWFL	Z_1	Z_0	
1	230	CG	61.501 (local), 91.669 (remote)	60.995 (local), 92.175 (remote)	$Z_1 = 22.86 \angle 80.75^\circ$ $Z_0 = 48.81 \angle 73.78^\circ$	$Z_1 = [2.82\%, 0.96^\circ]$ $Z_0 = [4.75\%, 7.35^\circ]$	
2A	220	BG	33.867 (local), 28.085 (remote)	33.837 (local), 28.143 (remote)	$Z_1 = 5.70 \angle 76.94^\circ$ $Z_0 = 12.32 \angle 72.68^\circ$	$Z_1 = [9.19\%, 2.59^\circ]$ $Z_0 = [3.08\%, 3.05^\circ]$	
2B	220	BG	33.867 (local), 28.085 (remote)	33.908 (local), 28.072 (remote)	$Z_1 = 5.63 \angle 80.09^\circ$ $Z_0 = 11.92 \angle 73.17^\circ$	$Z_1 = [7.99\%, 0.55^\circ]$ $Z_0 = [6.29\%, 2.57^\circ]$	
3	115	AG	3.1 (local), 54.66 (remote)	3.199 (local), 54.504 (remote)	$Z_1 = 6.1488 \angle 70.25^\circ$ $Z_0 = 17.52 \angle 78.48^\circ$	$Z_1 = [4.04\%, 1.04^\circ]$ $Z_0 = [7.63\%, 9.28^\circ]$	
4	132	AB	32.593 (local), 26.443 (remote)	32.665 (local), 26.375 (remote)	$Z_1 = 2.72 \angle 63.11^\circ$	$Z_1 = [4.24\%, 0.88^\circ]$	

Phenomena that impacts accuracy

- Z_1 estimates are sensitive to CT and PT errors at low load angle conditions
- Evolving faults, CT saturation, CCVT transients, faults with time varying resistance, and fast breaker operation impact accuracy of Z_0 estimates
- Inaccuracies in TWFL have direct impact on accuracy of Z_0 estimates
- Proposed method does not account for coupling of positive-sequence and negative-sequence quantities on pure-fault zero-sequence networks, which in turn, impacts Z_0 accuracy
- Proposed method cannot be applied on mutually coupled lines

Conclusion

- Pre-fault positive-sequence quantities and PI equivalent line model are used for Z_1 estimates
- Incremental zero-sequence quantities and pure-fault zero-sequence network are used for Z_0 estimates
- Proposed method provides better Z_0 estimates for both transposed and untransposed lines



Questions?