

# Protecting Mutually Coupled Transmission Lines: Challenges and Solutions

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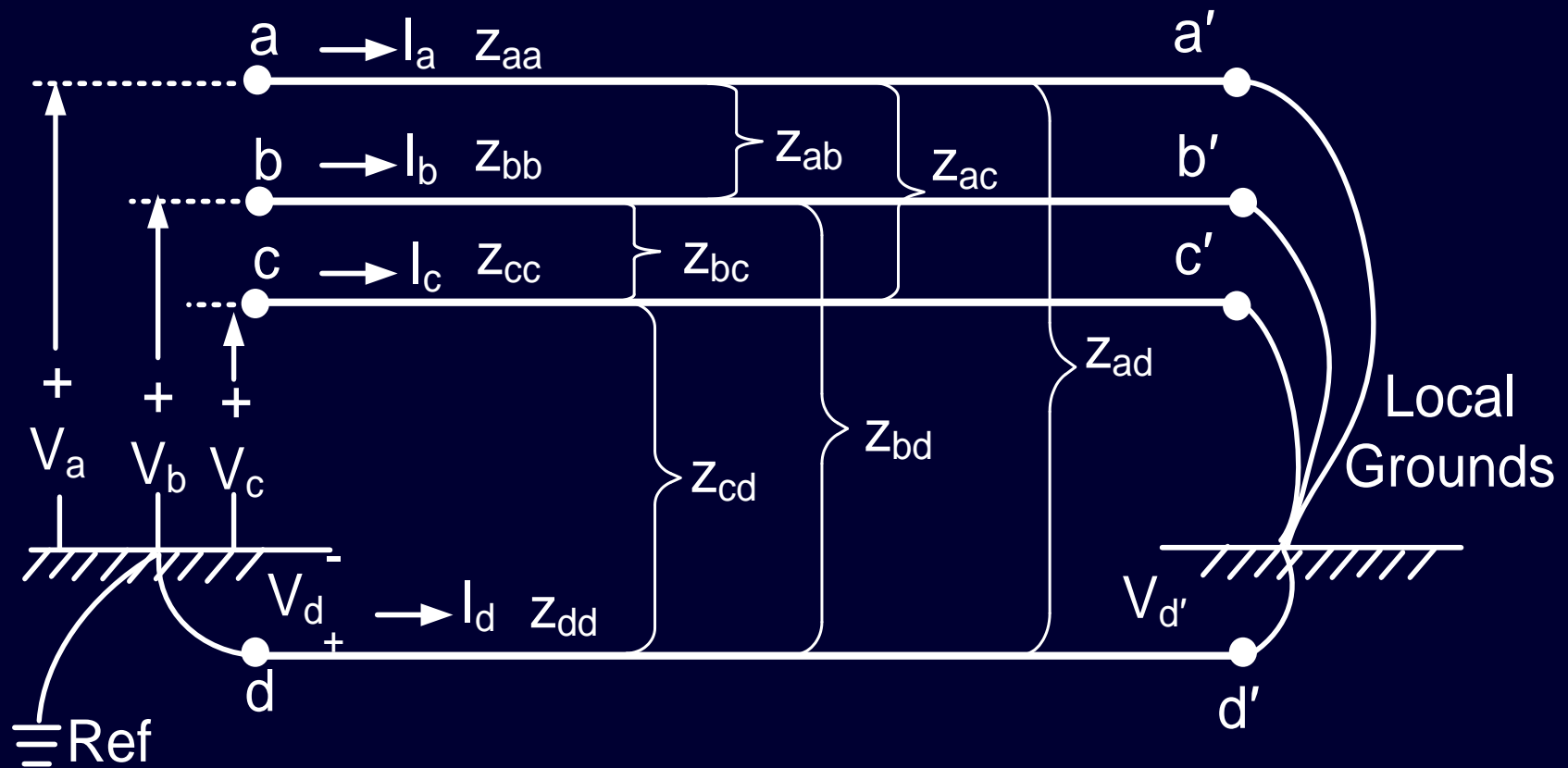
# Introduction

- Transmission line protection principles
- Mutually coupled transmission lines
- Directional element polarization problems
- Distance element reach errors
- Current differential scheme behavior
- Double-circuit lines operated as single circuit

# Transmission Line Protection Principles

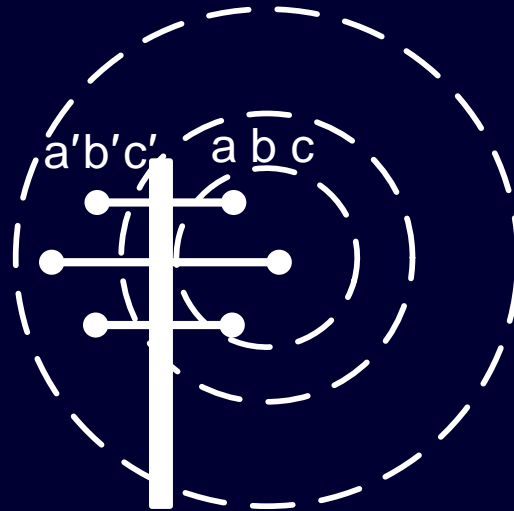
- Directional overcurrent
- Distance
- Directional comparison
- Current differential

# Transmission Line Impedances



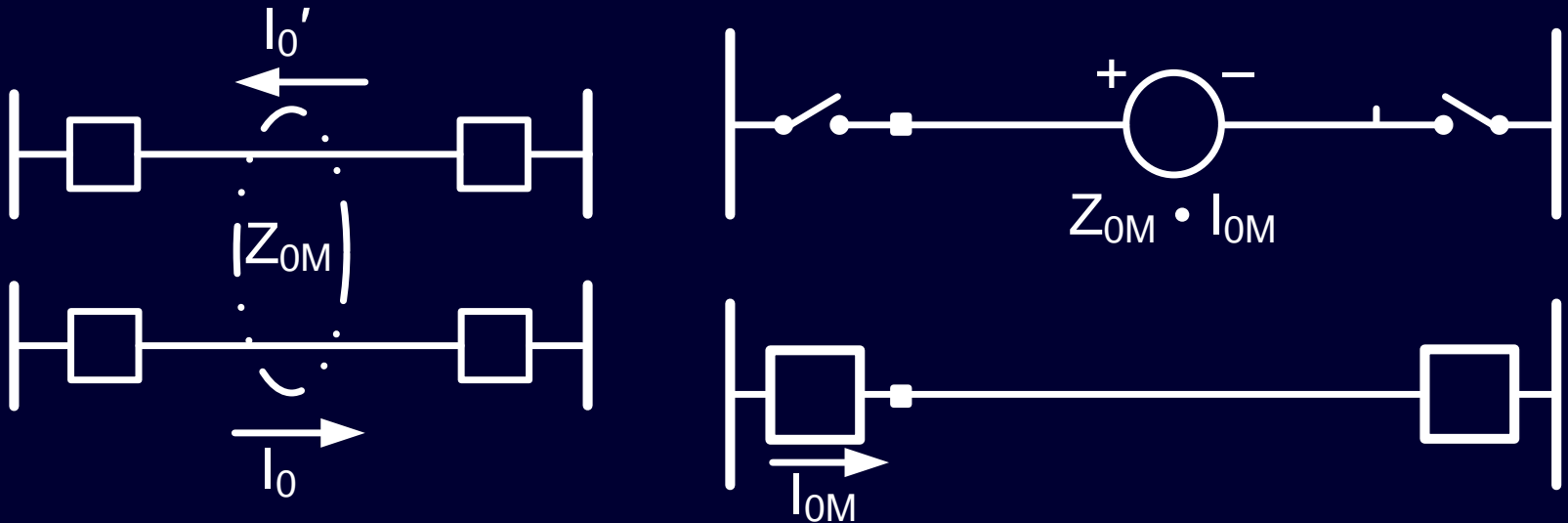
$$\begin{bmatrix} V_a \\ V_b \\ V_c \end{bmatrix} = \begin{bmatrix} Z_{aa} & Z_{ab} & Z_{ac} \\ Z_{ba} & Z_{bb} & Z_{bc} \\ Z_{ca} & Z_{cb} & Z_{cc} \end{bmatrix} \begin{bmatrix} I_a \\ I_b \\ I_c \end{bmatrix}$$

