

# **A Tutorial on Ferroresonance**

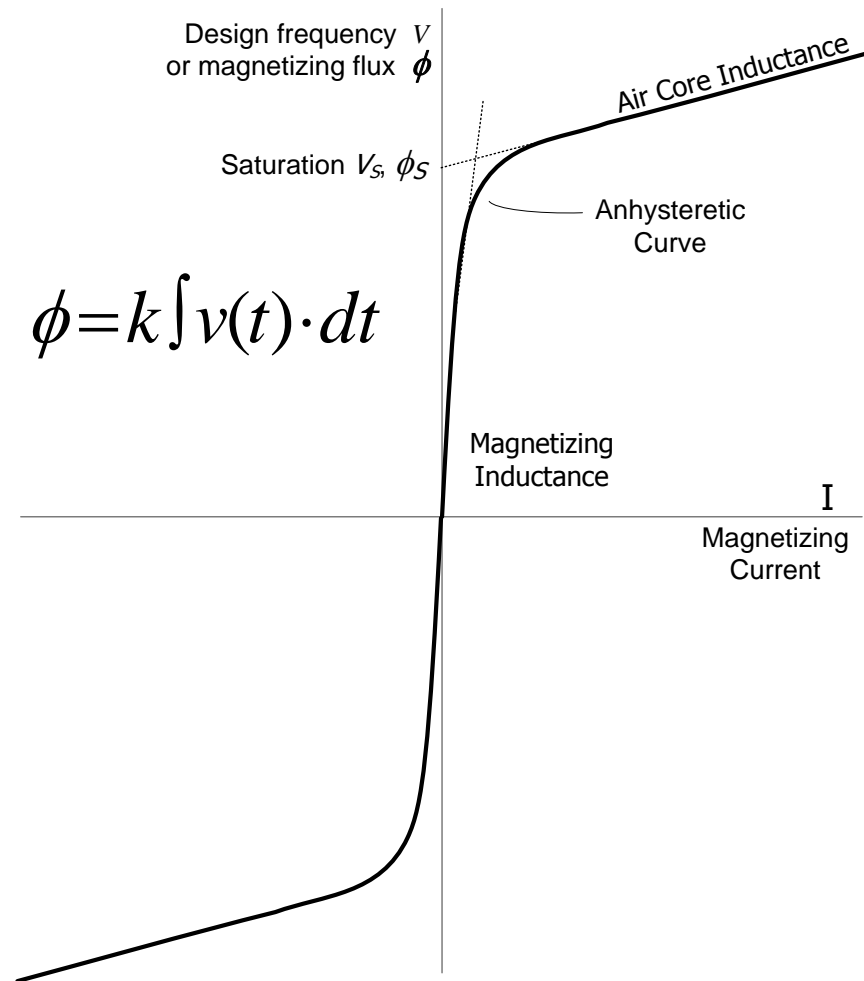
**Elmo Price**

ABB Inc.

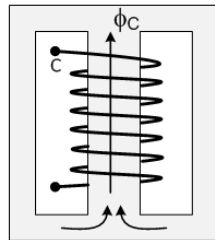
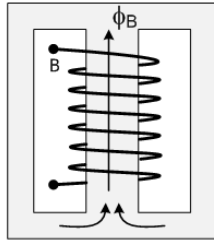
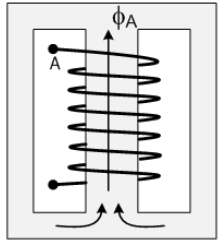
# Introduction

- Occurs in power system circuits containing series capacitance, a non-linear transformer magnetizing inductance and minimum transformer and load losses
- Initiated with transient disturbance such as opening a switch
- Results in overvoltages and/or high current spikes that may subject system apparatus to dielectric and thermal stresses resulting in apparatus failure
- Poses risk to operating personnel
- Protective relays that measure these quantities are subject to incorrect operations causing unwanted outages
- This presentation will present a simple tutorial with a graphical approach to explaining the ferroresonant operating states, circuit configurations and mitigation.
- It will provide the basic concepts necessary to understanding more advanced investigations into unique occurrences.

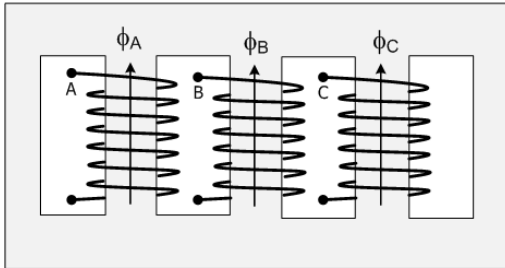
# Transformer Characteristics



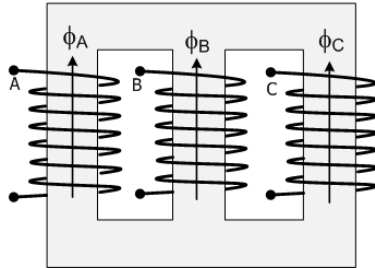
# Transformer Core and Coil



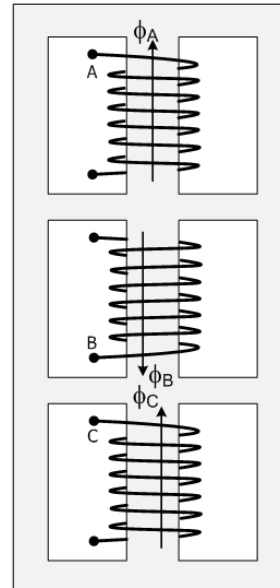
(a) Three single phase cores



(b) Three phase five legged core form



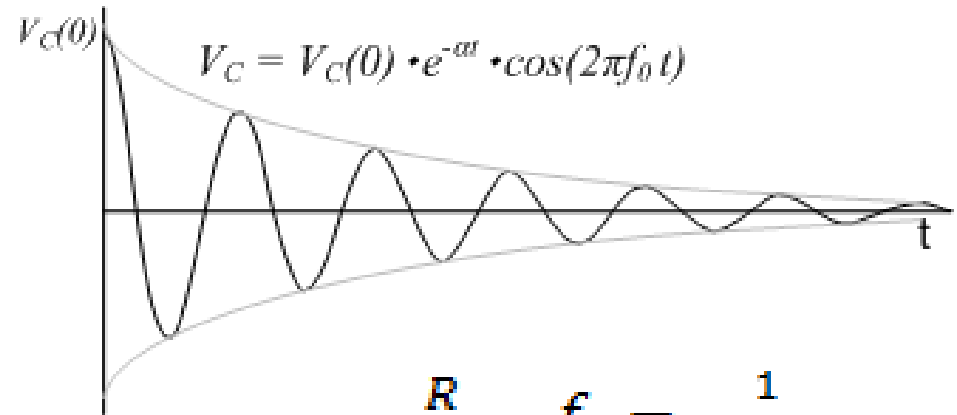
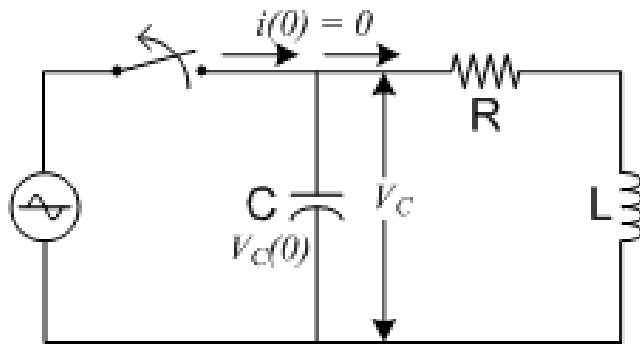
(c) Three phase three legged core form



(d) Three phase shell form

- Magnetic coupling between phases
  - Core construction
  - Winding connections
  - Core bracing, joints, etc.
- Phase flux saturation
- Zero sequence flux saturation

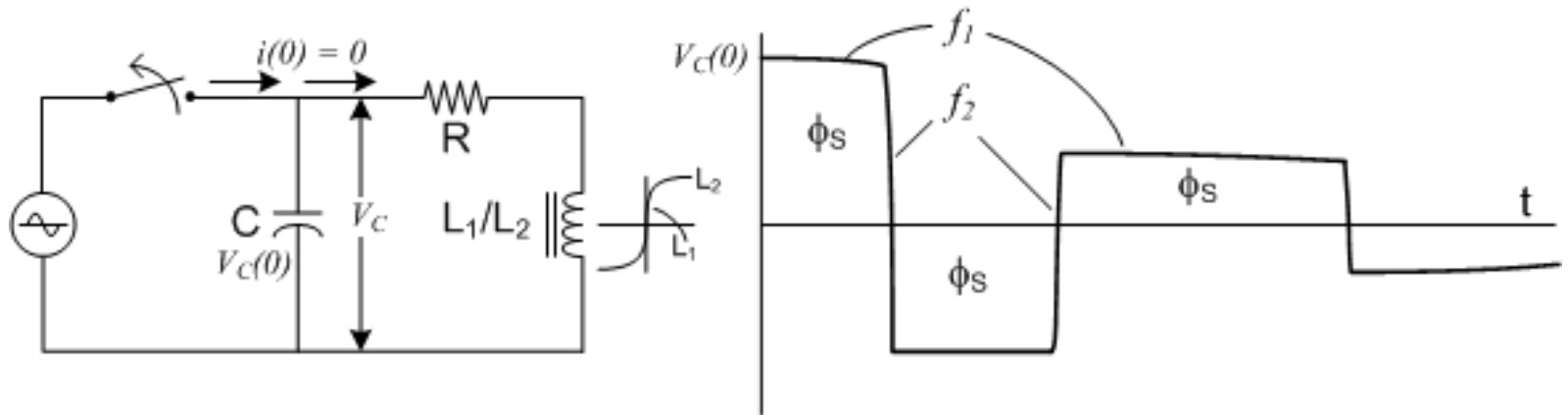
# RLC Circuit and Transient Response



$$\alpha = \frac{R}{2L} \quad f_0 = \frac{1}{2\pi\sqrt{LC}}$$

# RL<sub>1/2</sub>C Circuit and Transient Response

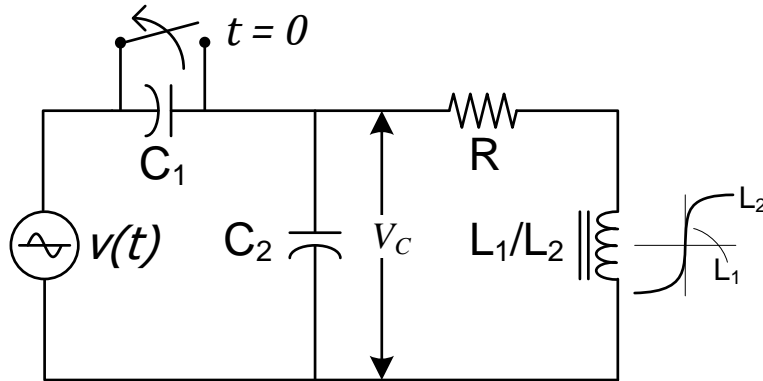
(L<sub>1/2</sub> is nonlinear transformer inductance)



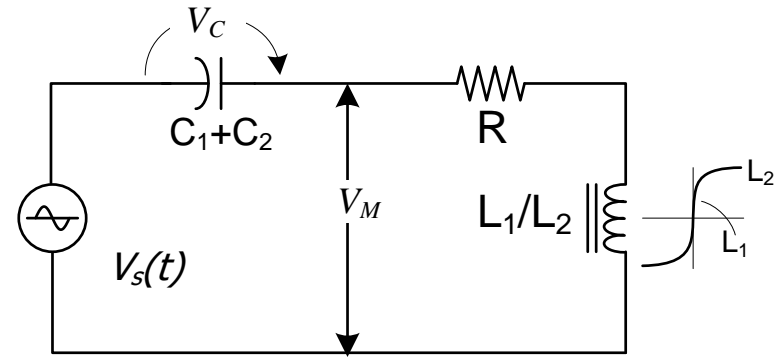
$$f_1 = \frac{1}{2\pi\sqrt{L_1 C}}$$

$$f_2 = \frac{1}{2\pi\sqrt{L_2 C}}$$

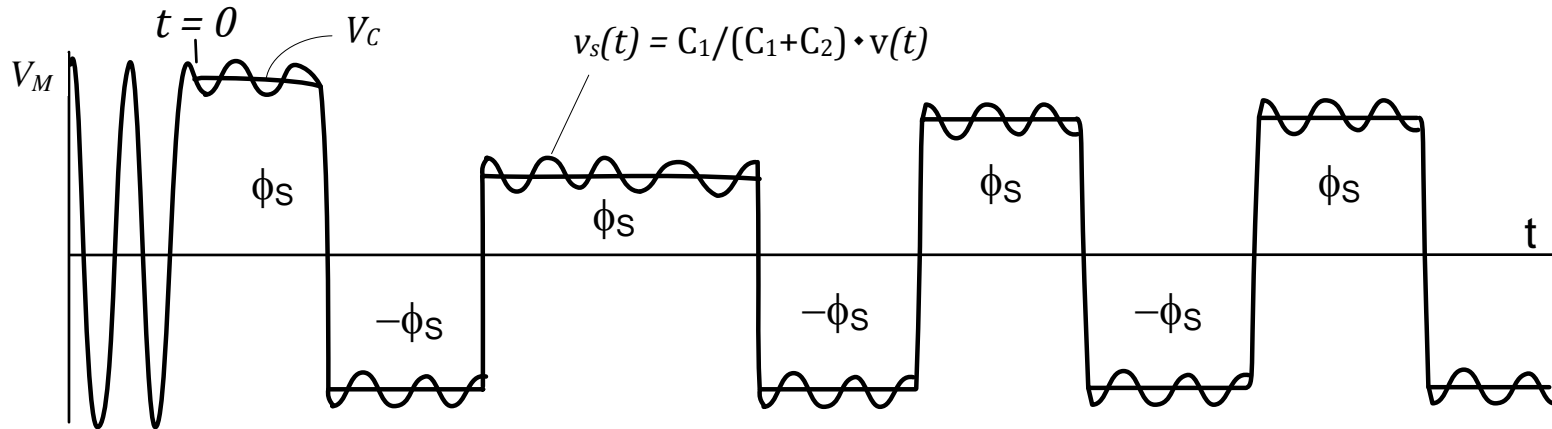
# RL<sub>1/2</sub>C Circuit with Driving Voltage and Transient Response



