

# Performance Comparison Between Mho Elements and Incremental Quantity-Based Distance Elements

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# Overview

- Present characteristics of incremental distance in impedance plane
- Compare performance of mho elements and incremental distance elements based on their characteristics
- Compare performance with series compensation
- Discover issues with mutually coupled lines and three-terminal lines

# Superposition Principle

CT Ratio: 240/1

VT Ratio: 2,000/1

All impedances in primary values

230 kV System

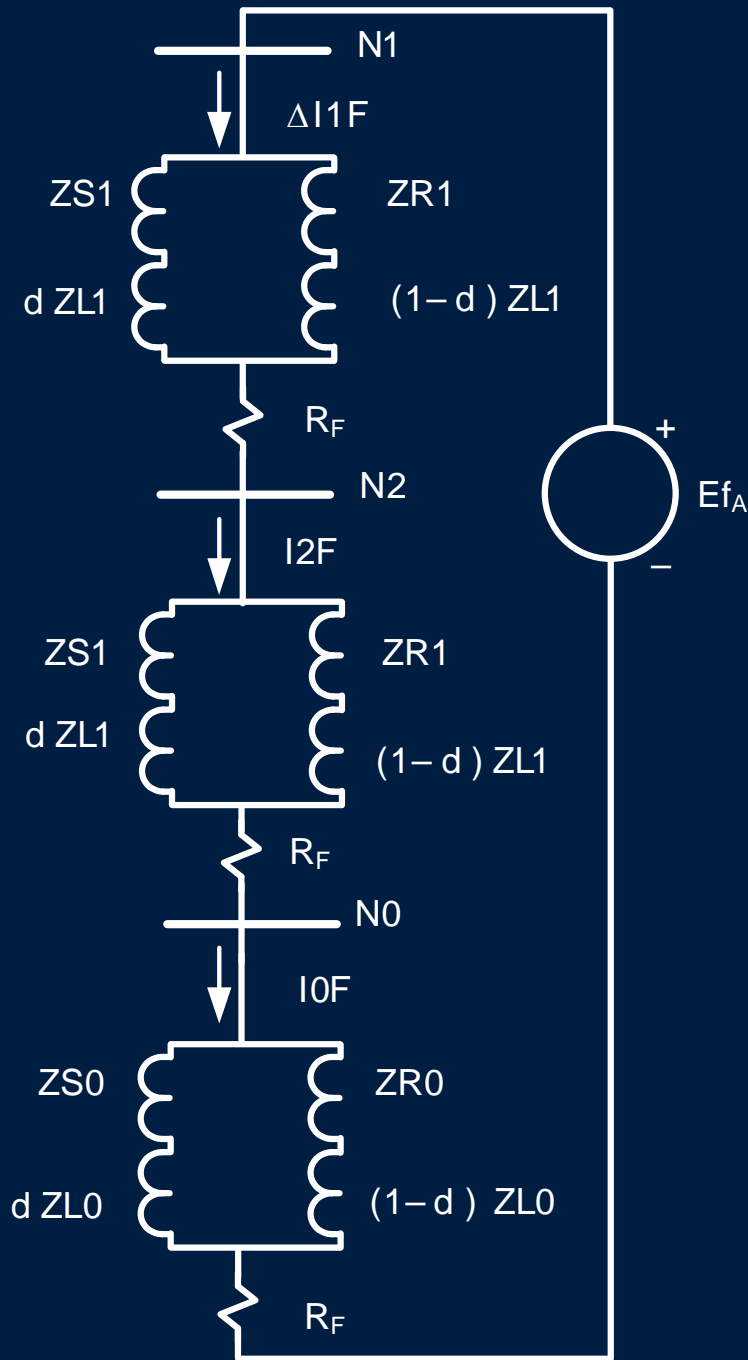
$Z_{L1} = 17.47 \text{ (} 86^\circ \text{) ohms}$

$Z_{L0} = 62.47 \text{ (} 75.38^\circ \text{) ohms}$



# Single-Phase Faults

## Pure-Fault Sequence Network



$$V = V_{PF} + \Delta V$$

$$I = I_{PF} + \Delta I$$

$$E_{f_A} = VM - (Z_{S1} + d \cdot Z_{L1}) \cdot I_{LD}$$

$$E_{f_A} = VA_{PF} - d \cdot Z_{L1} \cdot I_{LD} =$$

$$-\Delta VA + d \cdot Z_{L1} \cdot (\Delta IA + K_0 \cdot I_0) + 3R_F \cdot \Delta I_{1F}$$

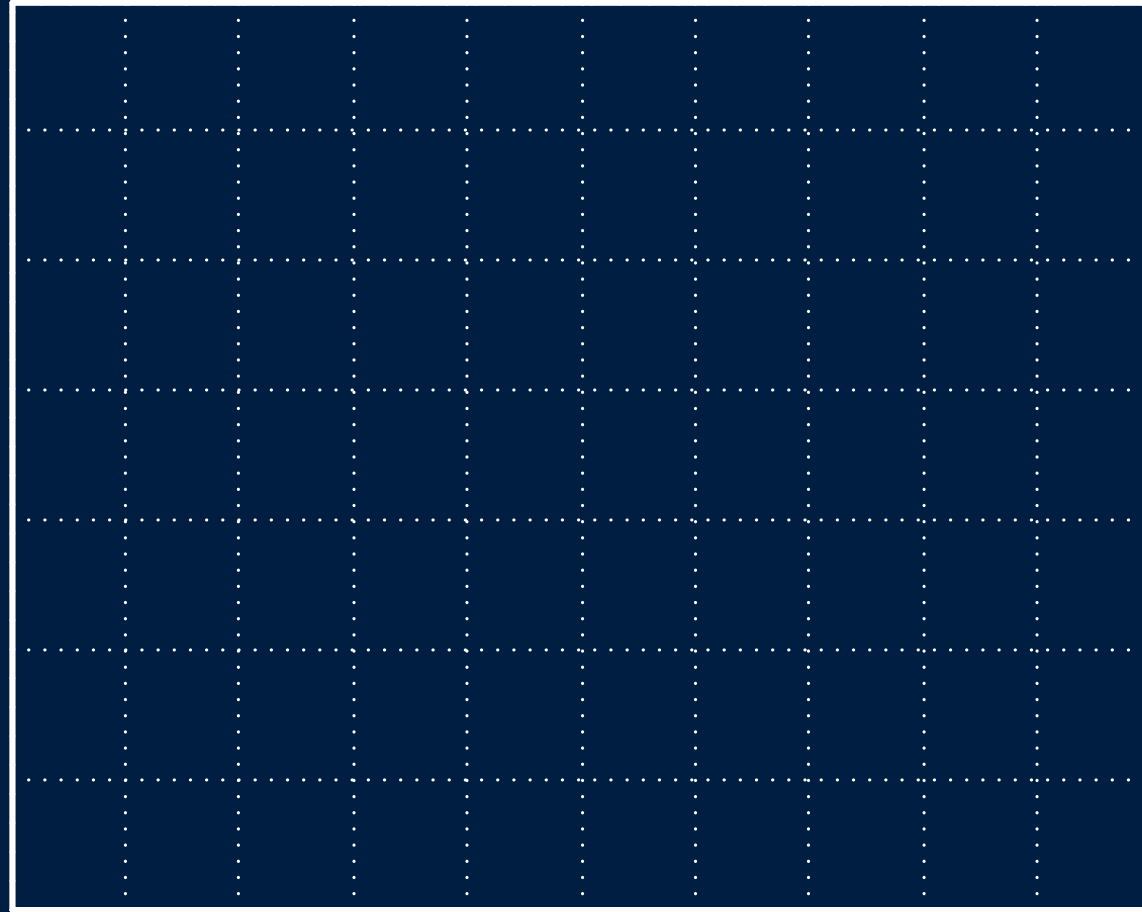
# Incremental Distance Principle

$$E_{f_A} = V_{A_{PF}} - d \cdot Z_{L1} \cdot I_{LD} =$$
$$-\Delta V_A + d \cdot Z_{L1} \cdot (\Delta I_A + K_0 \cdot I_0) + 3R_F \cdot \Delta I_{1F}$$