# Two Mutually Coupled Lines



- Positive- and negative-sequence currents add to zero
- Zero-sequence magnetic flux links the coupled line

# Zero-Sequence Mutual Impedance Modeling



Zero-sequence current on one line induces zero-sequence voltage along coupled line

# Mutually Coupled Transmission Lines

$$[Z_{\text{SEQ}}] = \begin{bmatrix} Z_{00} & 0 & 0 & Z_{0M} & 0 & 0 \\ 0 & Z_{11} & 0 & 0 & 0 & 0 \\ 0 & 0 & Z_{22} & 0 & 0 & 0 \\ Z_{0M} & 0 & 0 & Z'_{00} & 0 & 0 \\ 0 & 0 & 0 & 0 & Z'_{11} & 0 \\ 0 & 0 & 0 & 0 & 0 & Z'_{22} \end{bmatrix}$$

Regardless of transpositions,  
 $Z_{0M}$  is always present

# Ground Directional Elements (67N)

Performing phase comparison

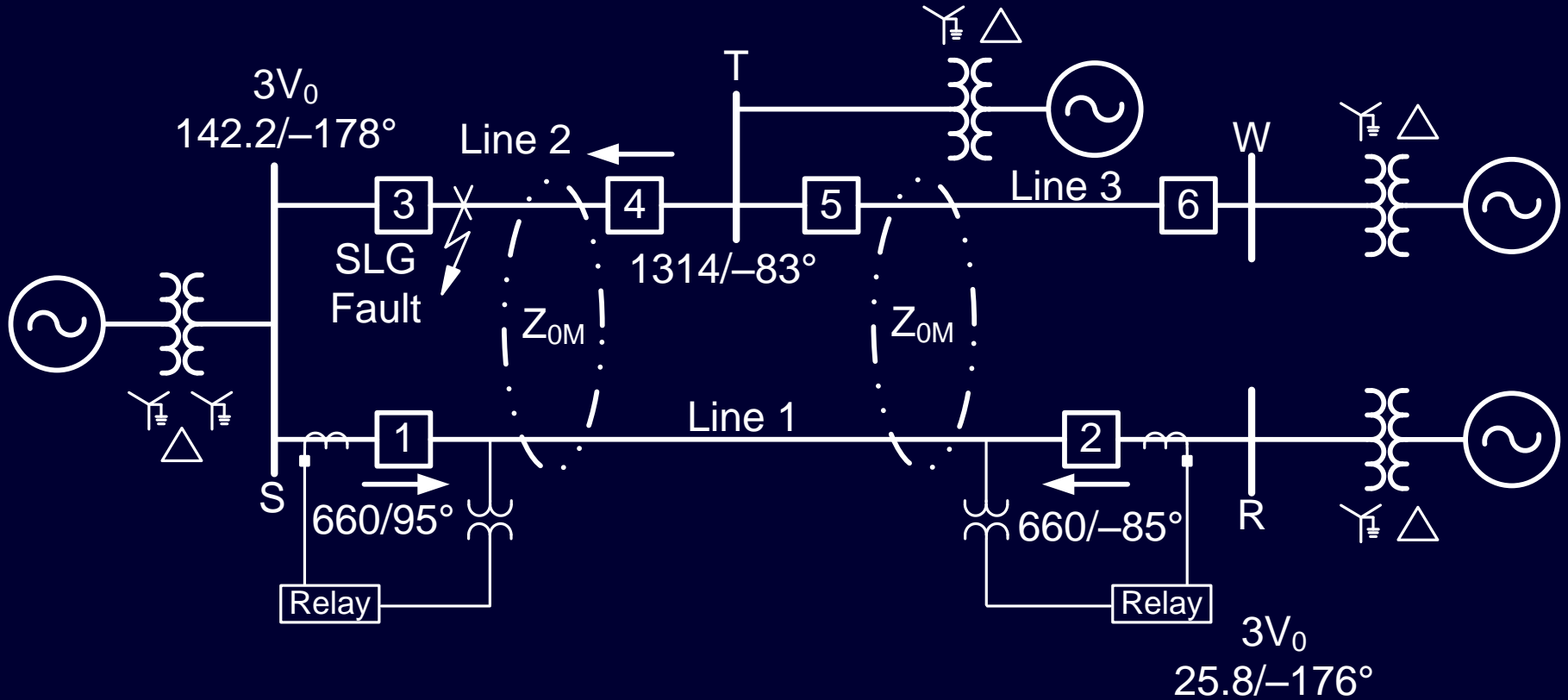
$$T = \text{Re} \left[ (S_{\text{POL}}) (I_{\text{OP}} \cdot 1 \angle \phi_{\text{MS}})^* \right]$$

Measuring sequence impedances

$$Z_2 = \frac{\text{Re} \left[ V_2 (I_2 \cdot 1 \angle \phi_{\text{MS2}})^* \right]}{|I_2|^2}$$