(a) RLC circuit with saturating inductance and driving voltage

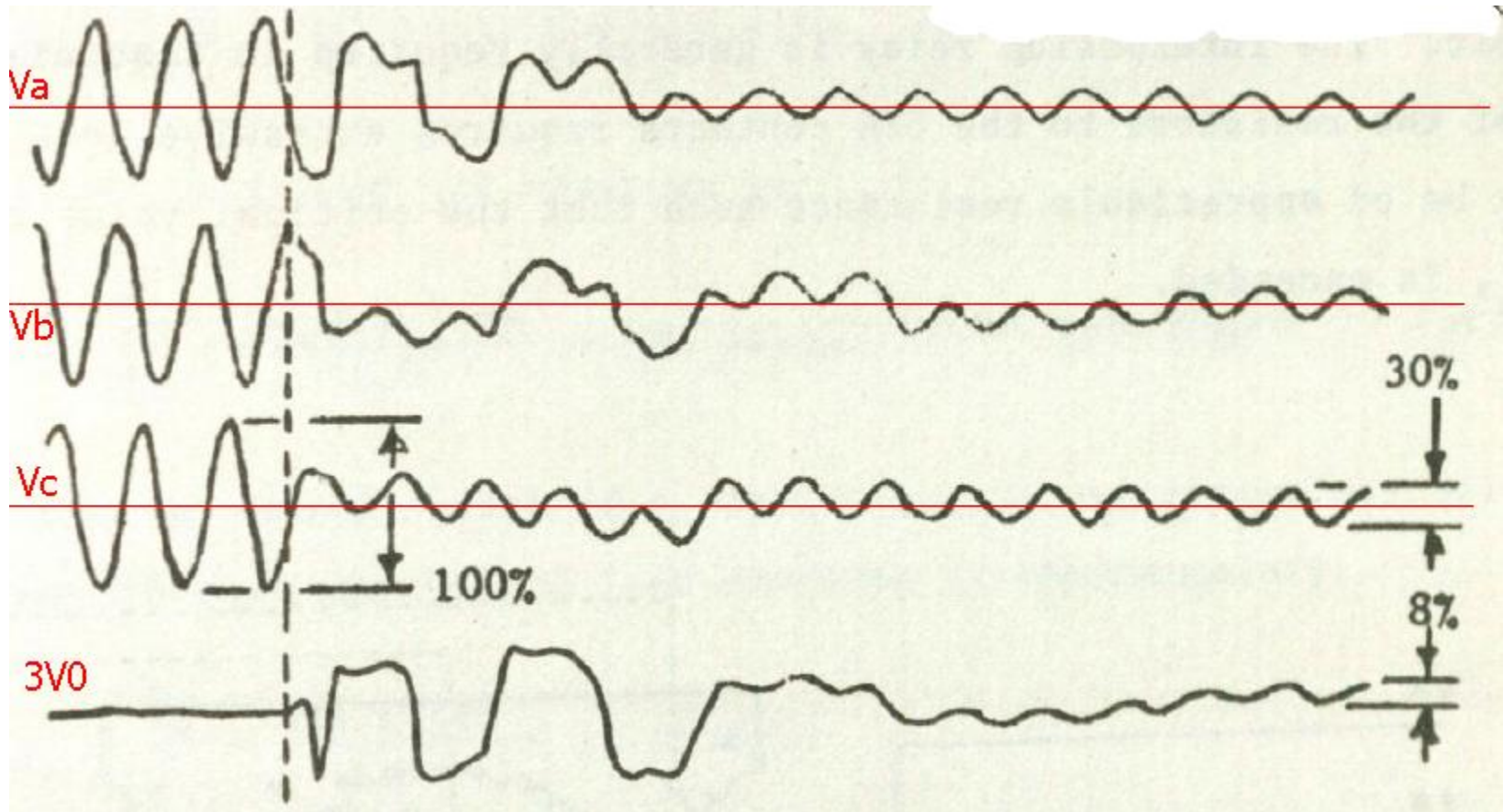


(b) Equivalent of figure (a)



(c) Transient response and ferroresonant operating state

# 345 kV Bus Clearing



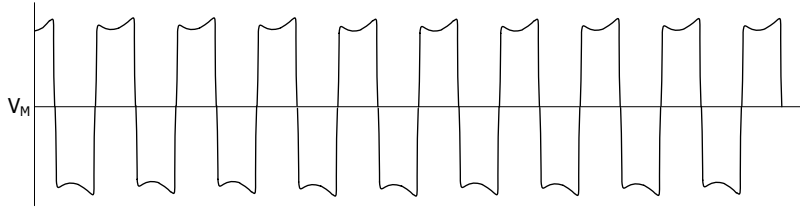
Energized through open breaker capacitance, circa 1976



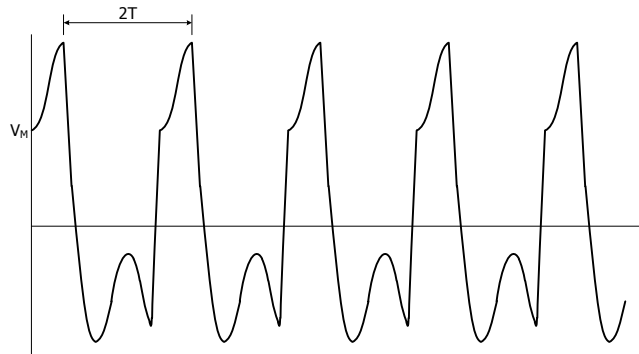
# Ferroresonant Modes

- Transformer operation in the ferroresonant state is dependent on a number of factors
  - system voltage magnitude
  - the initial voltage on the capacitor
  - the initial state of the magnetic characteristics of the transformer
  - the total loss in the ferroresonant circuit
  - the point on wave of initial switching
- It is normally initiated after some type of switching event such as transformer energization, single-phase switching, fault clearing, breakers opening, or loss of system grounding
- Given the right conditions it can lock into any of the following ferroresonant modes
- The one common characteristic among these ferroresonant modes is that they all contain the fundamental frequency driving voltage component, which sustains it.

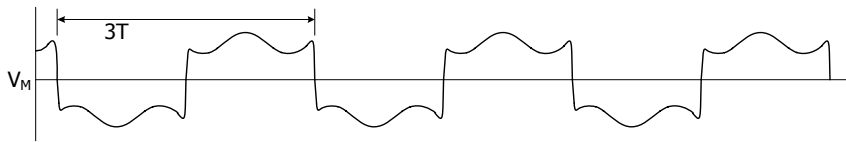
# Ferroresonant Modes



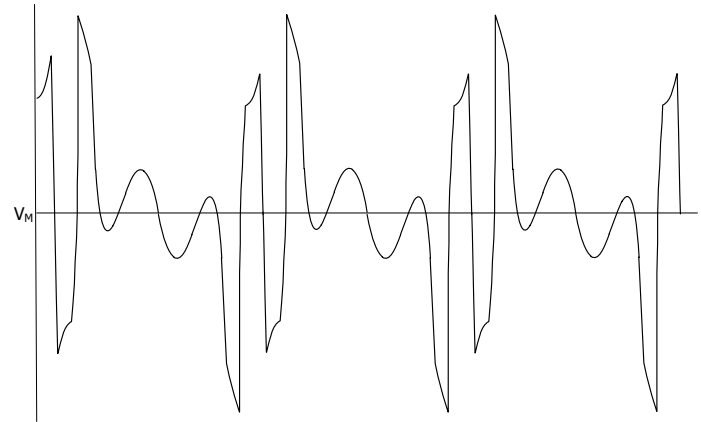
Fundamental – 60 Hz



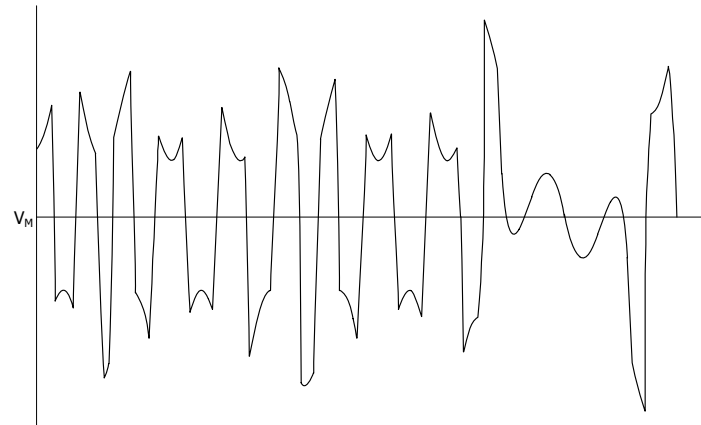
Subharmonic – 30 Hz



Subharmonic – 20 Hz

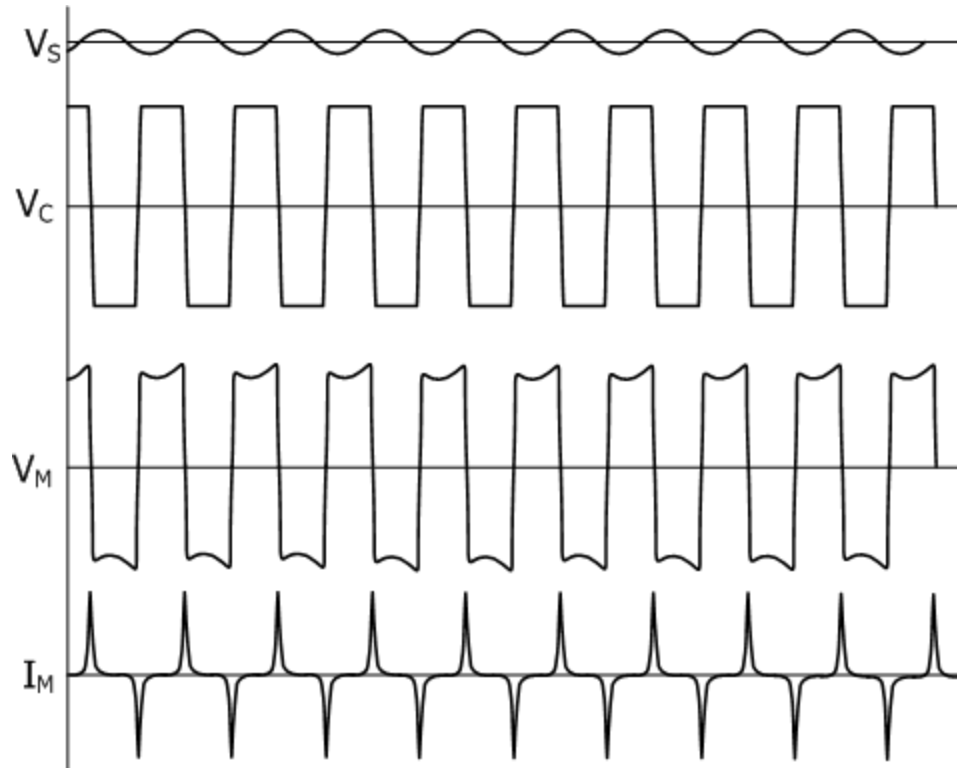


Quasi-periodic



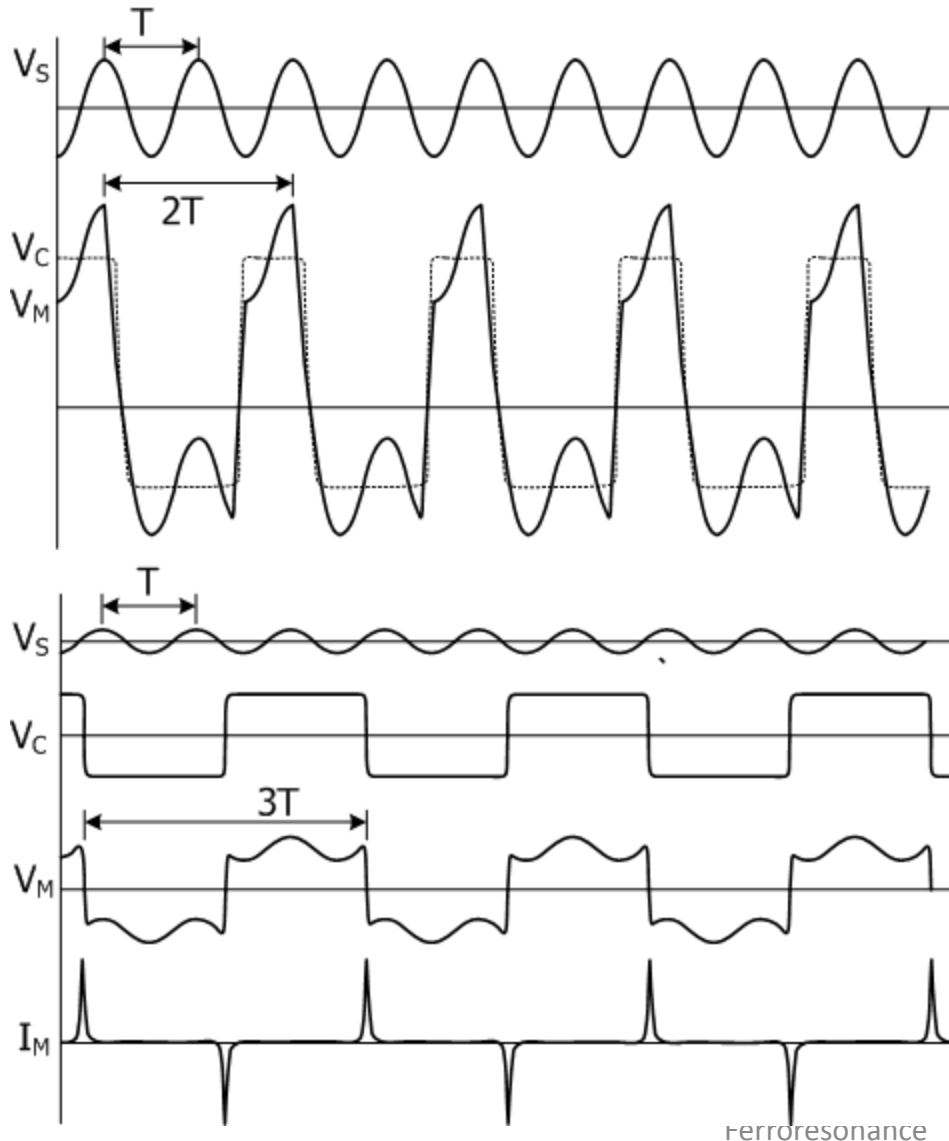
Chaotic  
(hunts for, but cannot lock into pattern)