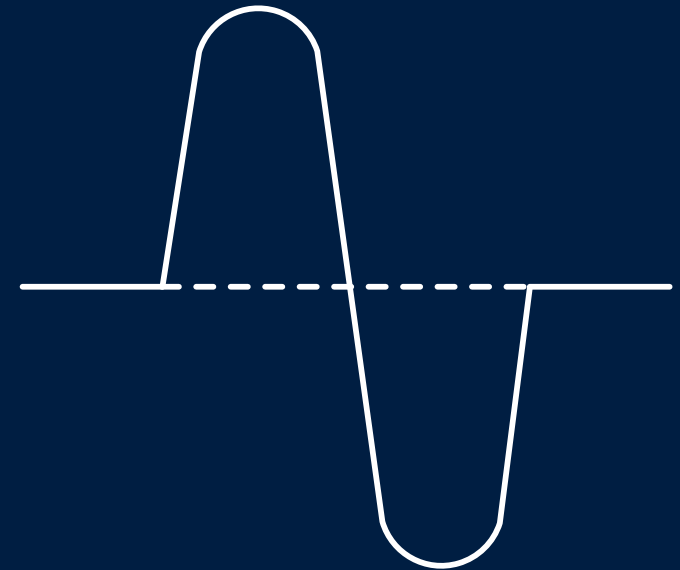
$$V_{f_{AG}} = V_{A_{PF}} - r \cdot Z_{1L} \cdot I_{A_{PF}}$$

$$V_{d_{AG}} = -\Delta V_A + r \cdot Z_{1L} \cdot (\Delta I_A + K_0 \cdot I_0)$$

# Variation of $Vf_{AG}$ and $Vd_{AG}$ ( $r = 80\%$ )



# Simple Delta Filter



# Delta Filters

- Delta filters provide  $\Delta V$  and  $\Delta I$  during a time interval equal to the delay  $\tau$  following a fault
- Delta filters can be used either in frequency domain with phasors or in time domain (high- and ultra-high-speed applications)
- Output is zero in steady state
- Limitations are cascading events, evolving faults, and switch-on-to-fault situations



# Incremental Distance Three-Phase Fault Characteristics

$$E_{f_A} = -\Delta V_A + d \cdot Z_{L1} \cdot \Delta I_A + R_F \cdot \Delta I_F$$

$$V_{d_A} = -\Delta V_A + r \cdot Z_{L1} \cdot \Delta I_A$$

$$E'_{f_A} = \frac{E_{f_A}}{\Delta I_A} = Z_{S1} + d \cdot Z_{L1} + \frac{R_F}{C1} = Z_{S1} + Z_{APP\_NLD}$$

$$V'_{d_A} = \frac{V_{d_A}}{\Delta I_A} = Z_{S1} + r \cdot Z_{L1}$$

# Incremental Distance Three-Phase Fault Characteristics

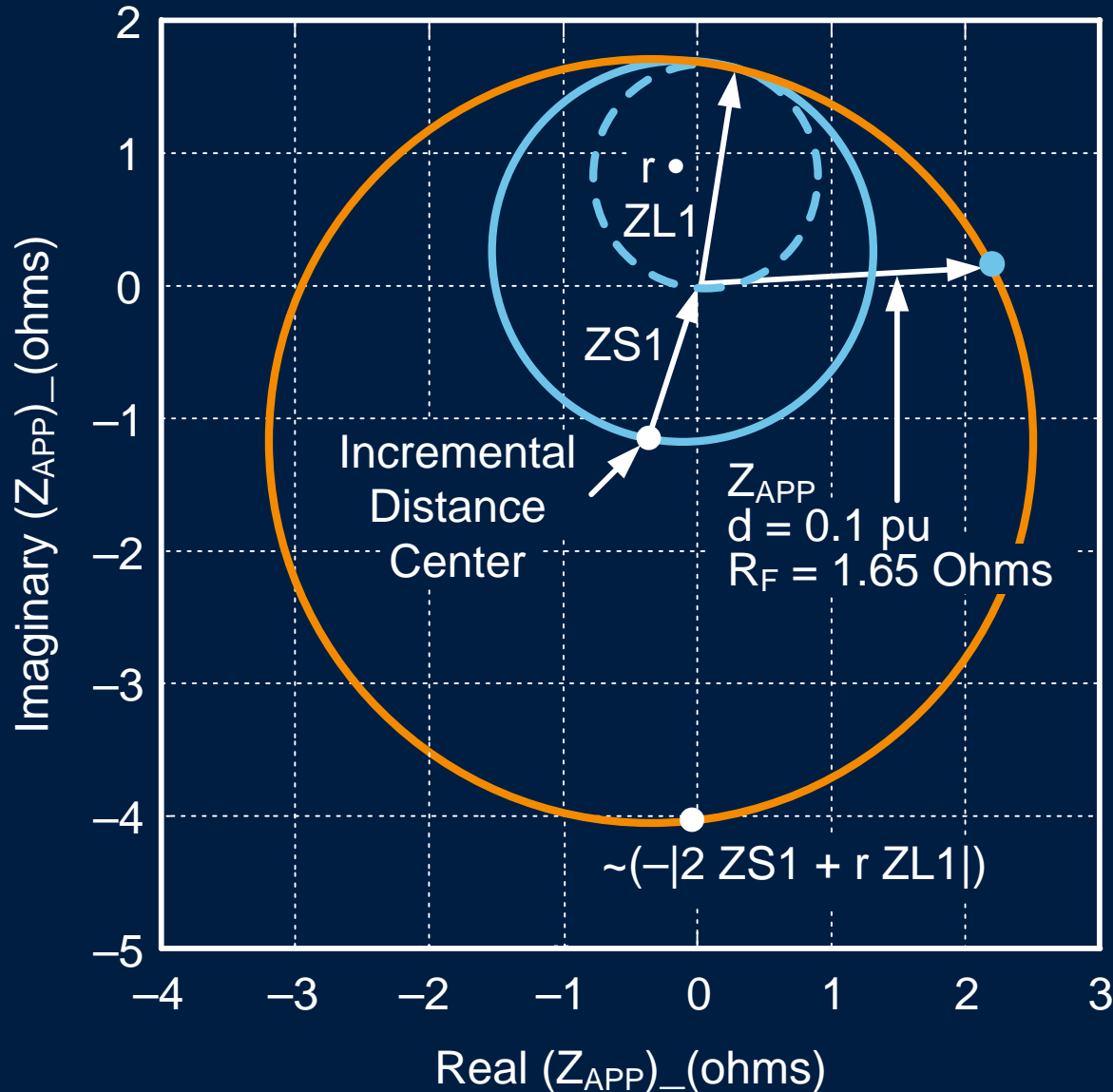
$$|(ZS1 + r \cdot Z1L)| \geq |(ZS1 + Z_{APP\_NLD})|$$