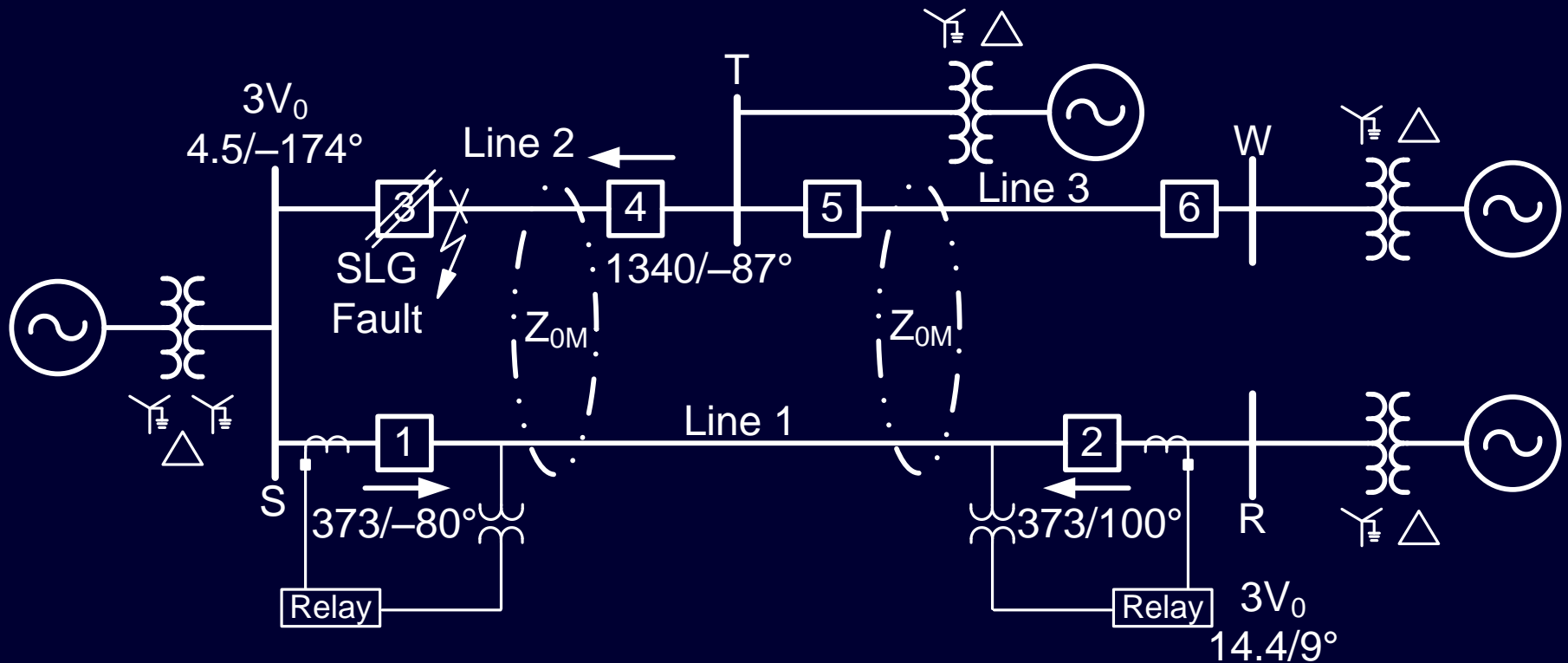


# Polarization Problems



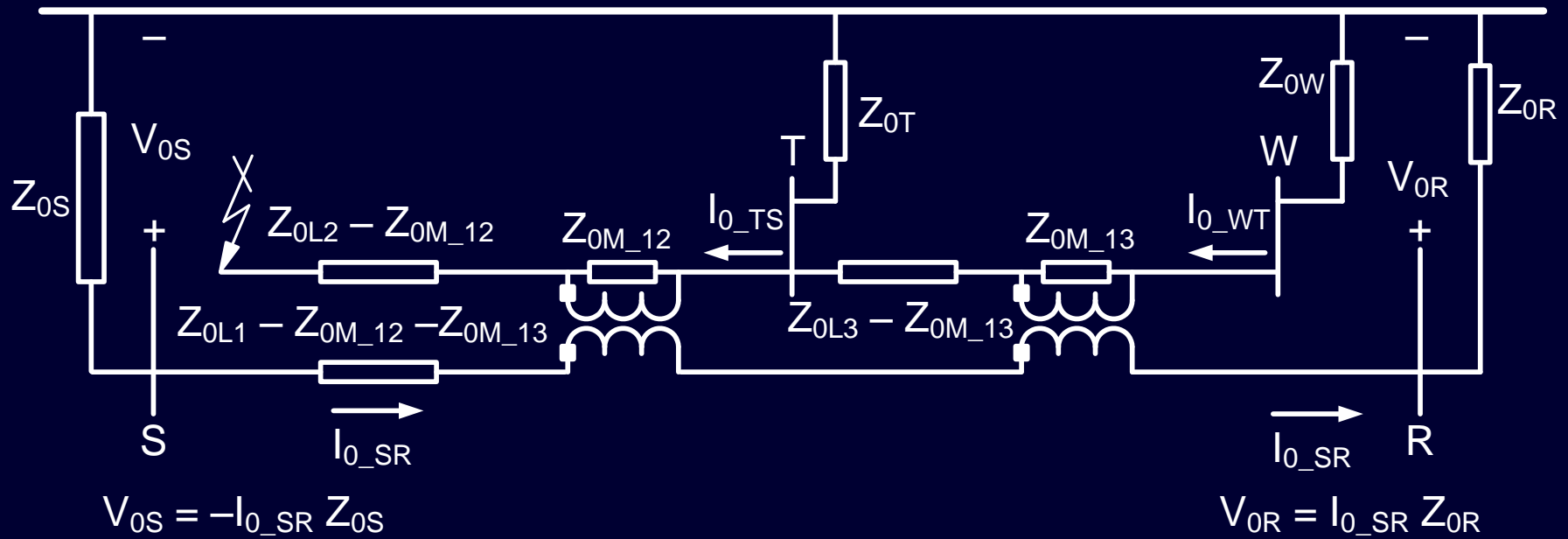
67N elements perform properly when electrical connection is strong

# Polarization Problems



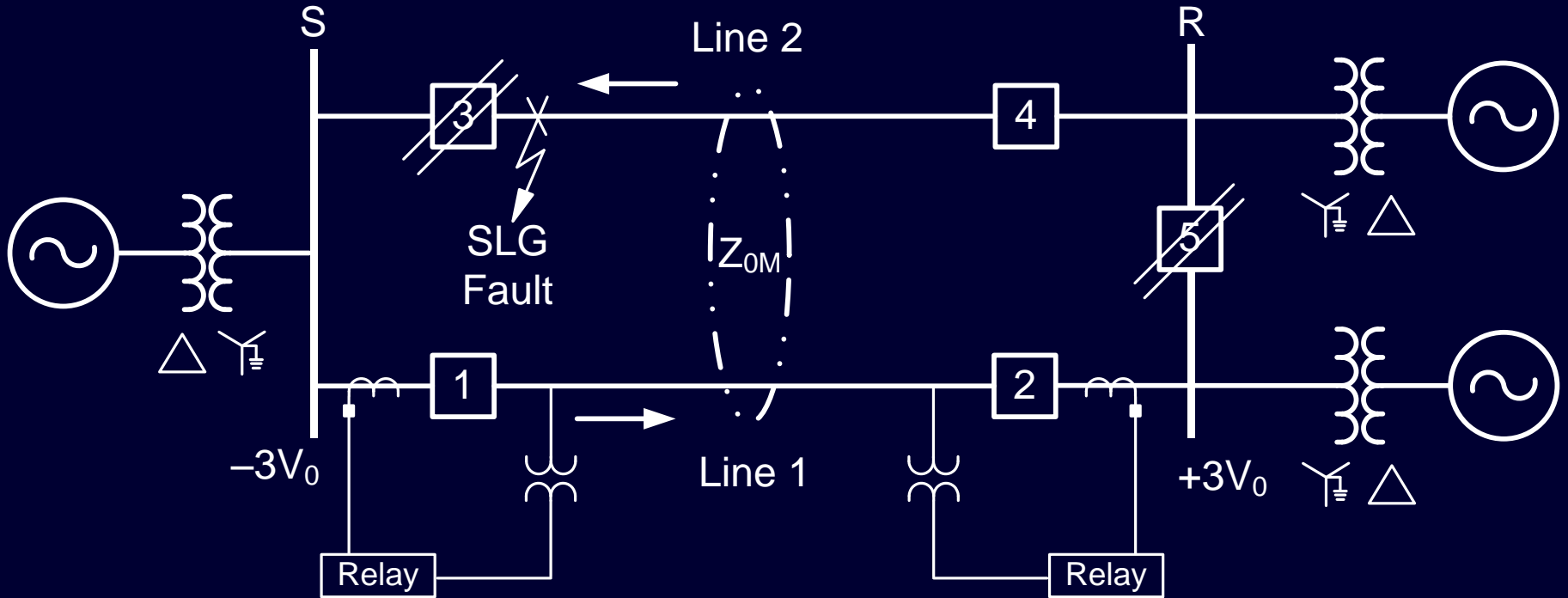
- Breaker 3 opens and isolates zero-sequence networks
- Line 1 could trip for external fault