# Fundamental Mode Ferroresonance



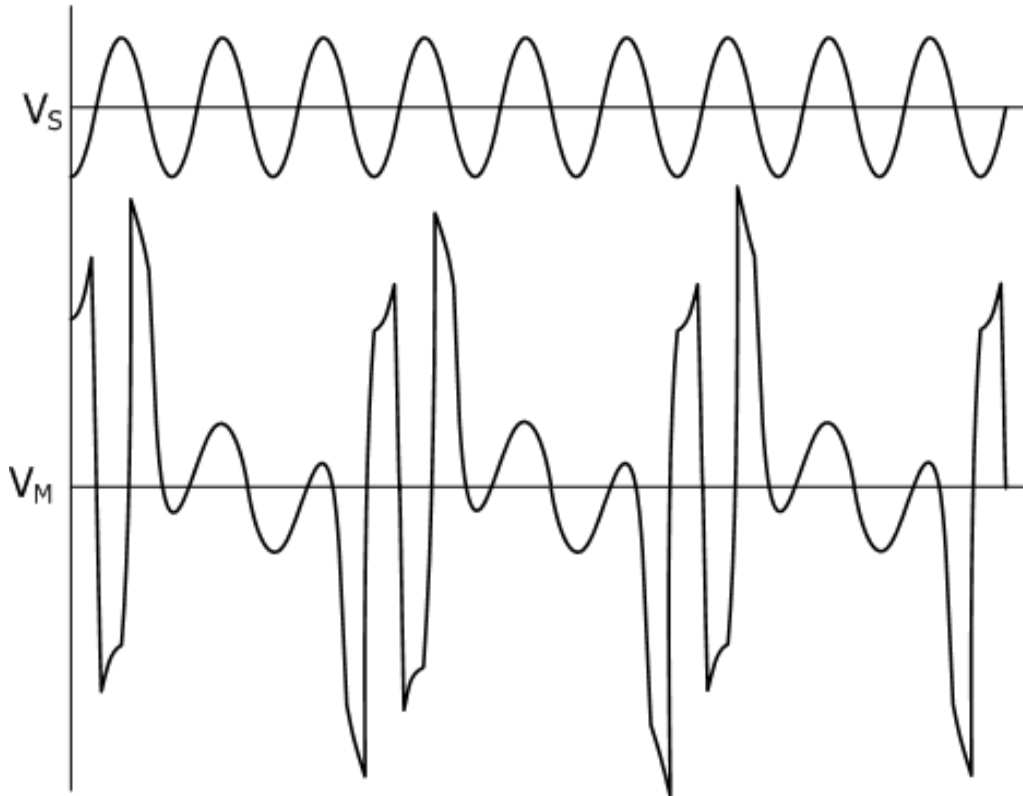
- $V_M$  oscillations at  $V_S$  (system) frequency
- Higher than nominal voltage of transformer
- $V_C$  and  $V_S$  components
- Phase reversal – opposite polarity to  $V_S$
- Positive and negative half cycles are generally symmetrical – exceptions
- High current spikes

# Sub-harmonic Mode Ferroresonance



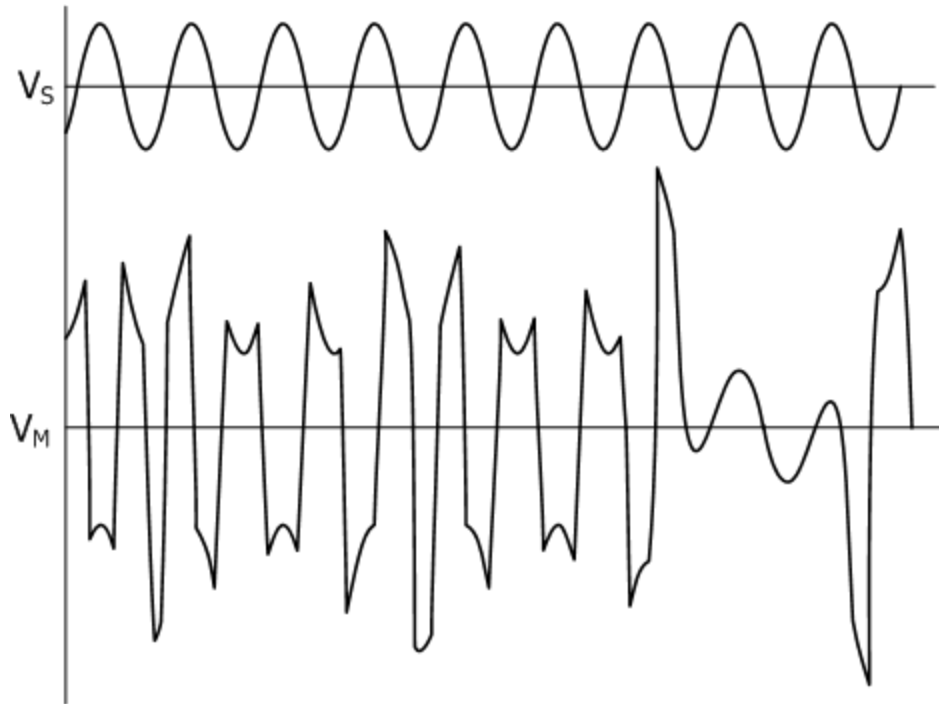
- $V_M$  oscillation periods in integer multiples of fundamental period,  $T_S = nT$ ,  $n = 2, 3, \dots$
- 30 Hz ( $T=2$ ) - Positive and negative half cycles are not always symmetrical, but patterns are repeated
- 20 Hz ( $T=3$ ) - Oscillations generally symmetrical and magnitude is lower than nominal voltage of transformer
- $V_C$  and  $V_S$  components
- High current spikes

# Quasi-periodic Mode Ferroresonance



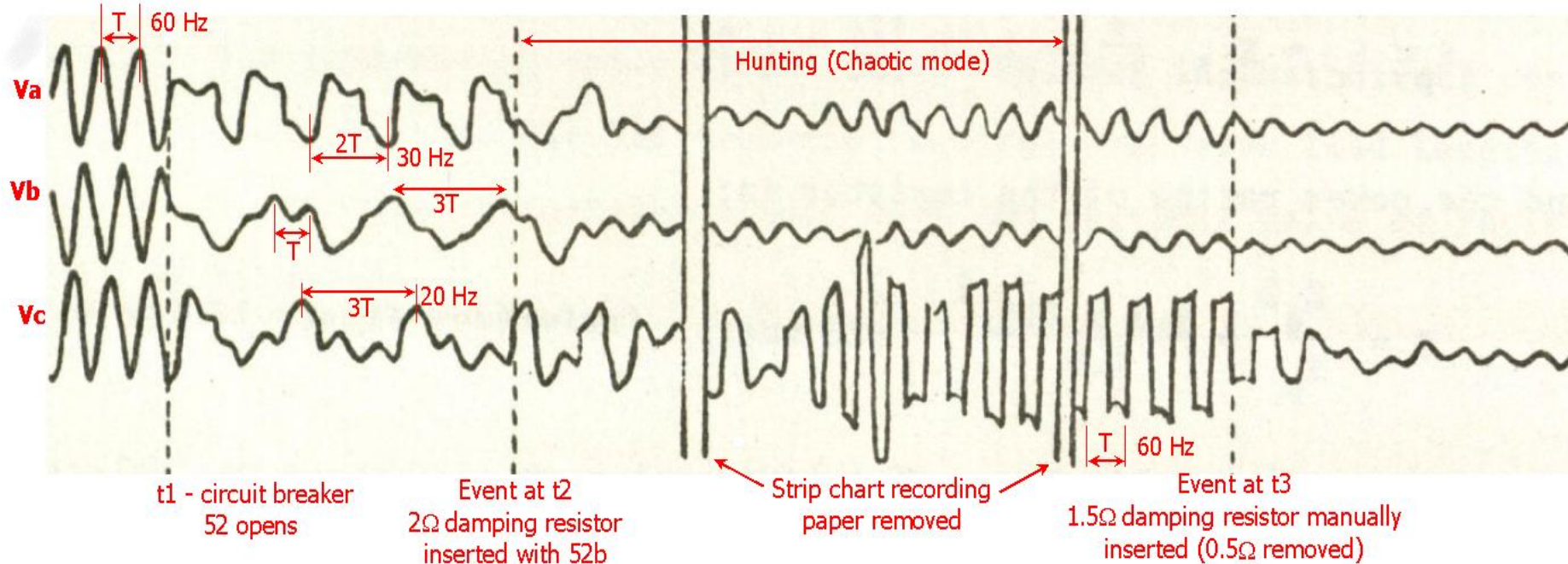
- $V_M$  oscillations are irregular, but appear periodic
  - Patterns are very nearly repeated,  $T^+$ ,  $T^-$ ,  $T^+$ , etc., and with different magnitudes
- Peak voltage much greater than transformer nominal
- Greater degree of saturation
- More coupling with other phases
- $V_C$  and  $V_S$  components
- High current spikes

# Chaotic (Hunting) Mode Ferroresonance



- $V_M$  oscillations are irregular with no repetition of patterns
- The system is hunting for a stable ferroresonant mode with a chaotic variation in voltage magnitudes and frequency
- Peak voltage much greater than transformer nominal
- Greater degree of saturation
- More coupling with other phases
- $V_C$  and  $V_S$  components
- High current spikes

# 345 kV Substation Vt Ferroresonance

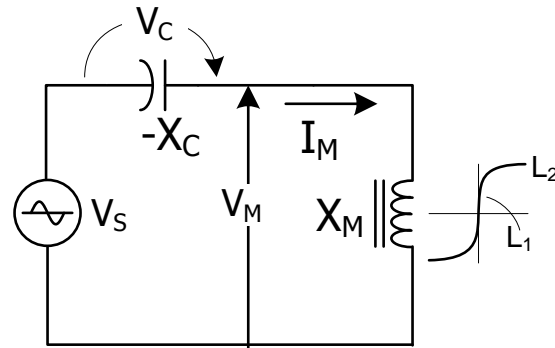


- Copy of strip chart record - Circa 1976

# Transformer Operating States

Without series resistance

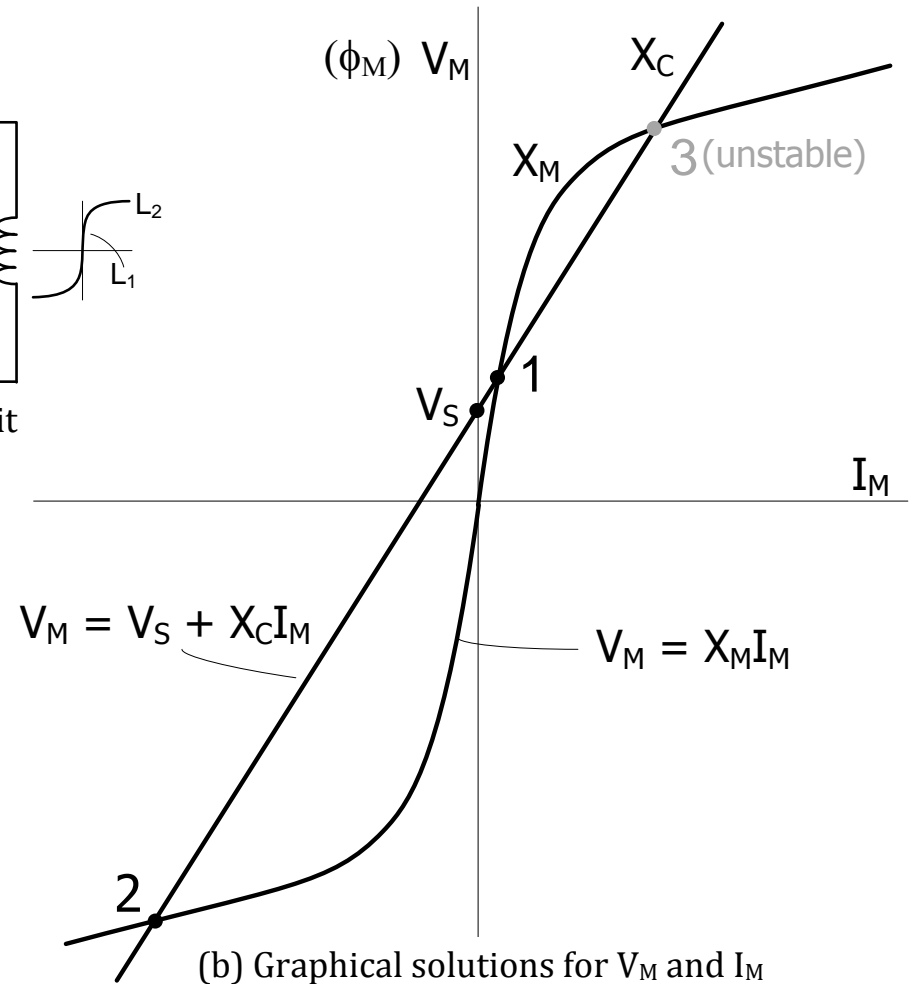
Without series resistance



(a) Equivalent circuit

## Two operating states

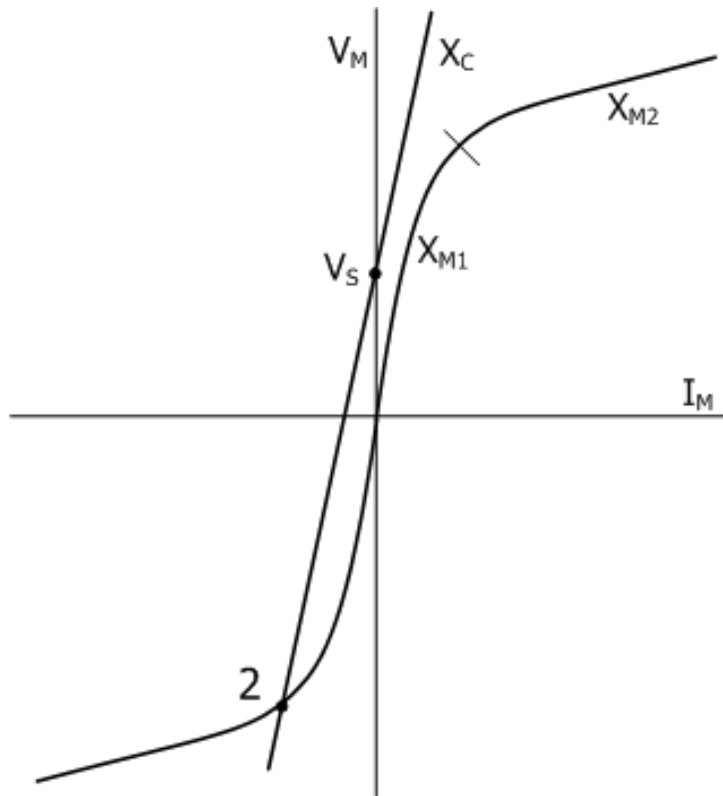
- Point 1 – normal
- Point 2 – ferroresonant with phase reversal from point 1
- Point 3 cannot occur