$$x_0 = -\text{real}(ZS1)$$

$$y_0 = -\text{imag}(ZS1)$$

$$R = |(ZS1 + r \cdot ZL1)|$$

# Three-Phase Fault Characteristics

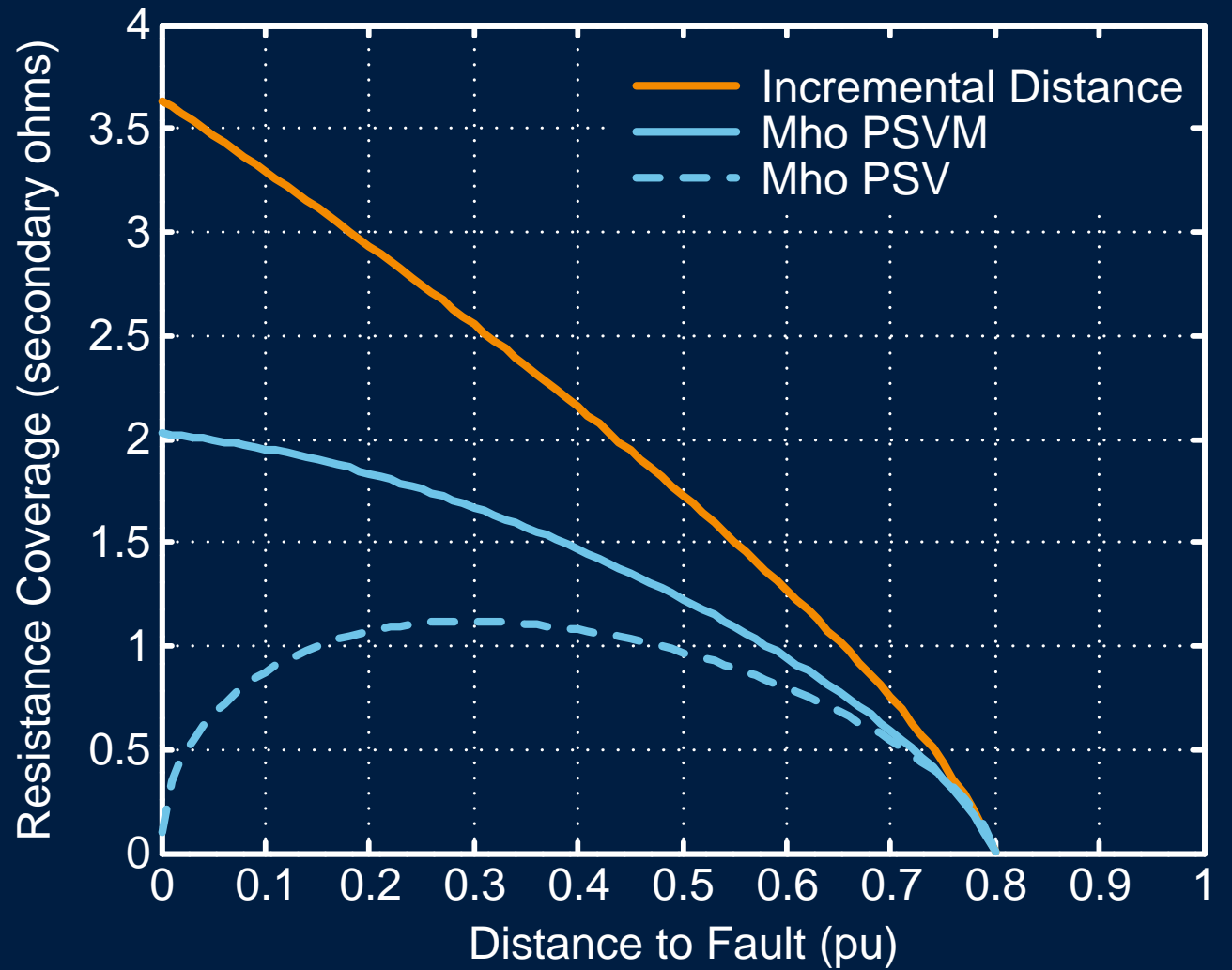
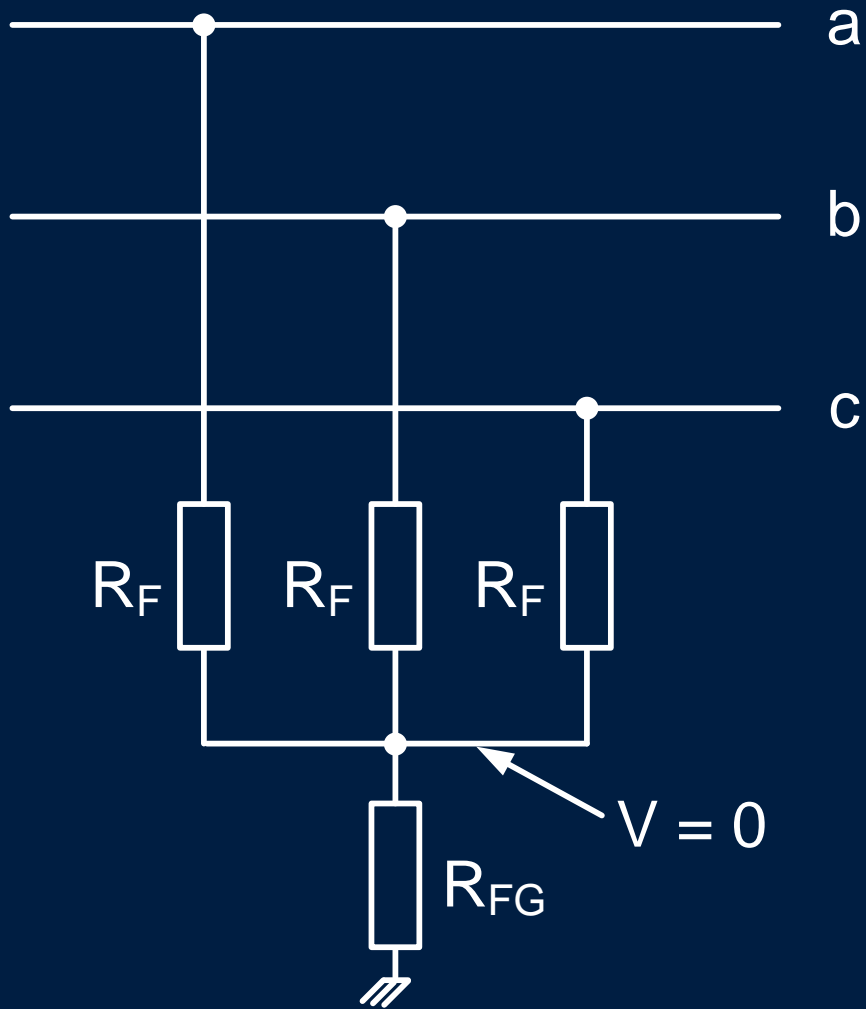


$$Z_{APP\_NLD} (d = 0.1, R_F = 1.6465) = \frac{VA}{\Delta IA} = d \cdot ZL1 + \frac{R_F}{C1} = (2.199 + j0.147) \Omega$$

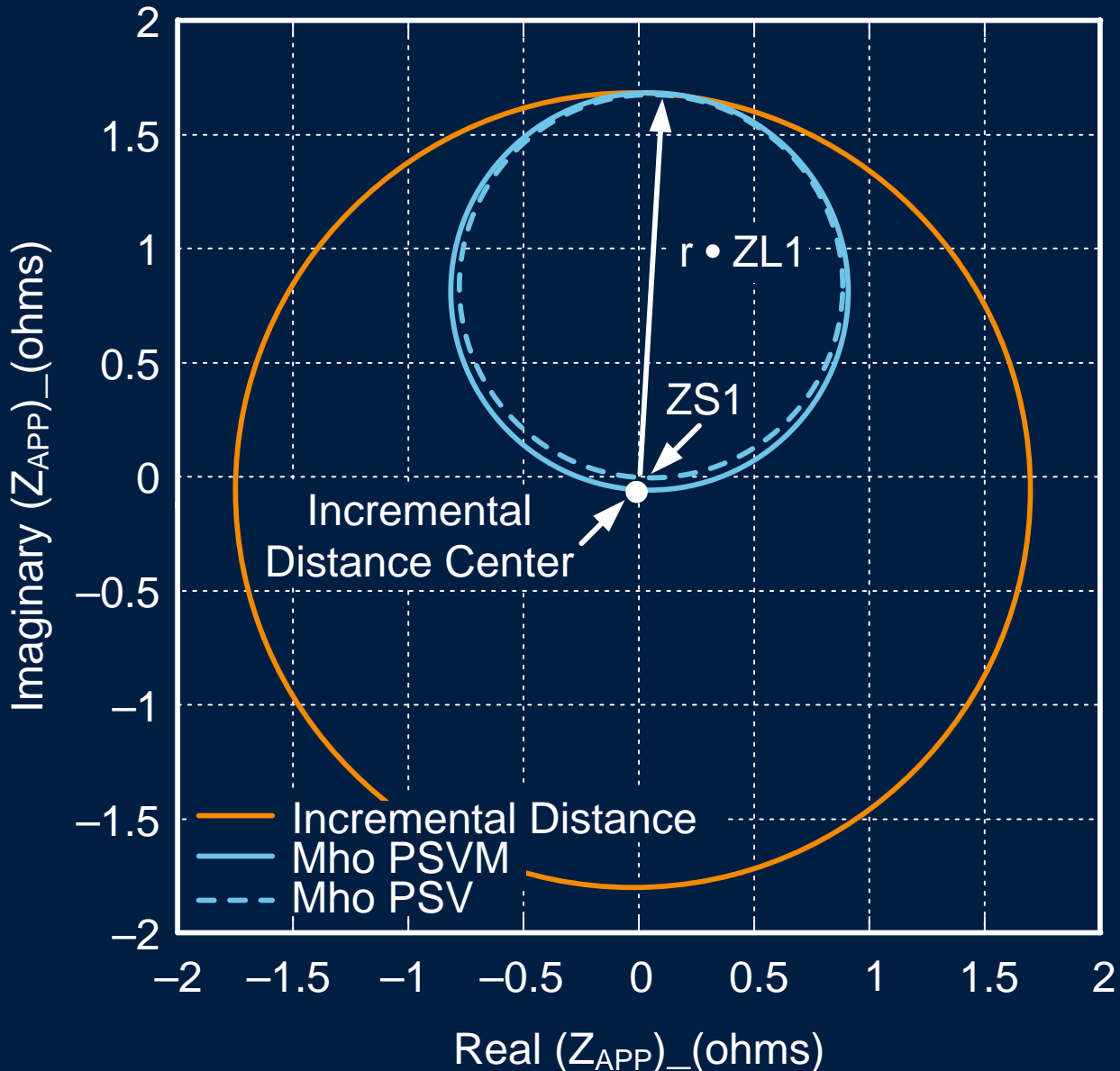
- Incremental Distance
- Mho PSVM
- - - Mho PSV