# Polarization Problems



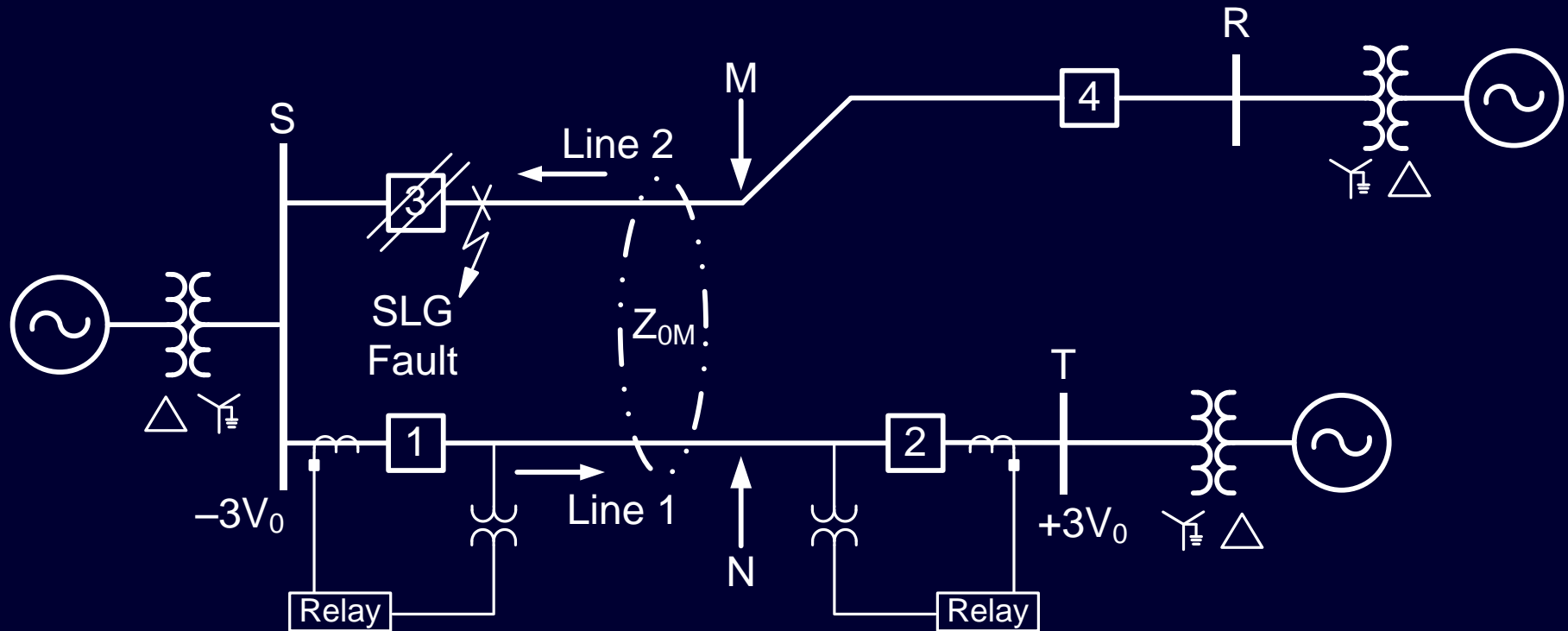
- Mutual coupling causes zero-sequence quantity reversal
- Wrong directional decision at R

# Polarization Problems



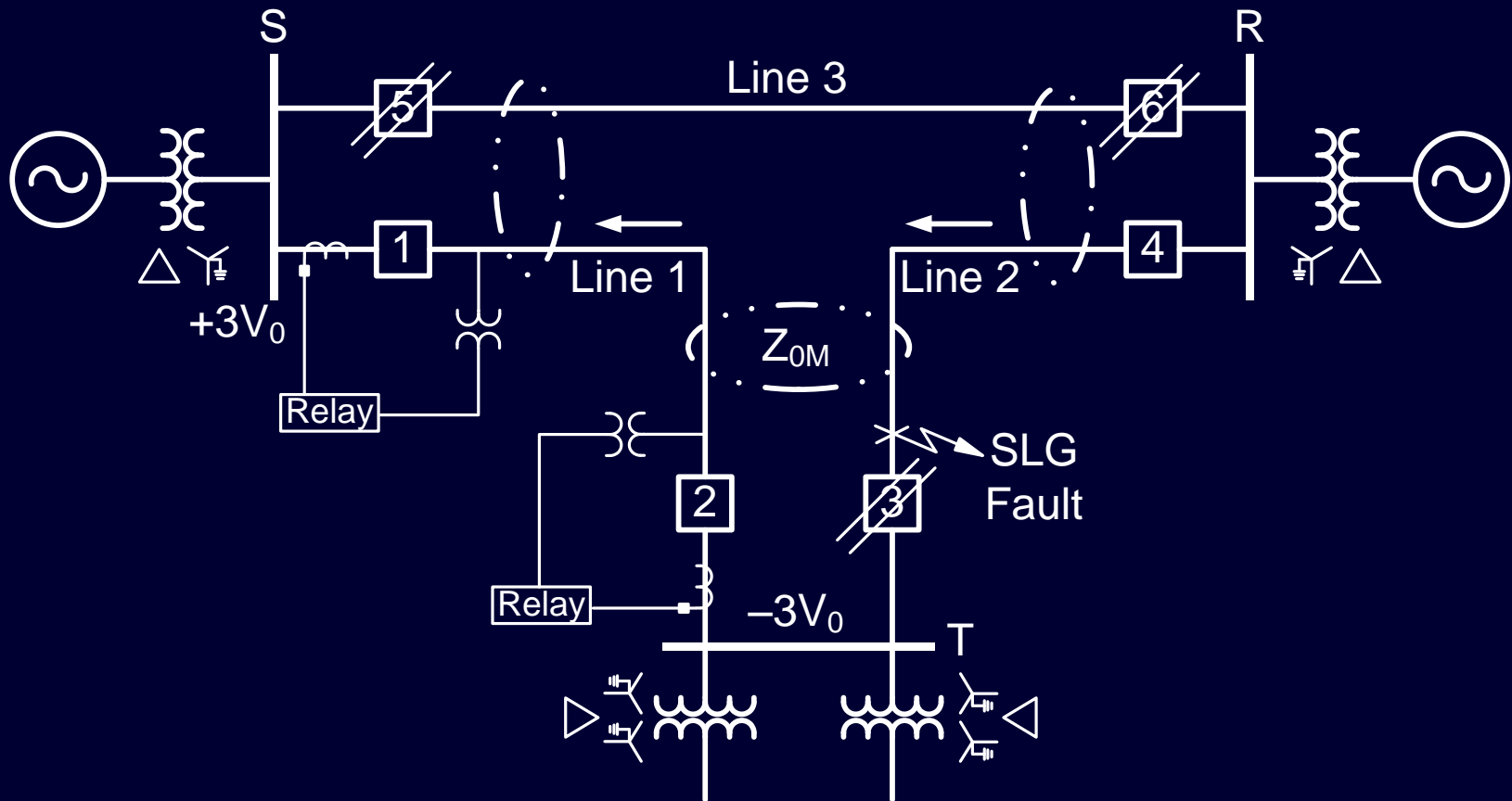
- Coupler breaker open – Breaker 3 opens and isolates the zero-sequence networks
- Wrong directional decision at R