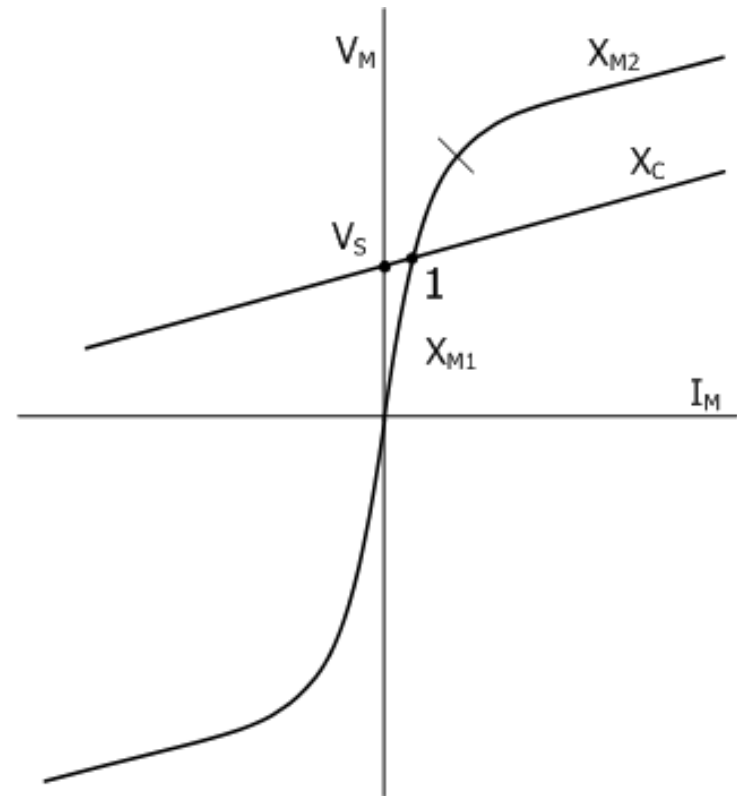


# Transformer Operating States

Without series resistance



(a) Ferroresonant (over excited) state -  $|X_C| \geq X_{M1}$

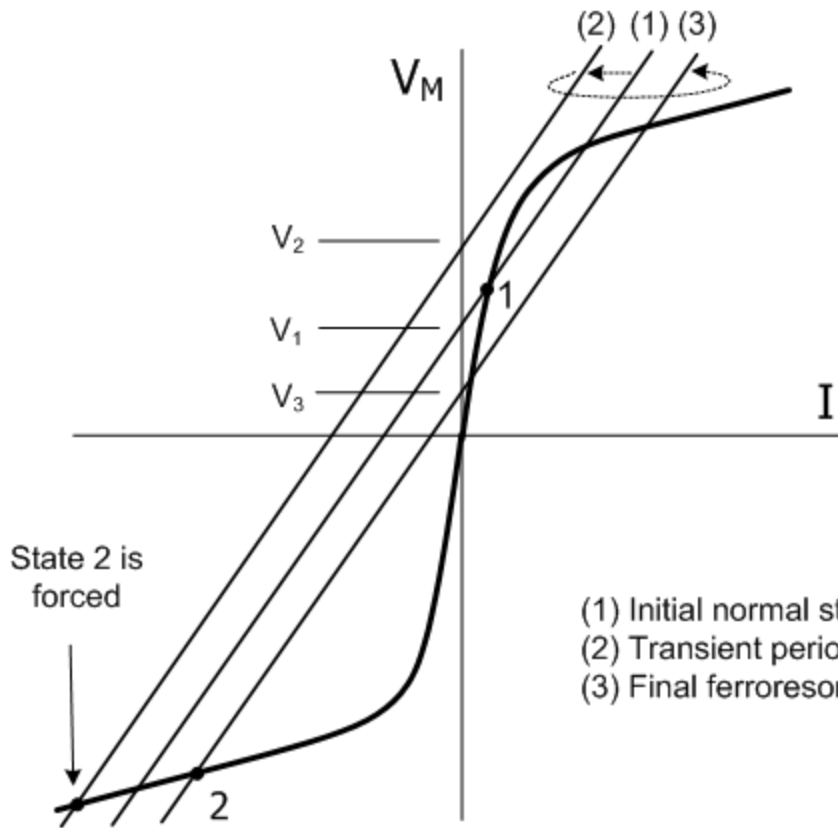


(b) Normal state -  $|X_C| \leq X_{M2}$

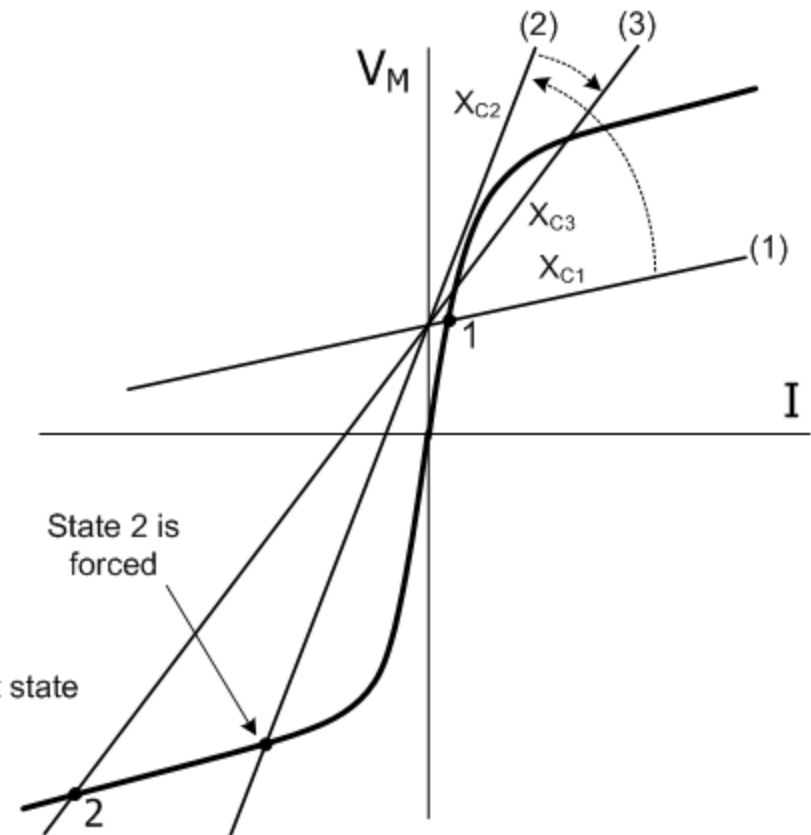
Single point solutions

# Transformer Operating States

Without series resistance



(a) Voltage transient – constant impedance

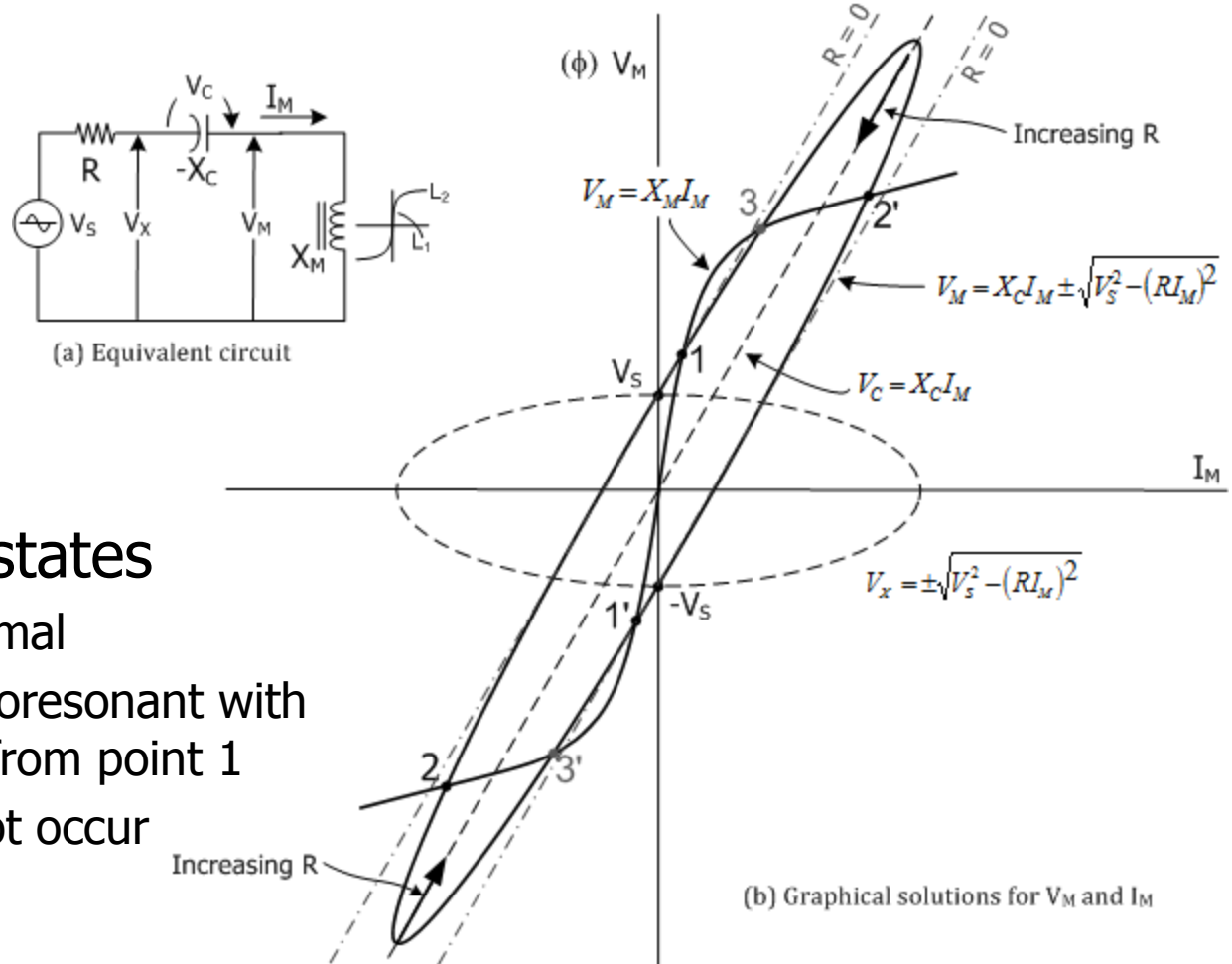


(b) Impedance transient – constant voltage

## Transient change of operating state

# Transformer Operating States

With series resistance

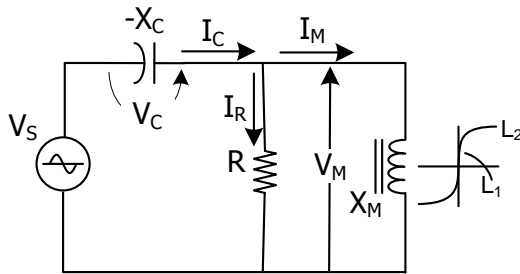


## Two operating states

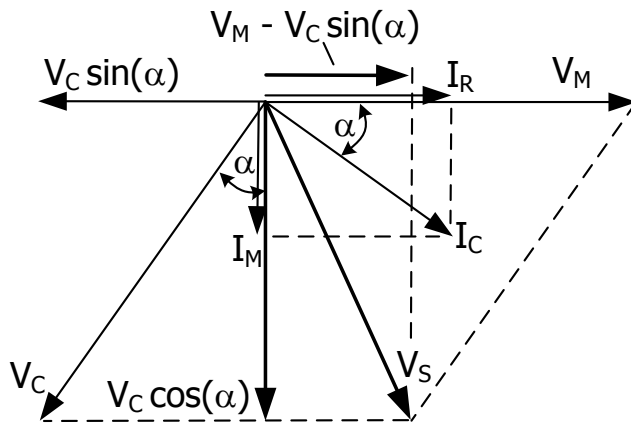
- Point 1/1' – normal
- Point 2/2' – ferroresonant with phase reversal from point 1
- Point 3/3' cannot occur