# Three-Phase Faults

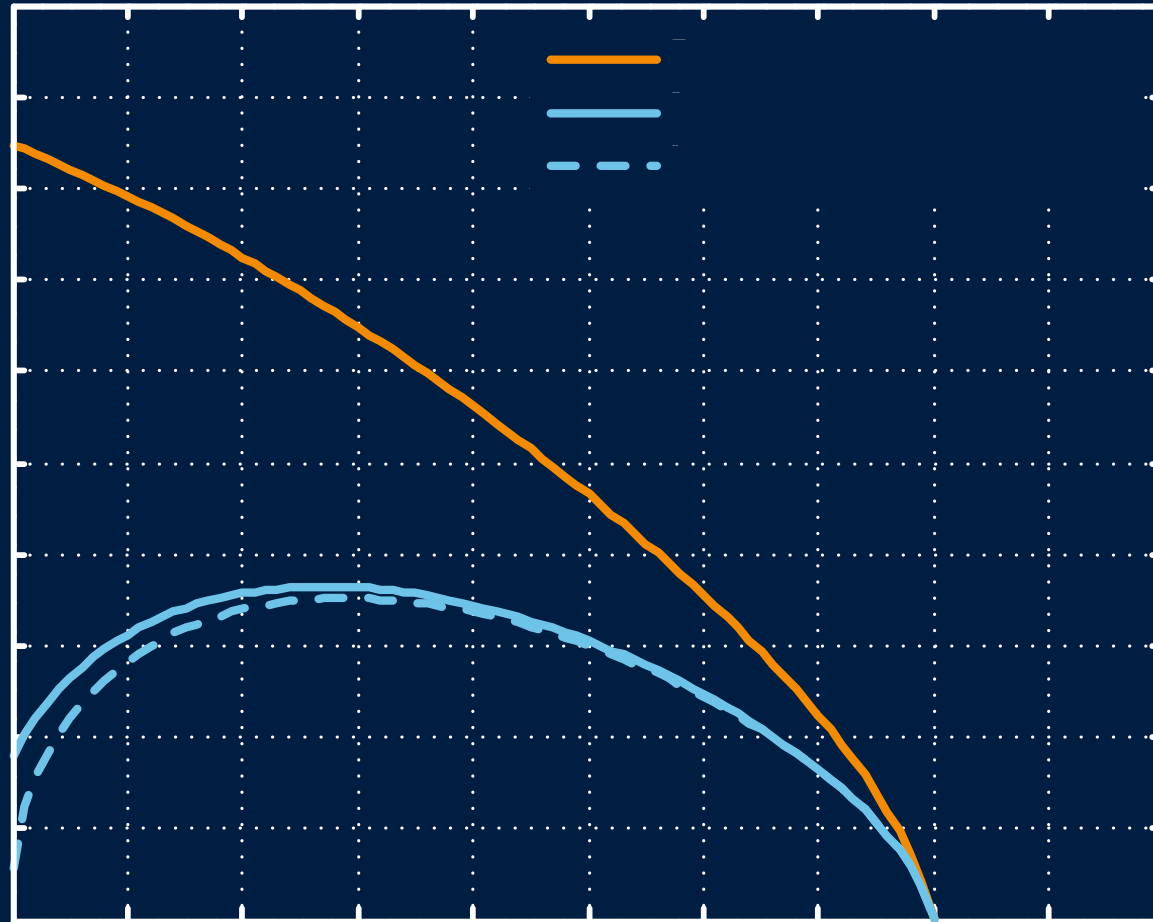
## Resistance Coverage



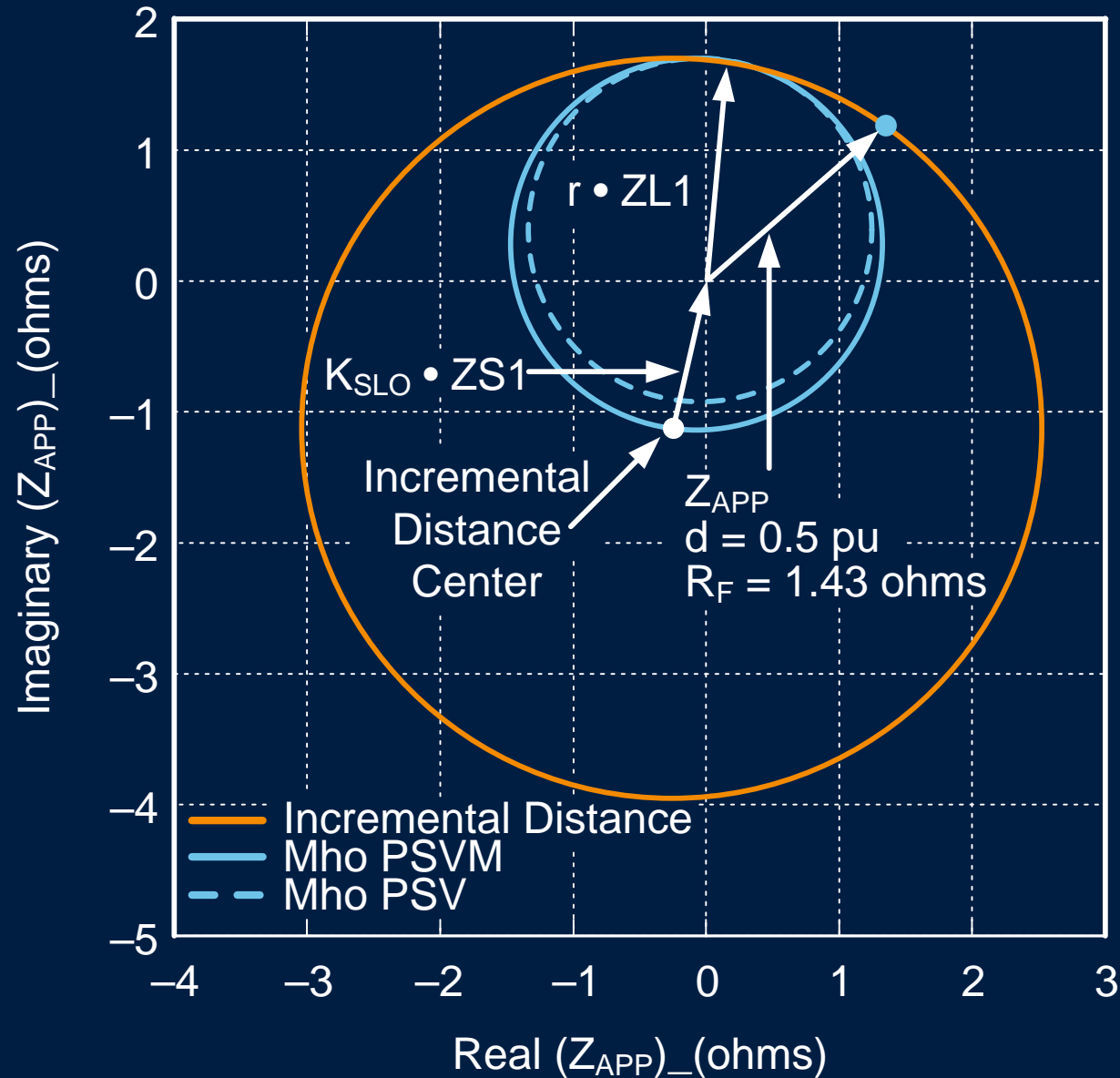
# Three-Phase Fault With ZS1 Divided by 20