# Polarization Problems



- Breaker 3 opens and isolates the zero-sequence networks
- Wrong directional decision at T

# Polarization Problems



- Line 3 out of service – Breaker 3 opens and isolates the zero-sequence networks
- Wrong directional decision at S

# Polarization Solutions

- Using negative-sequence directional elements
- Supervising ground directional comparison schemes with negative-sequence overcurrent elements
- Applying current differential schemes

# Ground Instantaneous Overcurrent Element Settings

- Extensive short-circuit studies
  - ◆ Strongest system behind relay
  - ◆ SLG fault at remote bus removing ground sources
  - ◆ SLG fault at remote bus removing parallel line
  - ◆ SLG fault at open end of parallel line
- Maximum fault current of different scenarios:  $I_{SET} = 1.25 I_{FLT MAX}$



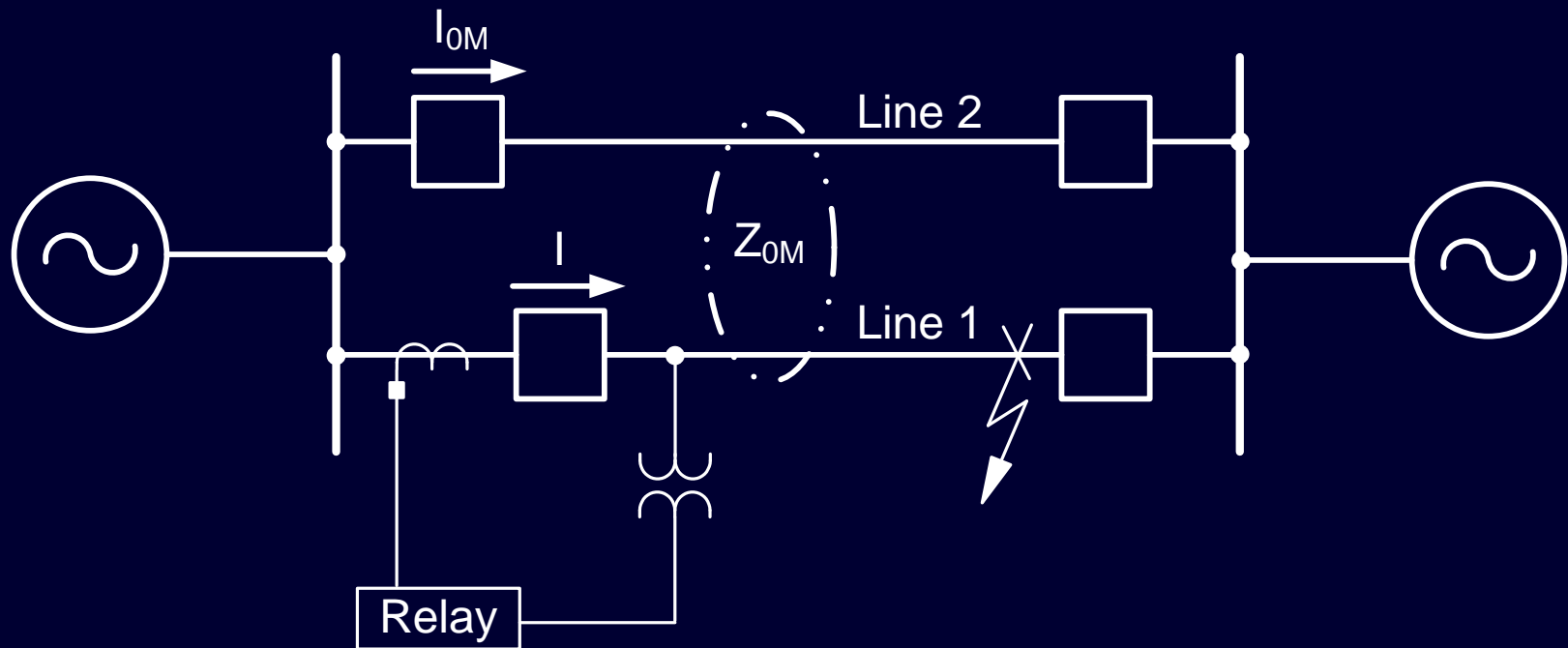
# Input Signals to Traditional Ground Distance Elements

Element	Voltage	Current
AG	$V_a$	$I_a + k_0 I_r$
BG	$V_b$	$I_b + k_0 I_r$
CG	$V_c$	$I_c + k_0 I_r$