# Transformer Operating States

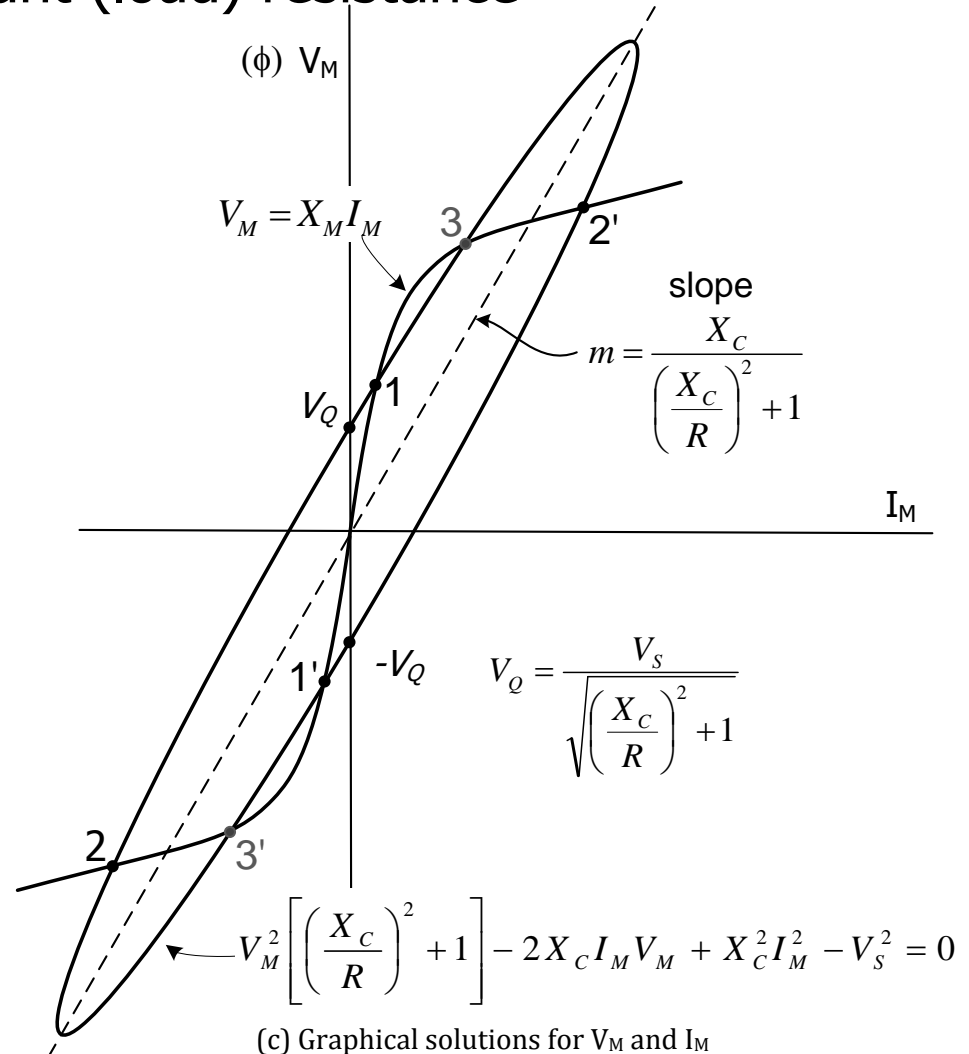
With shunt (load) resistance



(a) Equivalent circuit



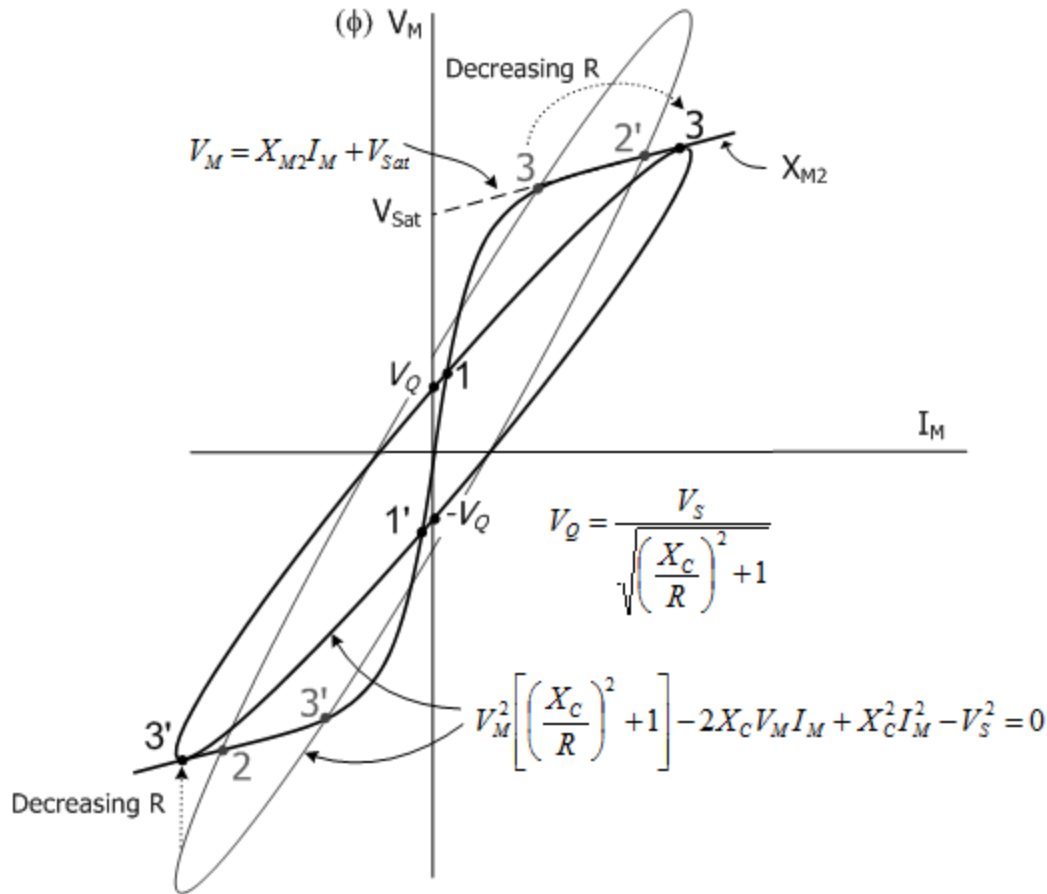
(b) Phasor diagram



(c) Graphical solutions for  $V_M$  and  $I_M$

# Transformer Operating States

With shunt (load) resistance

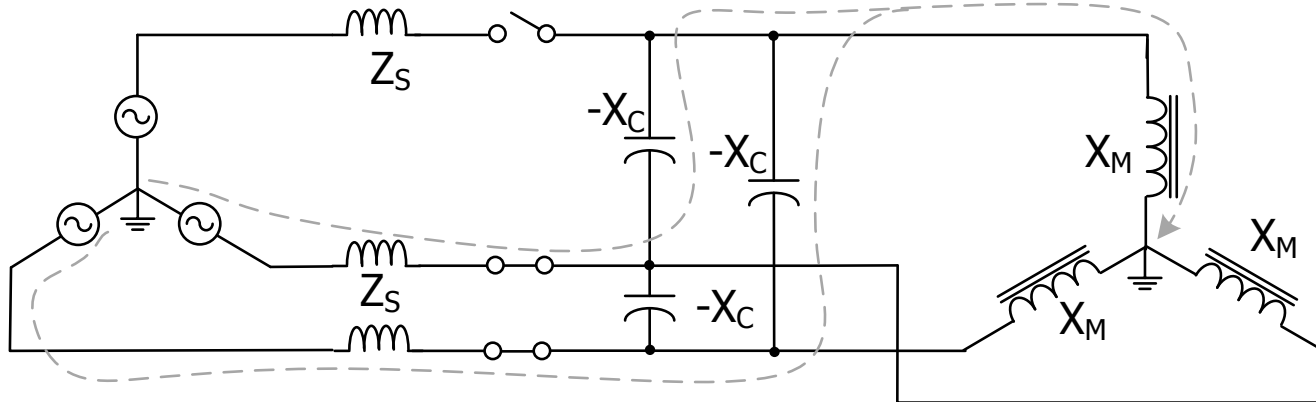


$$R_{Max} = \frac{X_C X_{M2}}{X_C - X_{M2}} \sqrt{\left(\frac{X_C V_{Sat}}{X_{M2} V_S}\right)^2 - 1}$$

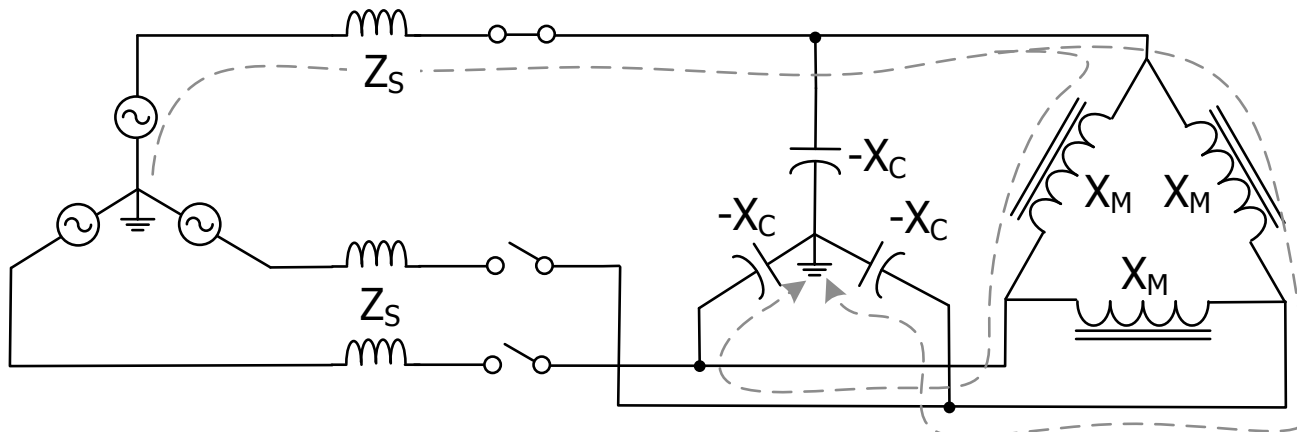
$$X_C \gg X_{M2}$$

$$R_{Max} = \frac{X_C V_{Sat}}{V_S}$$

# Ferroresonant Configurations

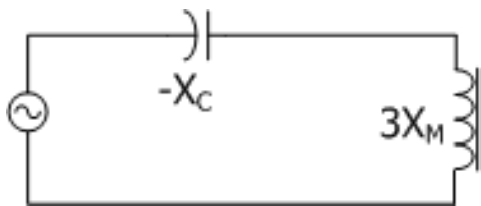
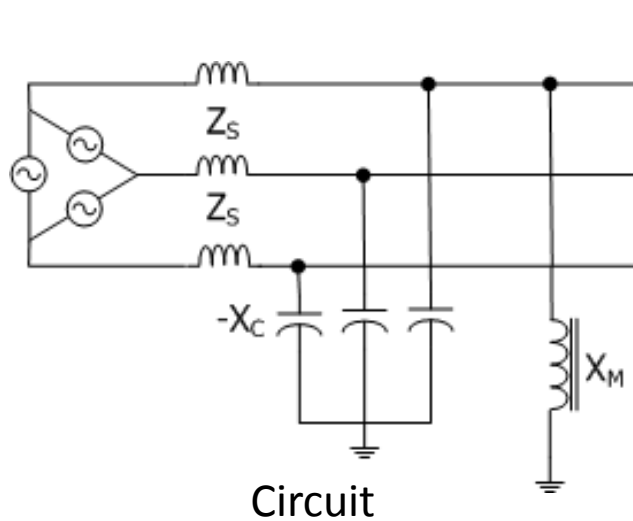