# Three-Phase Fault Resistance Coverage With ZS1 Divided by 20



# Single-Phase Fault Characteristics



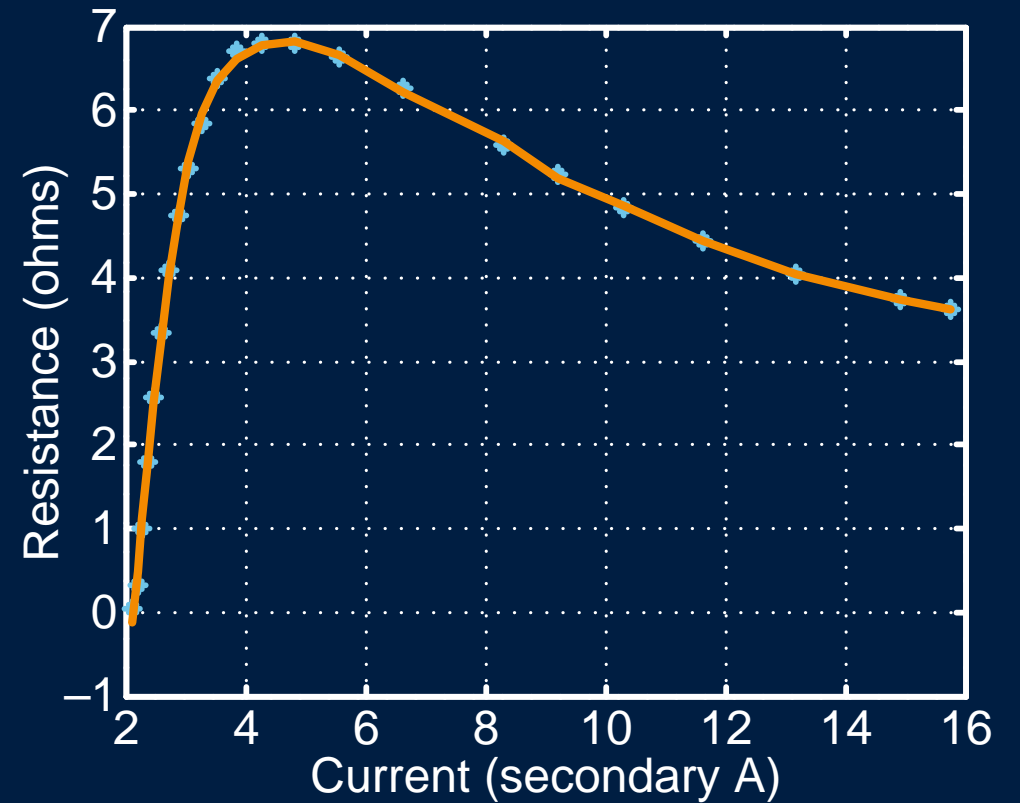
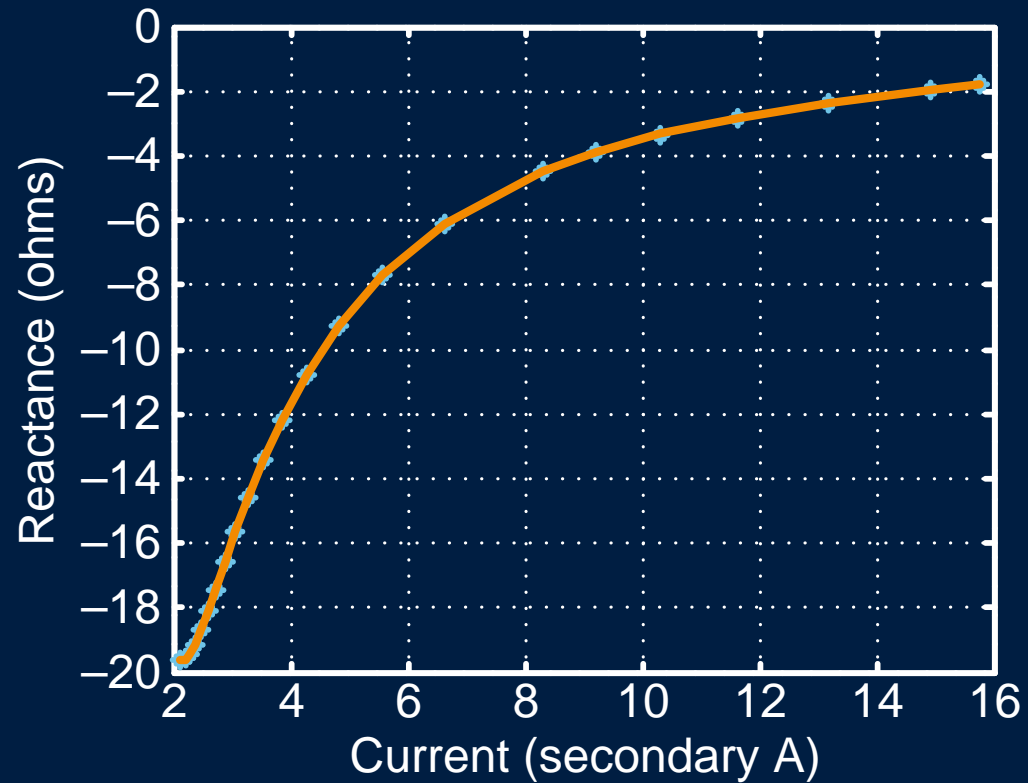
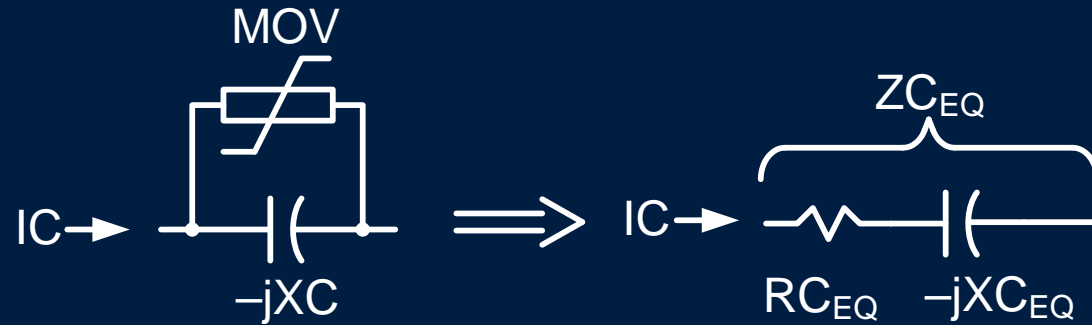
# Distance Element Characteristics

- Mho element characteristics in impedance plane always exist
- Incremental distance element characteristics in impedance plane are defined only if  $\Delta V$  and  $\Delta I$  are non-zero (they do not exist in steady state)
- In steady state, mho element asserts for overload condition (incremental distance element does not)