$$k_0 = \frac{Z_{0L} - Z_{1L}}{3Z_{IL}}$$

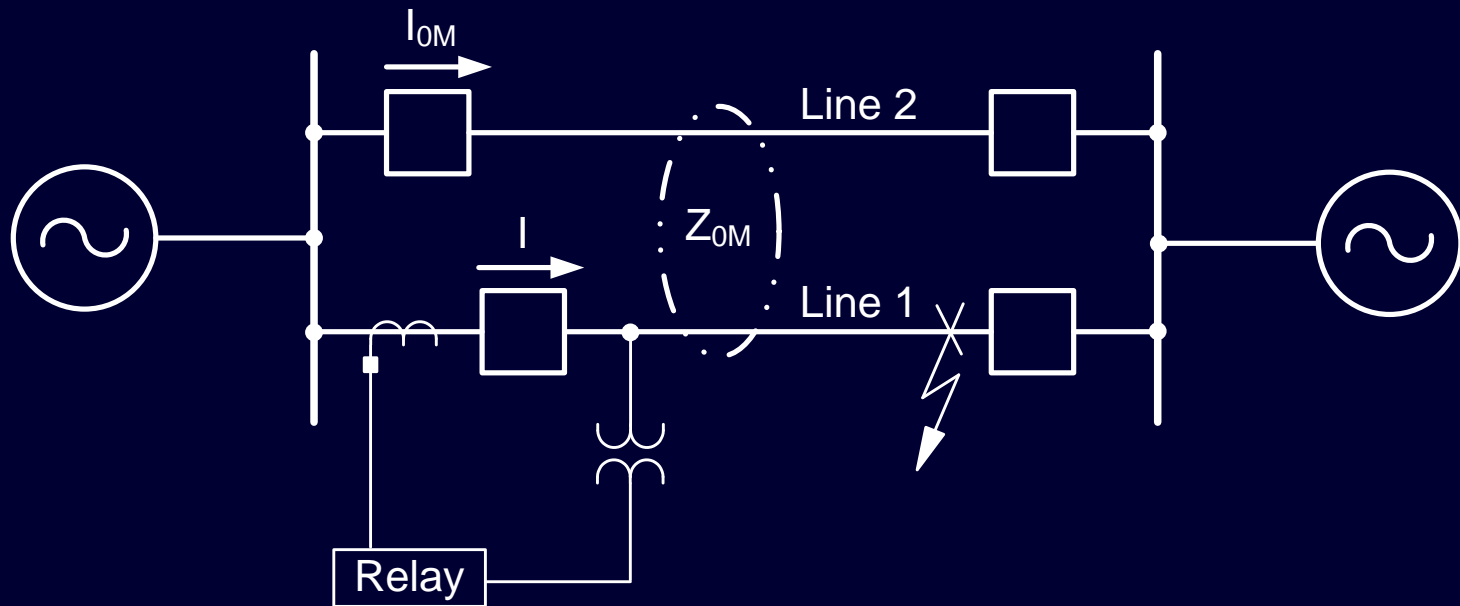
$$I_r = I_a + I_b + I_c$$

# Impact of Mutual Coupling



$$V_a = mZ_{1L} (I_a + k_0 I_r) + mZ_{0M} I_{0M}$$

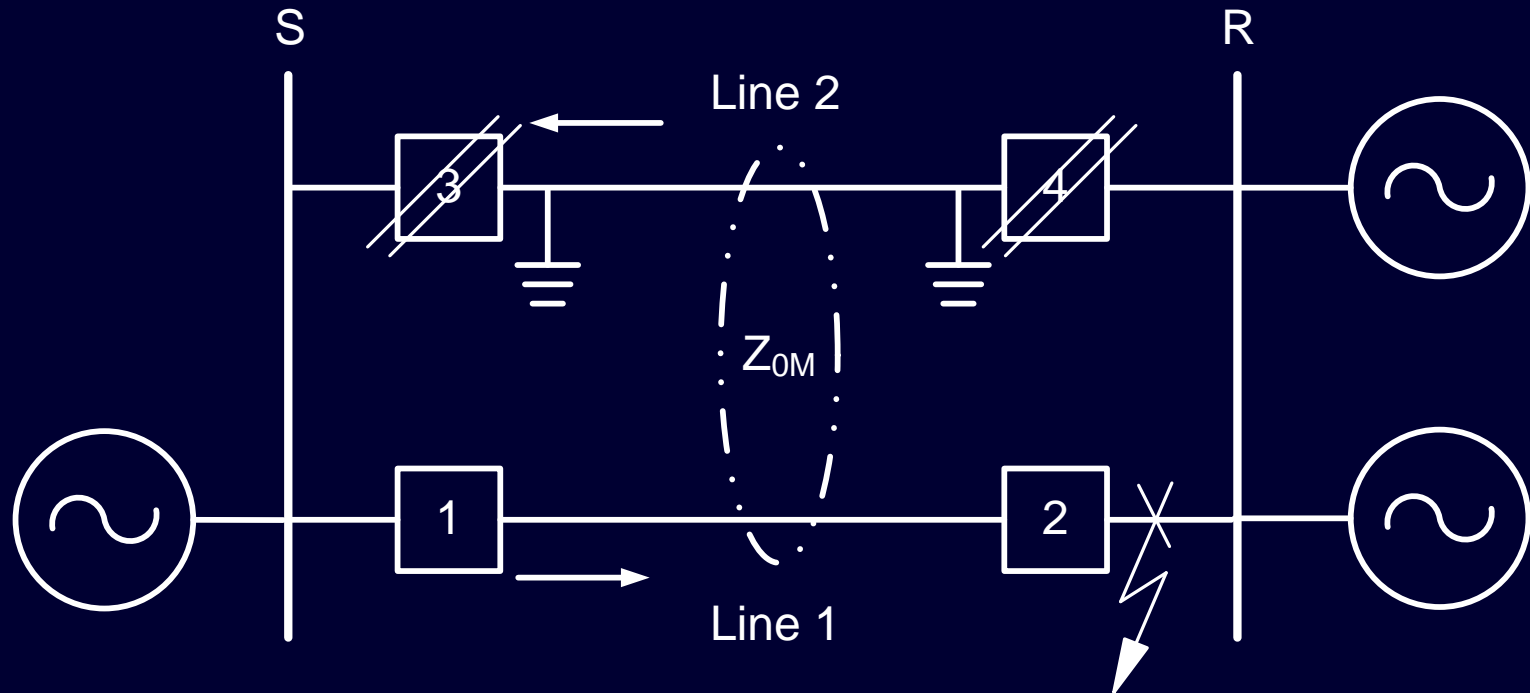
# Mutual Coupling Affects Reach



$$Z_{APP} = \frac{V_a}{I_a + k_0 I_r} = mZ_{1L} + mZ_{0M} \frac{I_{0M}}{I_a + k_0 I_r}$$