(a) Coupling through phase-to-phase capacitance with grounded transformer

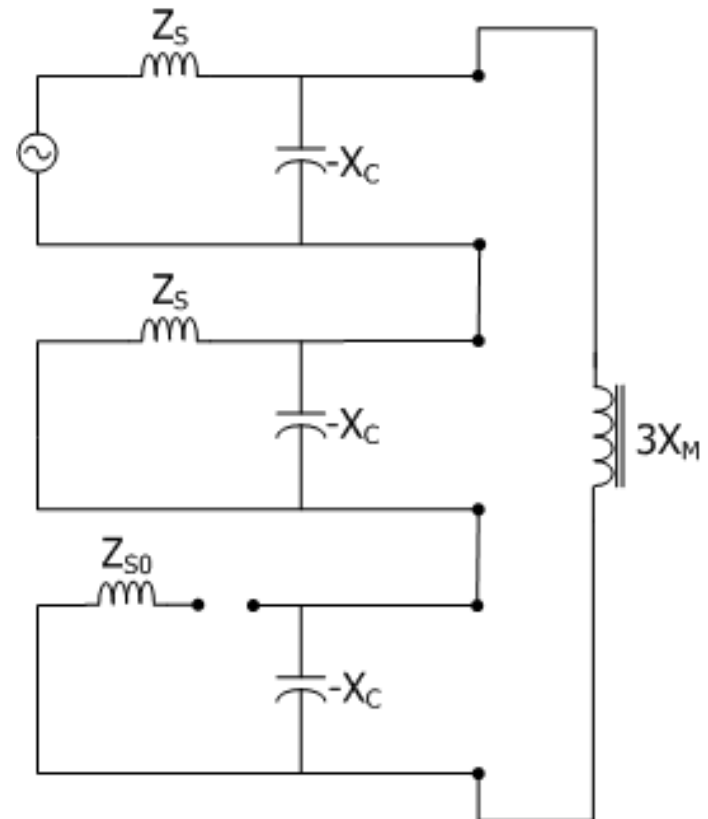


(b) Coupling through phase-to-ground capacitance with ungrounded transformer

# Ferroresonant Configurations



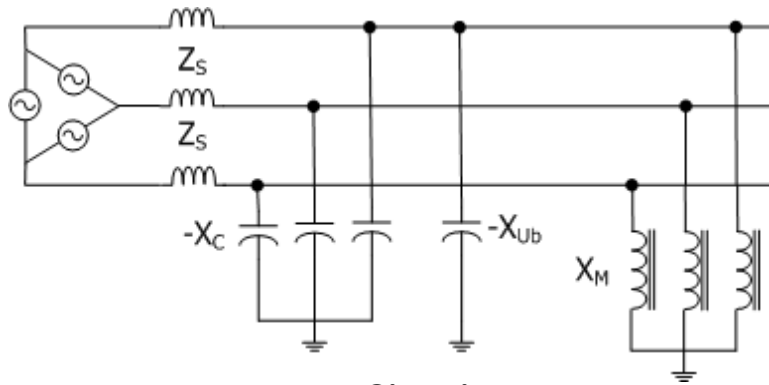
Equivalent circuit,  $Z_S = 0$



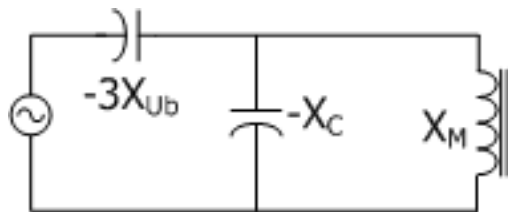
Sequence networks and connection

Grounded single phase transformer on ungrounded system

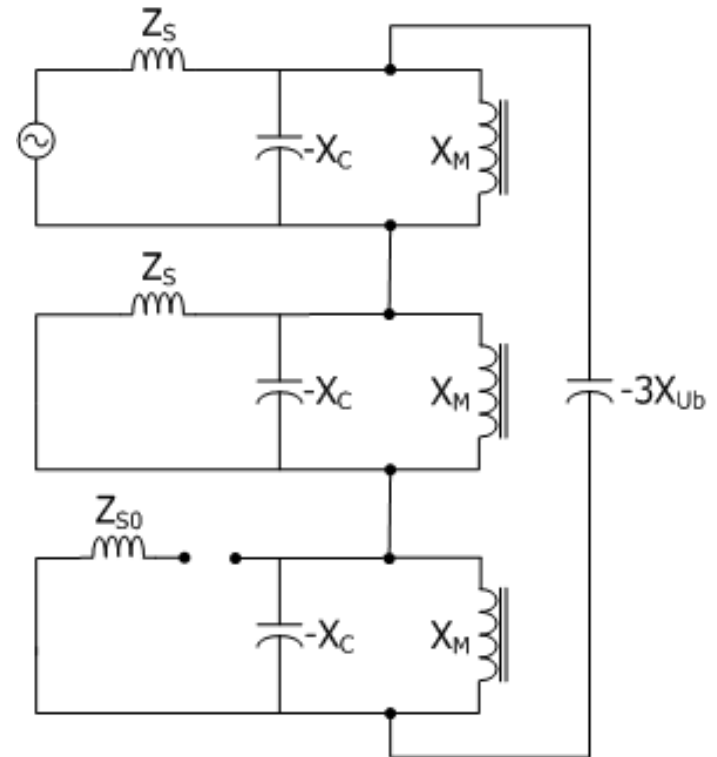
# Ferroresonant Configurations



Circuit



Equivalent circuit,  $Z_S = 0$

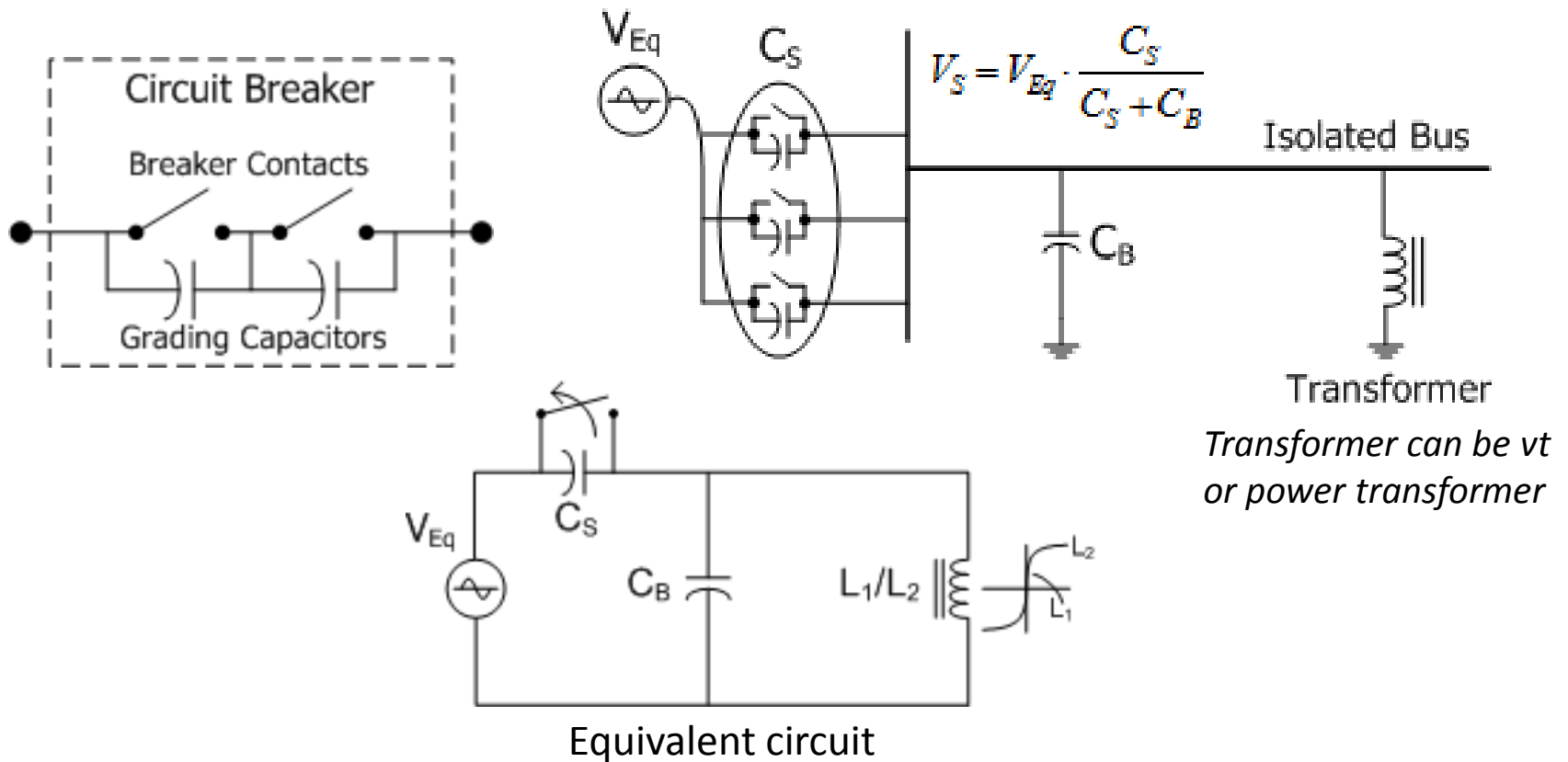


Sequence networks and connection

Grounded three phase transformer on ungrounded system with unbalanced phase-to-ground capacitance

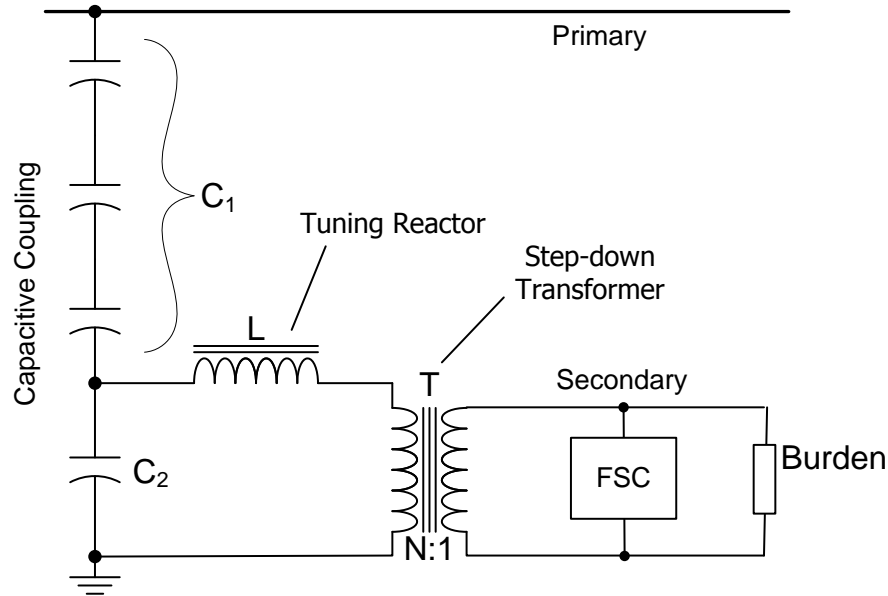


# Ferroresonant Configurations

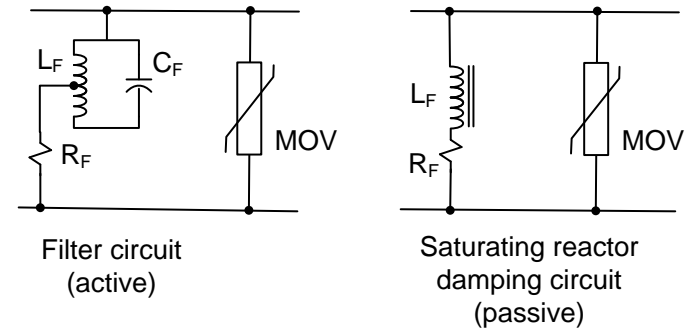


Open breaker capacitance and transformers

# Ferroresonant Configurations



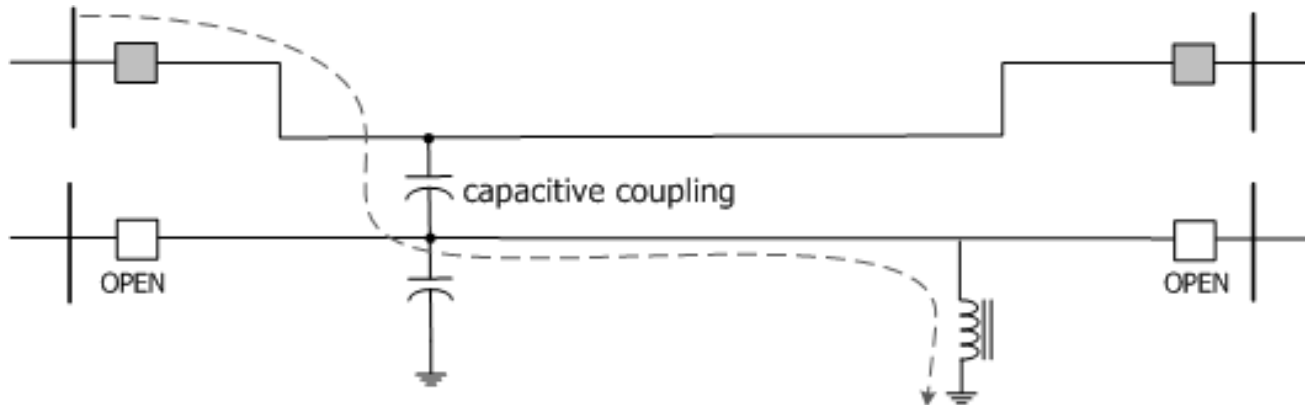
(a) CVT equivalent circuit



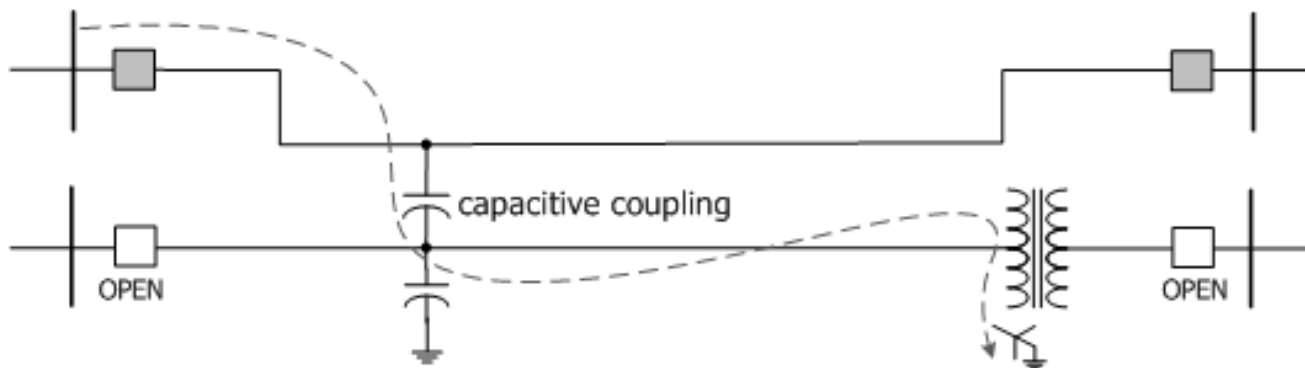
(b) Typical Ferroresonance suppression circuits with surge arrestor

Ccvt

# Ferroresonant Configurations



(a)  $V_t$  or tapped transformer



(b) Transformer terminated line

Transformer connected to isolated line

# Mitigation

- Mitigation of ferroresonance involves one or more of following:
  - Correcting voltage unbalance
  - Changing the transformer magnetic design
  - Inserting damping resistance
  - Detuning the circuit