# Series Compensation

# MOV / Capacitor Equivalent



# Voltage Inversion

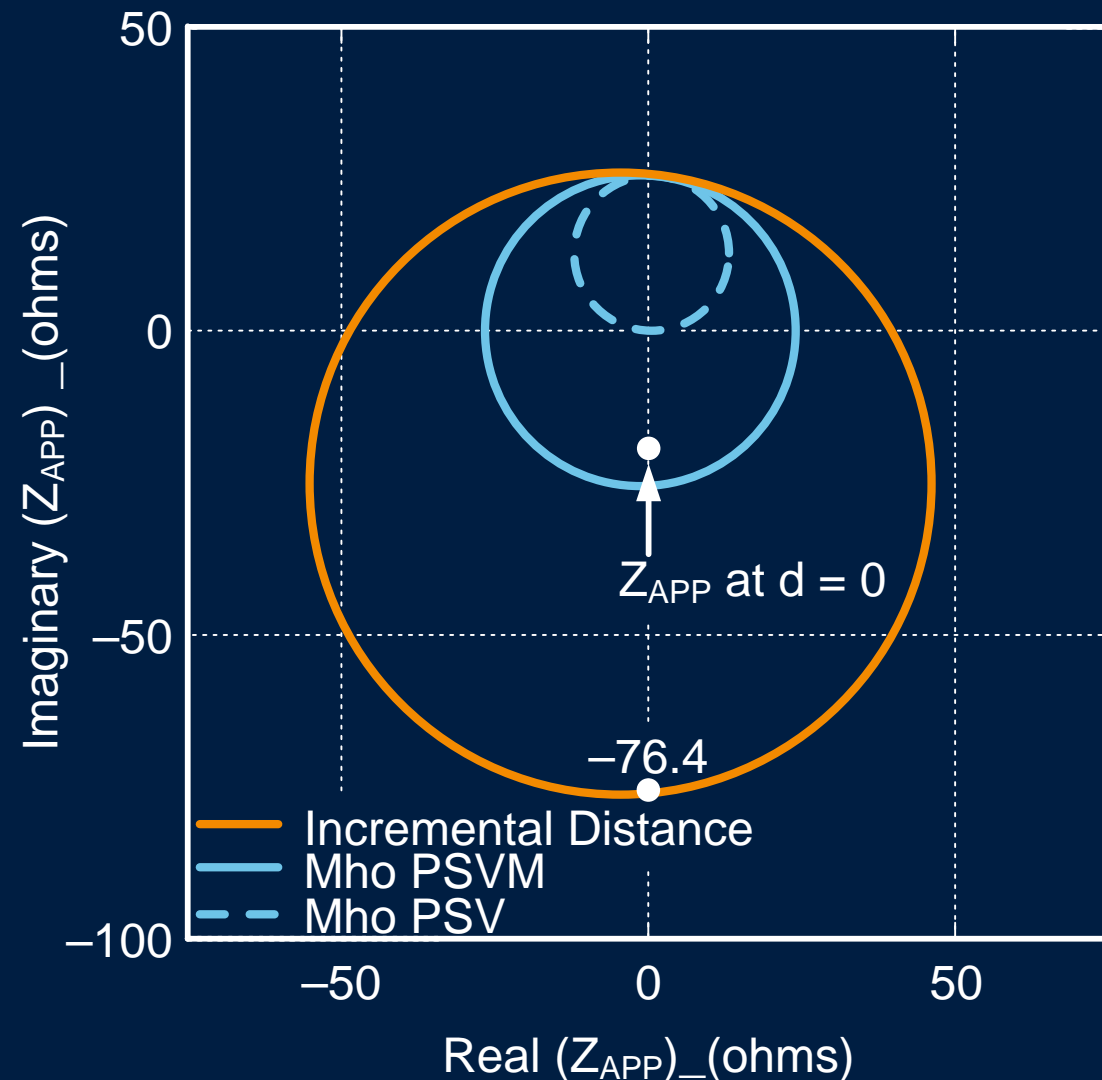
No MOV,  $d = 0$ ,  $R_F = 0$

$$|Z_{C_{EQ}}| > |d \cdot Z_{L1}|$$

$$|Z_{S1} + d \cdot Z_{L1}| > |Z_{C_{EQ}}|$$

$$|-j19.6| \text{ ohms} > 0$$

$$25.4 \text{ ohms} > |-j19.6| \text{ ohms}$$

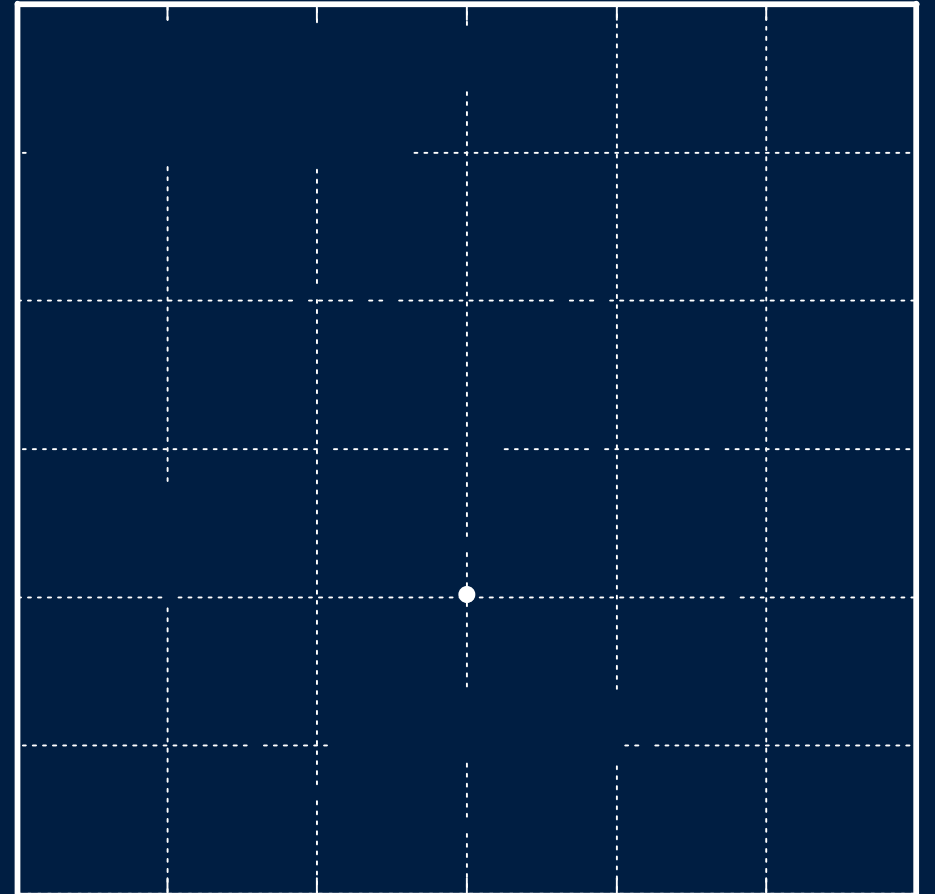


# Current Inversion

No MOV,  $d = 0$ ,  $R_F = 0$ ,  $Z_{S1}$  Divided by 2

$$|Z_{C_{EQ}}| > |Z_{S1} + d \cdot Z_{L1}|$$

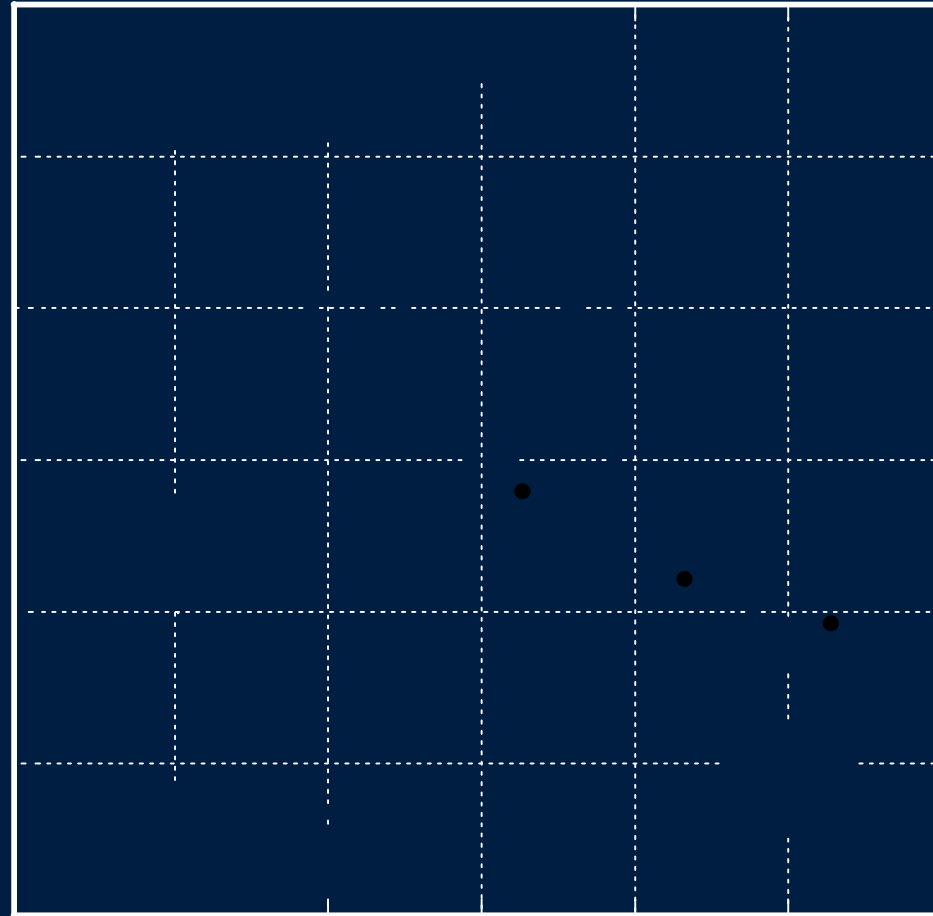
$$|-j19.6| \text{ohms} > 12.7 \text{ohms}$$