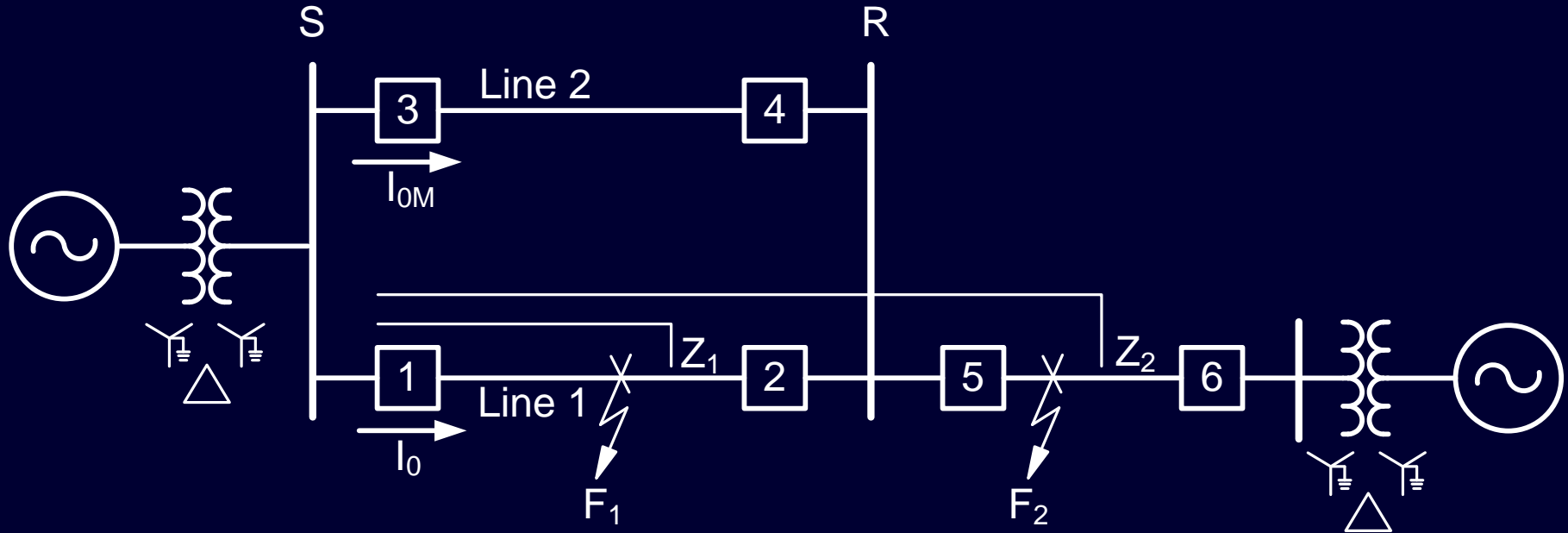
- Underreach if  $I_{0M}$  and  $I_0$  in same direction
- Overreach if  $I_{0M}$  and  $I_0$  in opposite directions

# Another Cause of Reach Errors



- Parallel line grounded at both ends
- Zone 1 may overreach

# Solutions: Applying Reach Settings



- Zone 1 should never overreach
- Zone 2 and other overreaching zones should never underreach

# Solutions: Applying Reach Settings

## Measured Impedances for Different Switching States of the Coupled Line

State of Coupled Line	Measured Impedance
In service	$Z_{APP} = Z_{1L} + \frac{Z_{0M}}{3(1+k_0)}$
Out of service and grounded at one point or not grounded	$Z_{APP} = Z_{1L}$
Out of service and grounded at both line ends	$Z_{APP} = Z_{1L} - \frac{Z_{0M}^2}{3Z_{0L}(1+k_0)}$

## Solutions: Using $I_{0M}$

$$V_a = mZ_{1L} \left( I_a + k_0 I_r + \frac{Z_{0M}}{Z_{1L}} I_{0M} \right)$$

- Compromises relay security during external faults in coupled line
- $I_{0M}$  is not always available
- Increases wiring complexity
- Is not widely accepted

# Solutions: Applying $k_0$ Settings

State of Coupled Line	Measured Impedance
In service	$k_0' = \frac{Z_{0L} - Z_{1L} + Z_{0M}}{3Z_{1L}}$
Out of service and grounded at one point or not grounded	$k_0 = \frac{Z_{0L} - Z_{1L}}{3Z_{1L}}$
Out of service and grounded at both line ends	$k_0'' = \frac{Z_{0L} - Z_{1L} - \frac{Z_{0M}^2}{Z_{0L}}}{3Z_{1L}}$

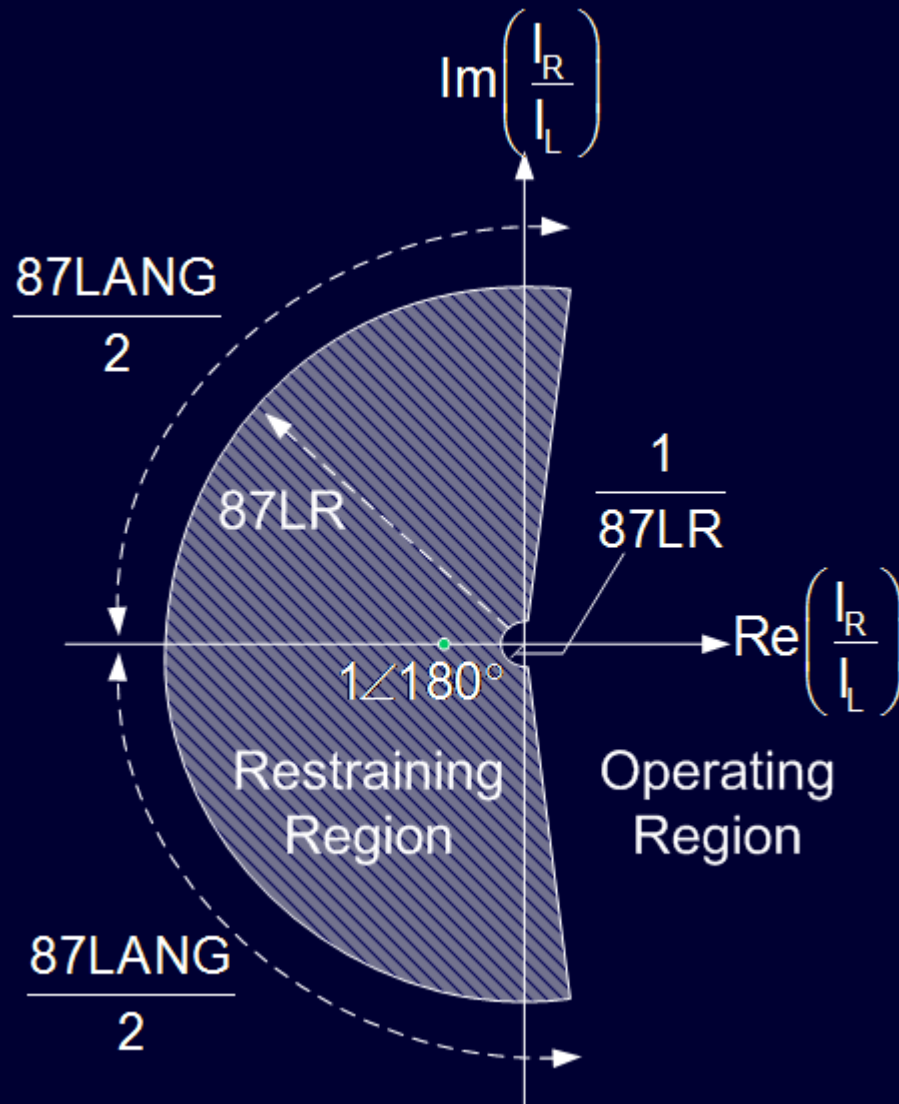
- Prevents  $Z_1$  overreach and  $Z_2$  underreach
- Is applicable for lines connected in parallel