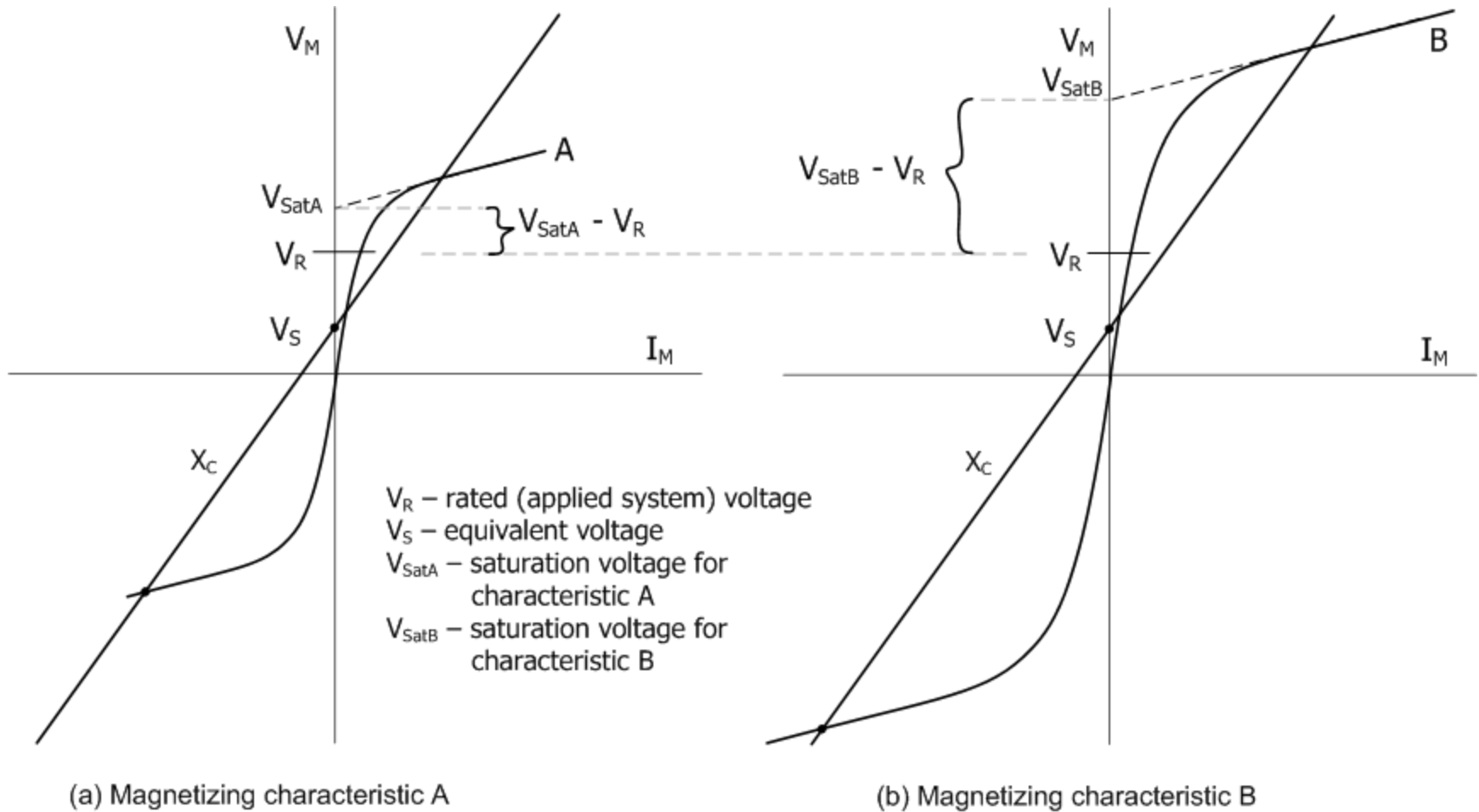
# Mitigation

## Correcting voltage unbalance

- Change operating procedures
  - E.g. - single phase switching of three phase distribution transformers may be changed to three phase operation
- Applying protective relays to sense and remove the unbalanced condition that drives ferroresonance
  - E.g. - a voltage relay that is used to sense excessive zero sequence voltage and trip a circuit breaker
- Opportunities to correct voltage unbalance should be investigated.
- There are many applications where steady state unbalanced voltages cannot be avoided and alternative solutions are required

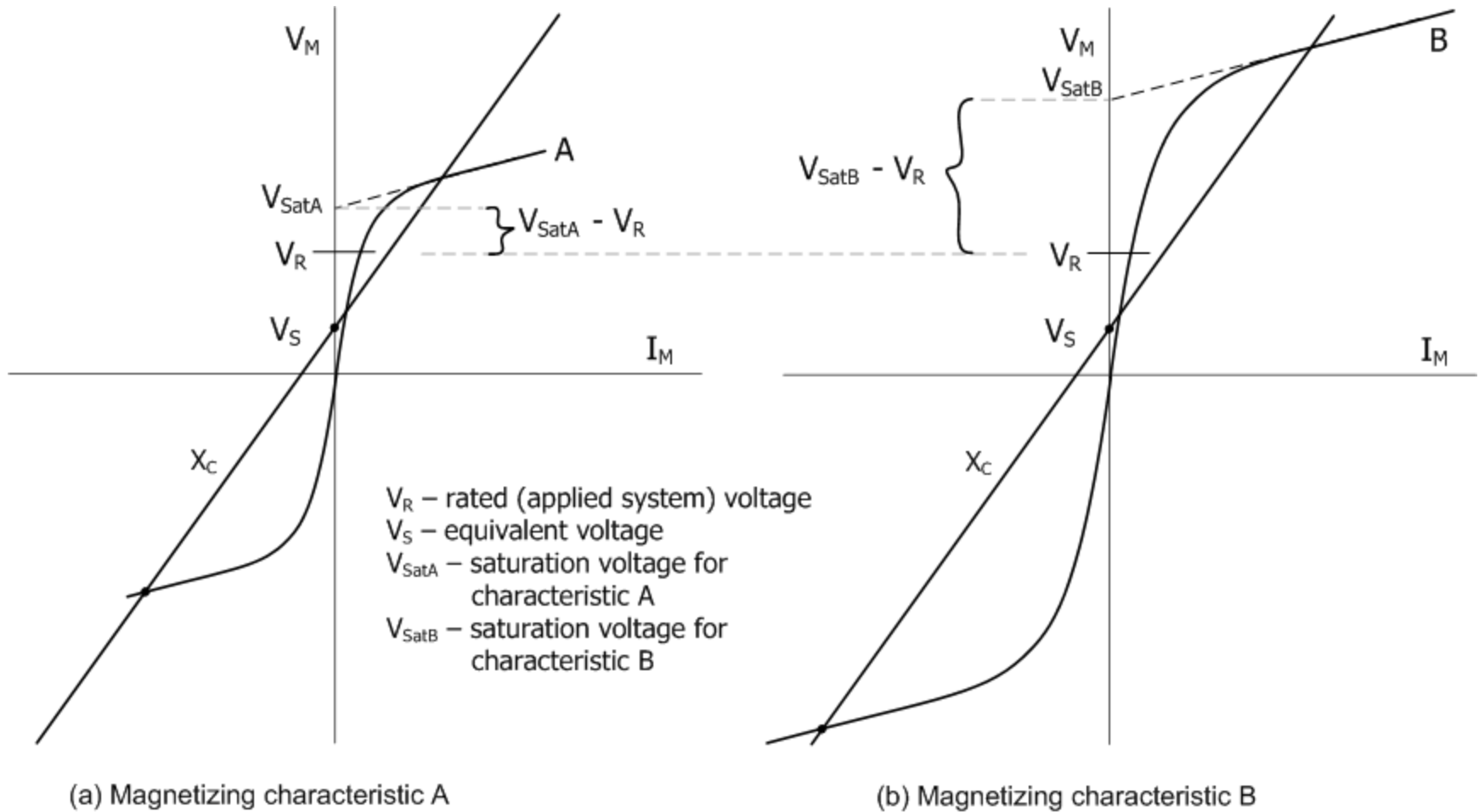
# Mitigation

## Changing the transformer magnetic design



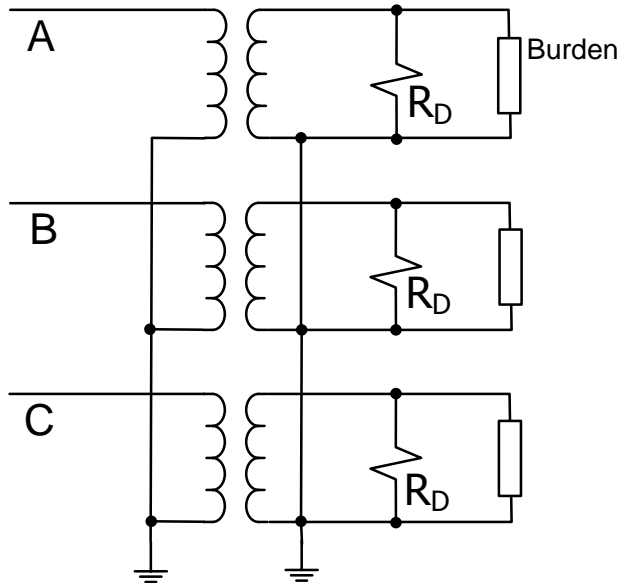
# Mitigation

## Changing the transformer magnetic design

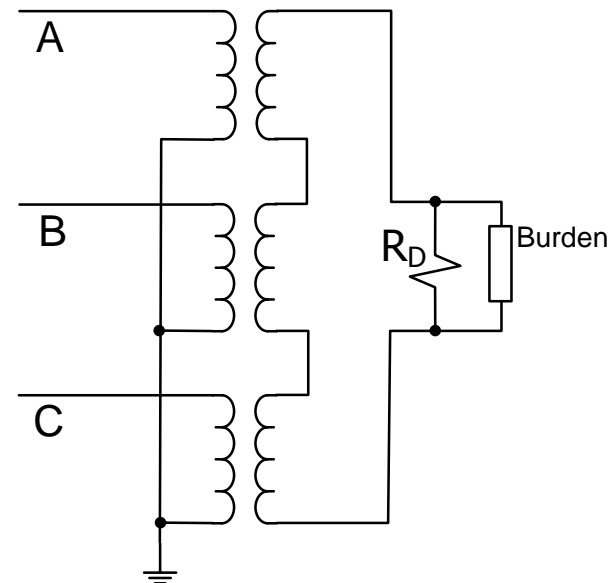


# Mitigation

## Inserting damping resistance



(a) per phase damping with a wye grounded secondary



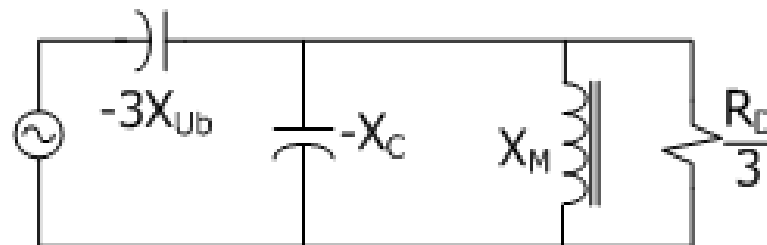
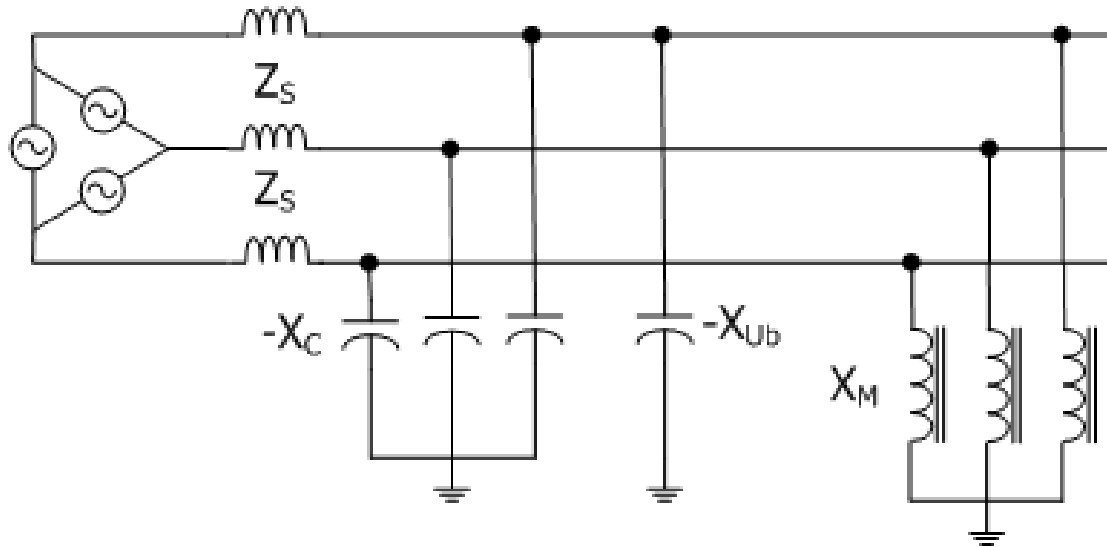
(b) zero sequence damping with a broken delta secondary

- Generally requires some form of “switching”  $R_D$  to address thermal requirements
- May require “switching” to address thermal requirements
- Affect of permanent connection on measurement accuracy of burden devices
- Correction of unbalance