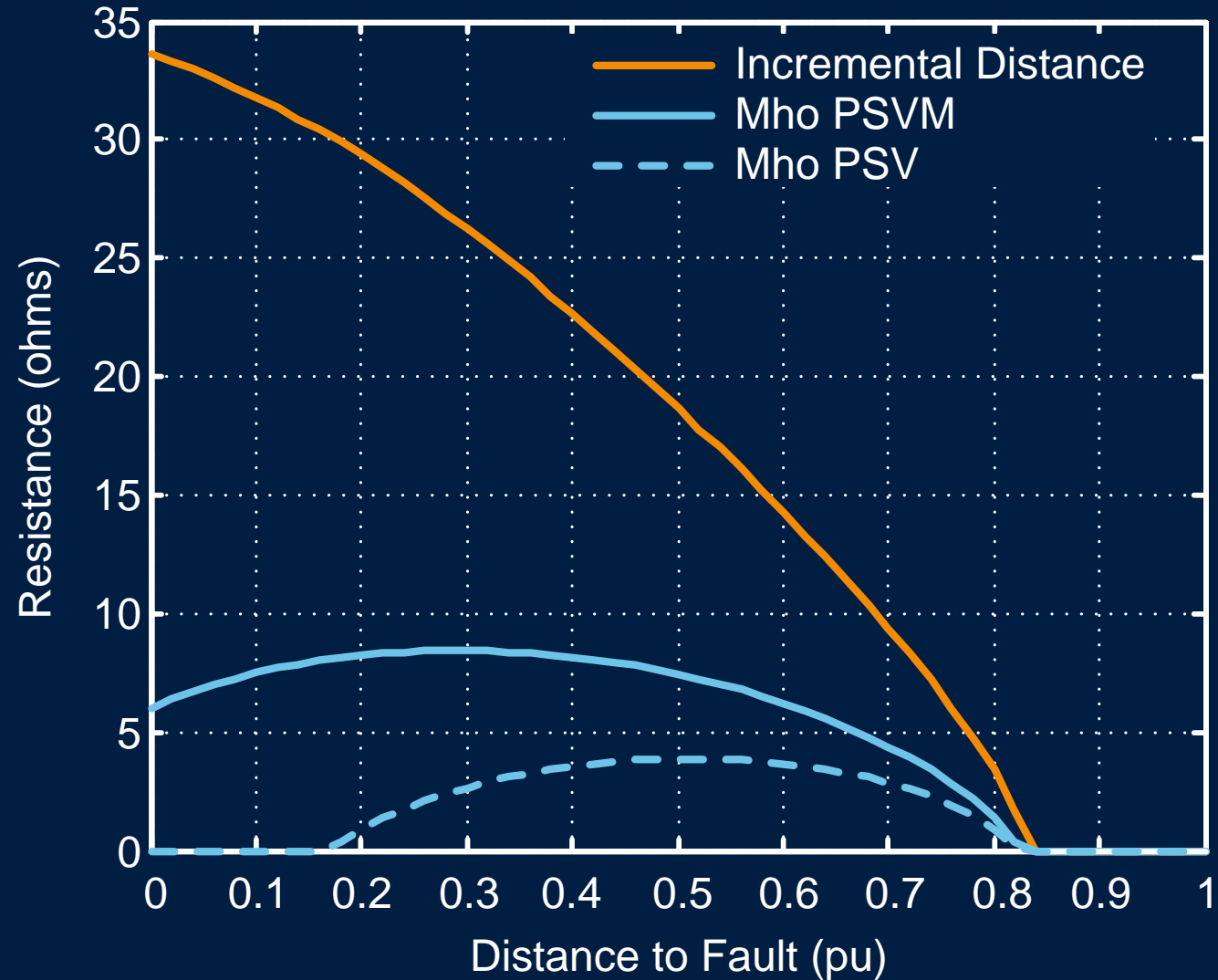
# Linearized Sequence Network for Three-Phase Fault

# Apparent Impedances for Three-Phase Fault

$d = 0, r = 50\%$

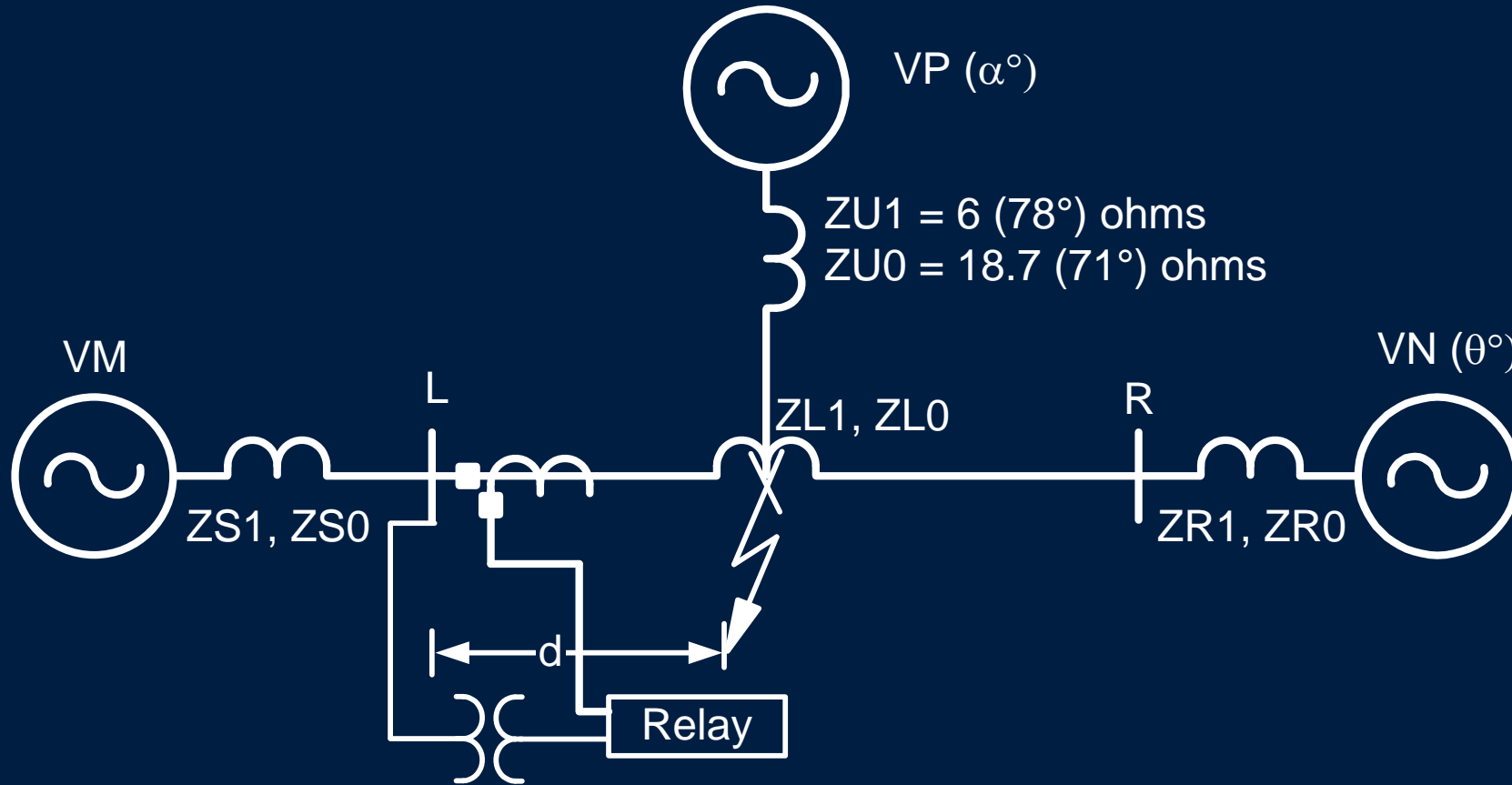


# Three-Phase Fault Resistance Coverage



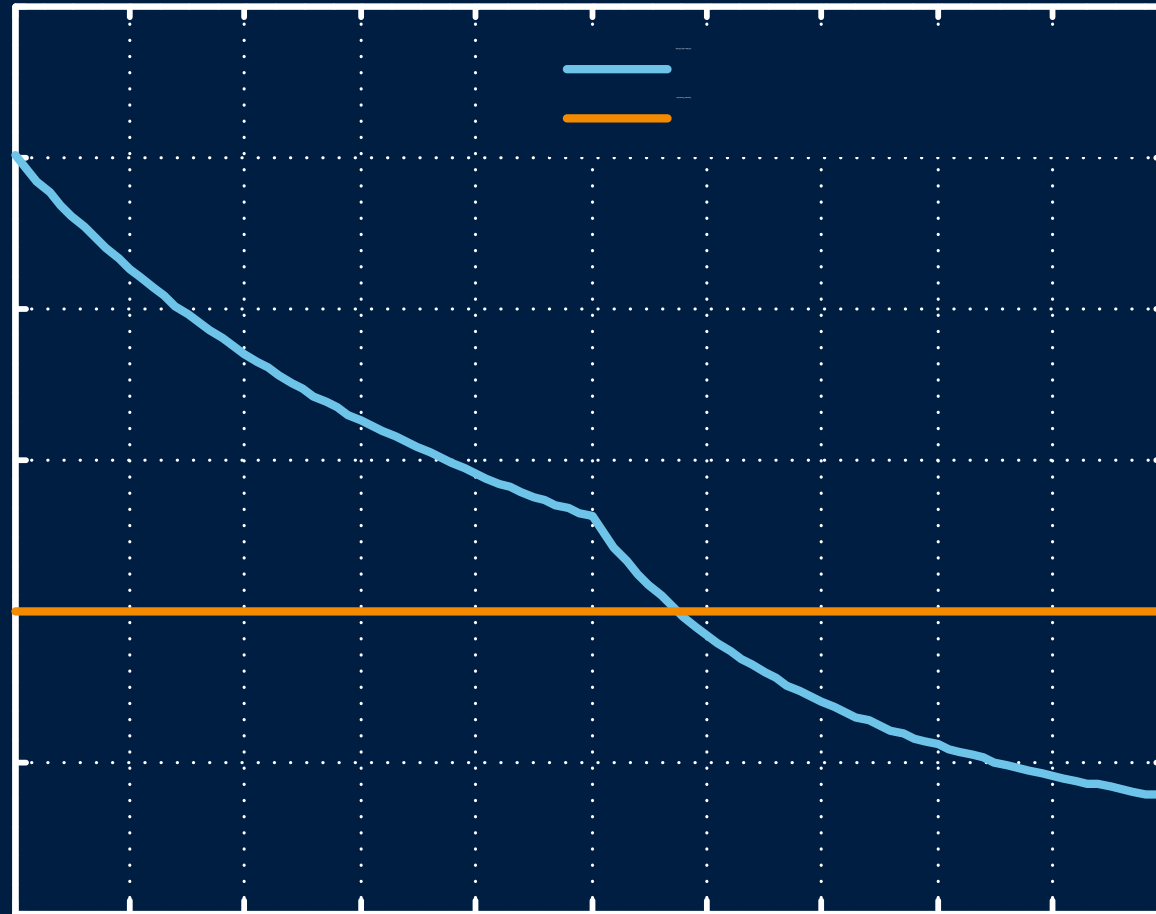
# Impact of Element Reach

## Example of Remote Infeed

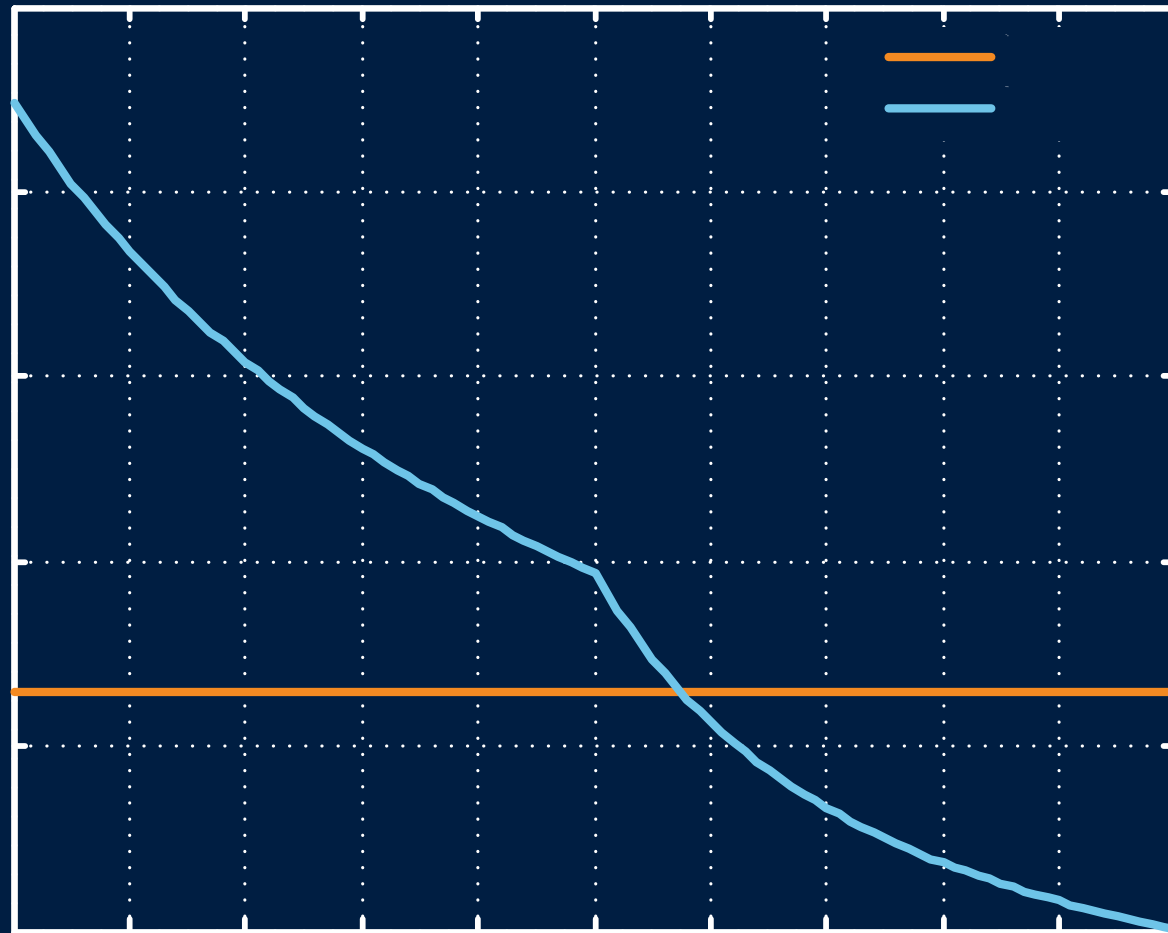




# Mho AB Loop Scalar Product for Three-Phase Fault Applied From $d = 0$ to 1 pu



# $V_{f_{AB}}$ and $V_{d_{AB}}$ for Three-Phase Fault Applied From $d = 0$ to 1 pu



# Conclusion

- Incremental distance characteristics do not exist in steady state
- Incremental distance elements have increased sensitivity, increased resistance coverage, and immunity to voltage or current inversion
- Incremental distance element reach is affected in same way as mho elements (series compensation, remote infeed or outfeed, and parallel lines)

# Conclusion

- Limits of incremental distance elements are limits imposed by delta filters (window typically of 1 cycle)
- Optimal configuration consists of mho element that is parallel with incremental distance element (high- or ultra-high-speed element with slower conventional mho element backup)
- Single comparator was considered in the study

**Questions?**