# Mitigation

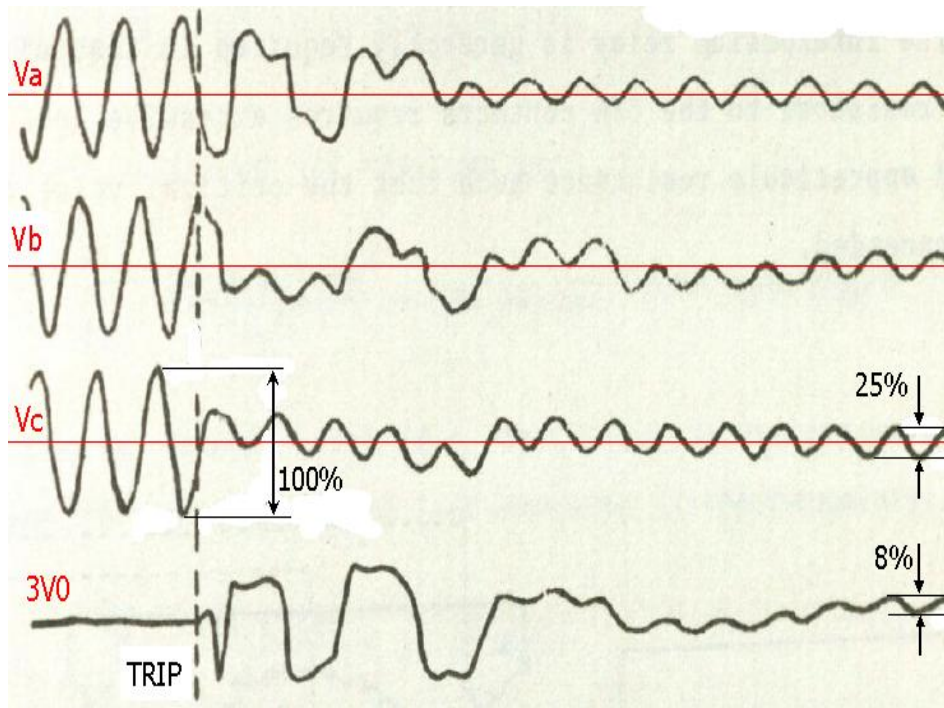
With zero sequence damping resistance



Equivalent Circuit with broken delta resistor  $R_D$

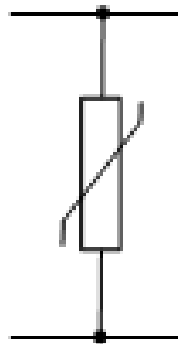
# Mitigation

With zero sequence damping resistance

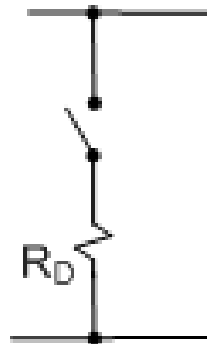


- Ferroresonance has often been mitigated with zero sequence damping
- Coupled phase voltage  $V_A$ ,  $V_B$ ,  $V_C$  is an indication of phase-to-ground capacitance
- $3V_0$  is an indication of the bus capacitance unbalance
- If  $3V_0$  is relatively small zero sequence damping will probably not be sufficient and phase damping required
- About the only generalization that can be made is that the greater the unbalance (the higher  $3V_0$ ) the more likely zero sequence damping will be successful

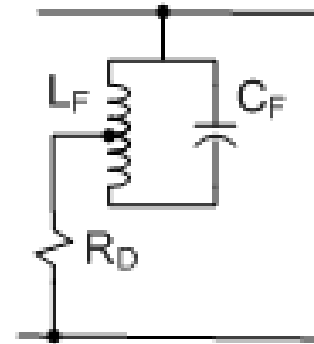
# Ferroresonance Suppression Circuits



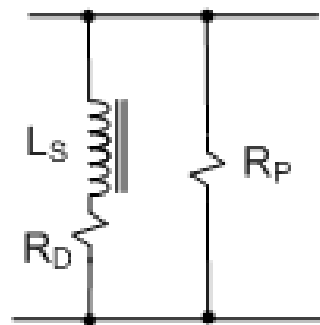
MOV



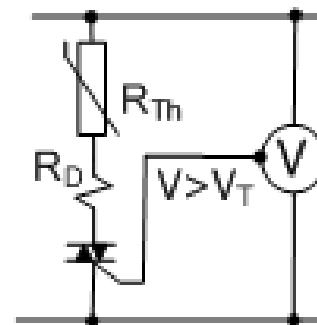
Switched  
resistor



Filter circuit

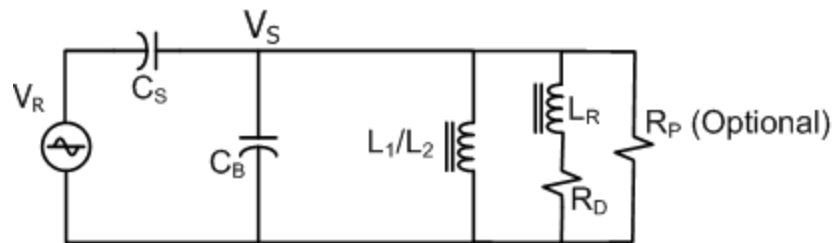


Saturating reactor  
damping circuit

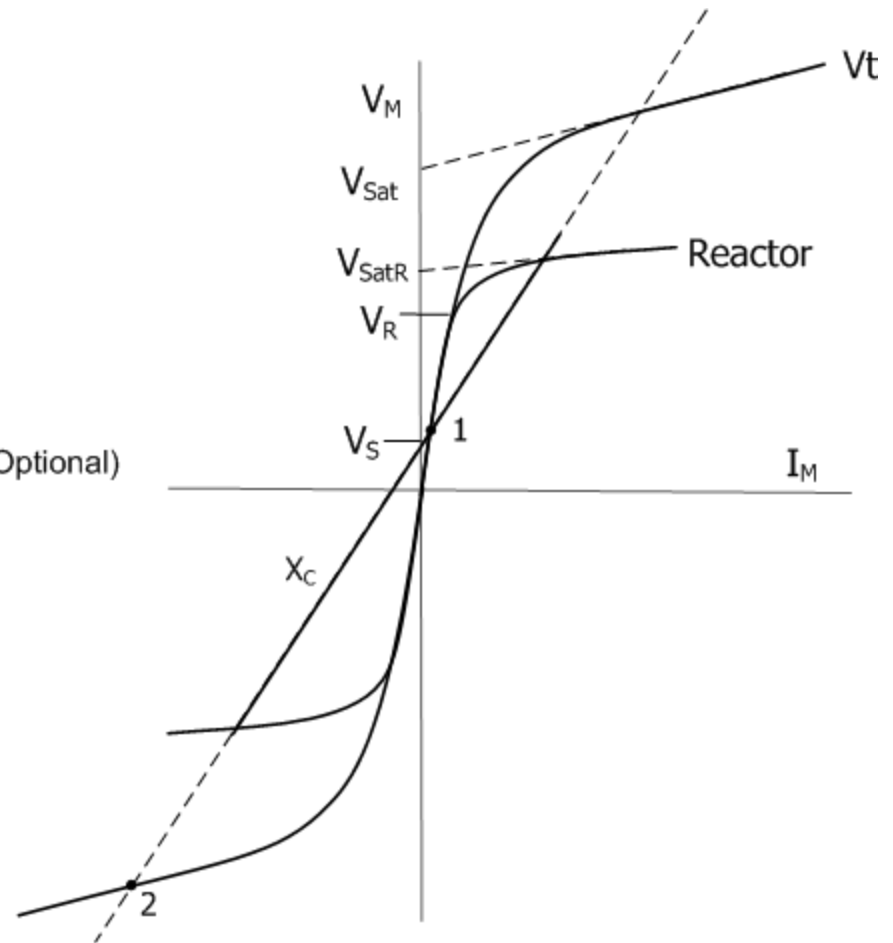


PTC thermistor  
with triac switch

# Saturating Reactor Damping Circuit

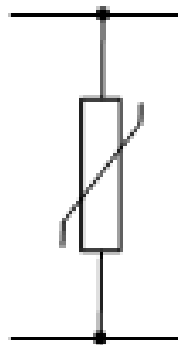


(a) Ferroresonant circuit

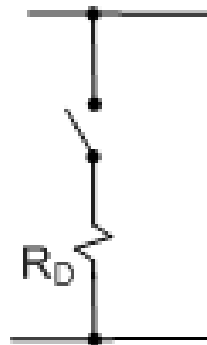


(b) Saturating reactor

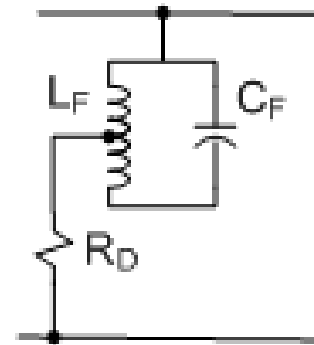
# Ferroresonance Suppression Circuits



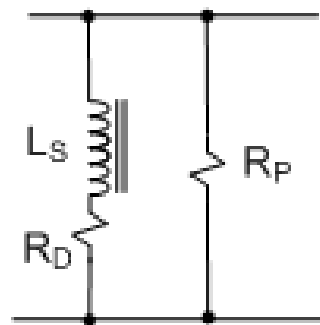
MOV



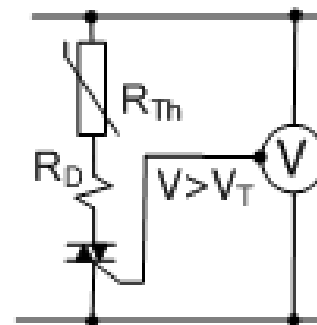
Switched  
resistor



Filter circuit



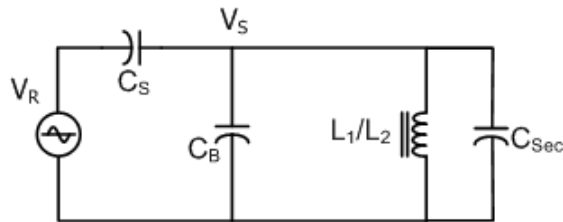
Saturating reactor  
damping circuit



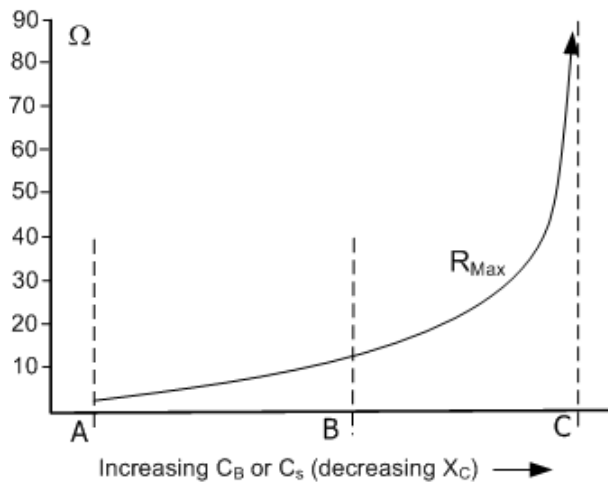
PTC thermistor  
with triac switch

# Mitigation

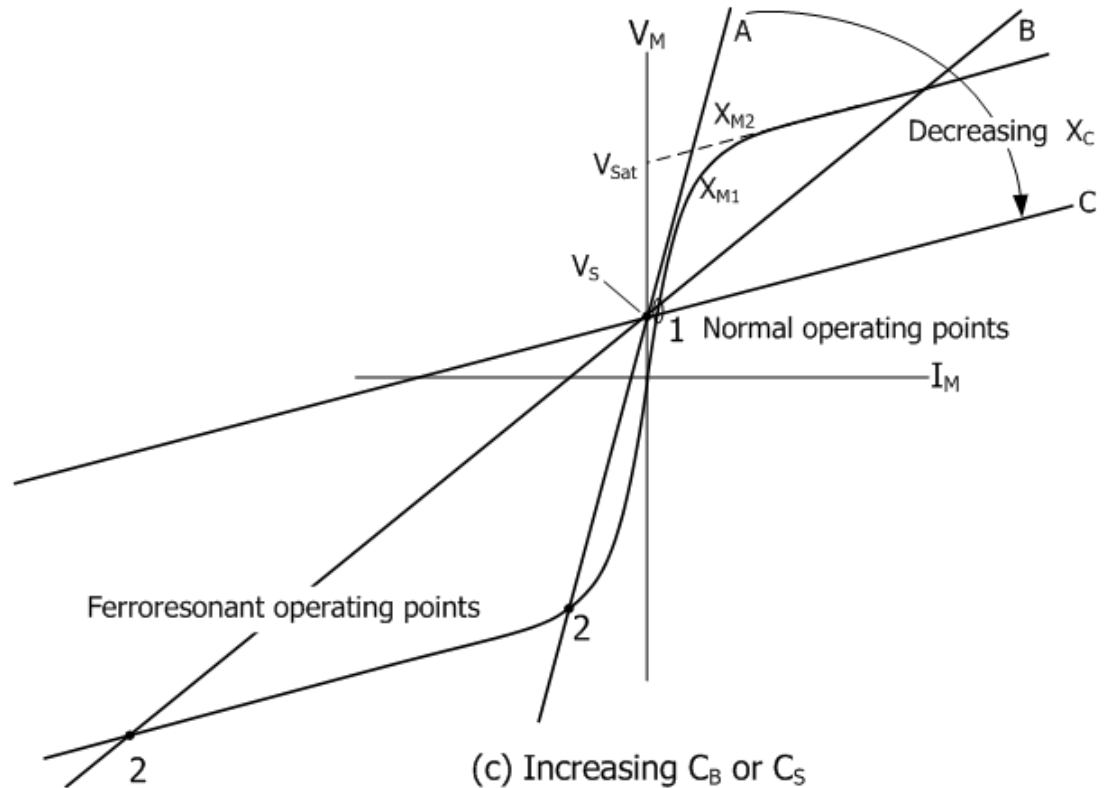
## Detuning the ferroresonant circuit



(a) Ferroresonant circuit



(b) Maximum damping resistance



(c) Increasing  $C_B$  or  $C_S$

# Conclusions

- Ferroresonance is a widely studied phenomenon but it is still not well understood because of its complex behavior - “fuzzy-resonance”
- A simple graphical approach using fundamental frequency phasors has been presented to elevate the readers understanding
- Its occurrence and how it appears is extremely sensitive to the transformer characteristics, system parameters, transient voltages and initial conditions
- More efficient transformer core material has lead to its increased occurrence
- It has considerable effects on system apparatus and protection
- Power system engineers should strive to recognize potential ferroresonant configurations and design solutions to prevent its occurrence