# Fault Locating Algorithms

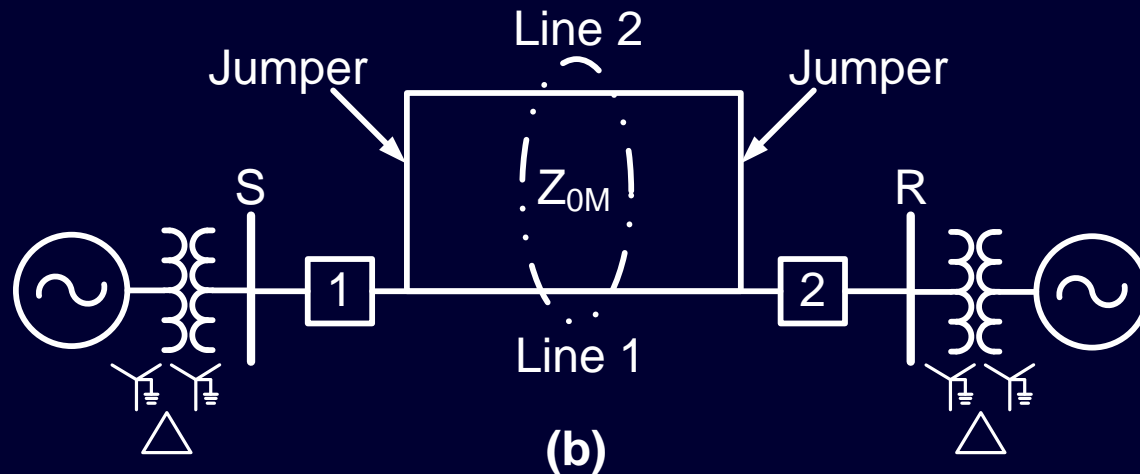
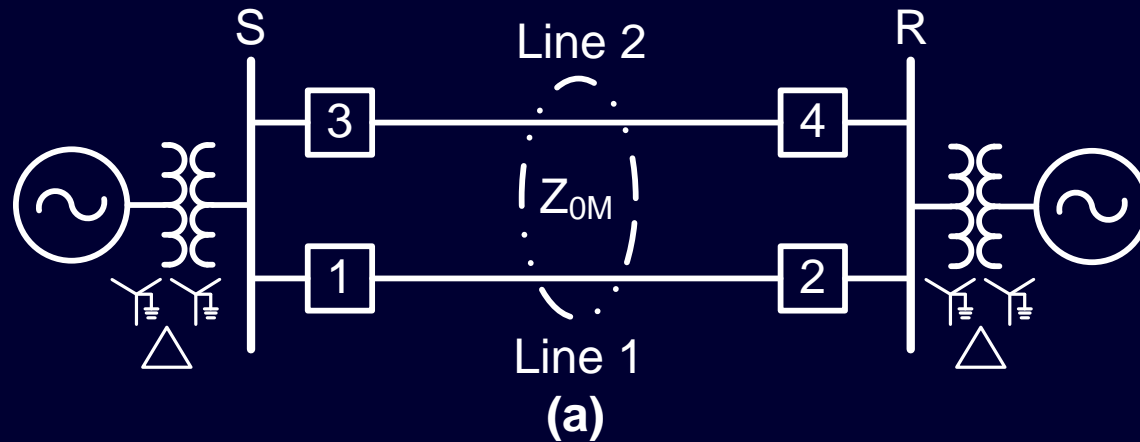
- Zero-sequence single-ended algorithms not using  $I_{0M}$  have errors
- Solutions
  - ◆ Obtain  $I_{0M}$  via relay-to-relay communications
  - ◆ Use negative-sequence multi-ended algorithms
  - ◆ Use traveling wave algorithms

# Line Current Differential Schemes



- Not affected by mutual coupling
- Best solution if communications channel available

# Double-Circuit Transmission Lines Operated as a Single Circuit



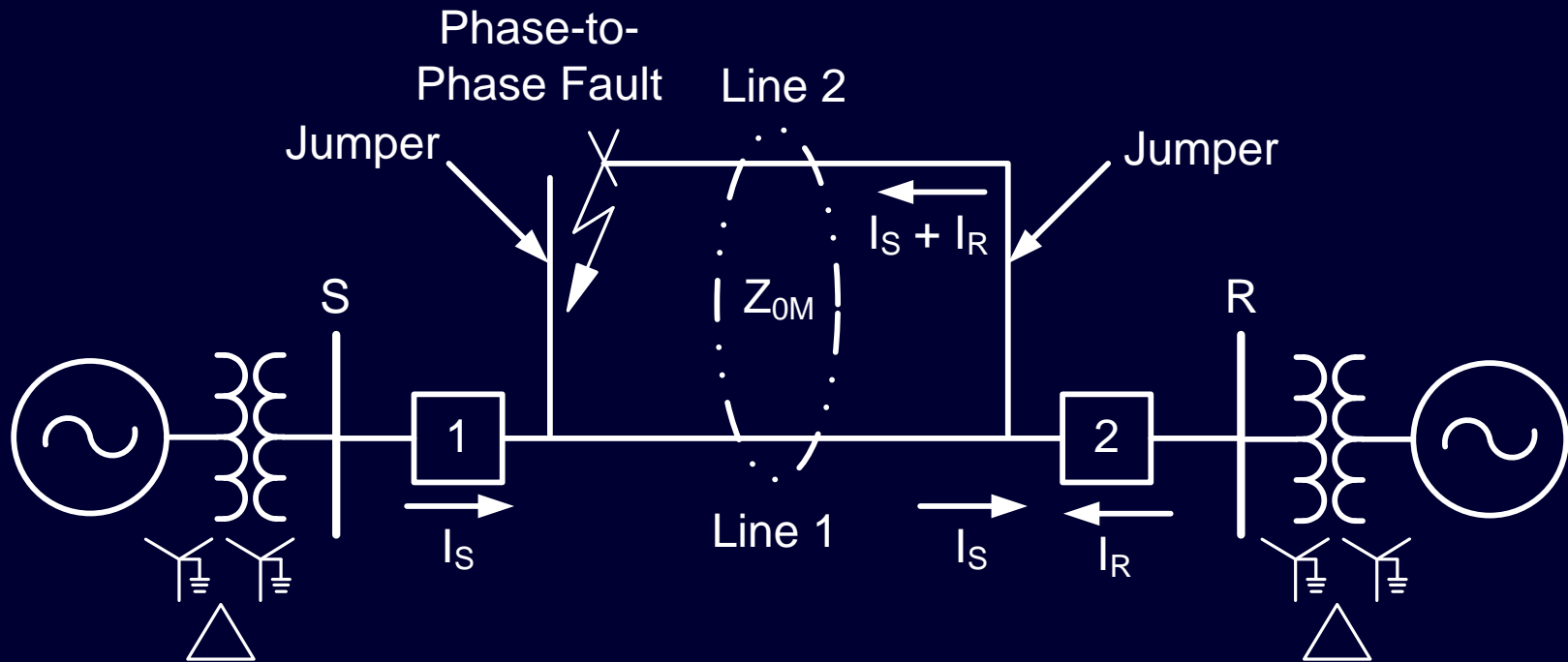
# Measured Impedances at Bus S and R

## Three-Phase Faults on Line 2

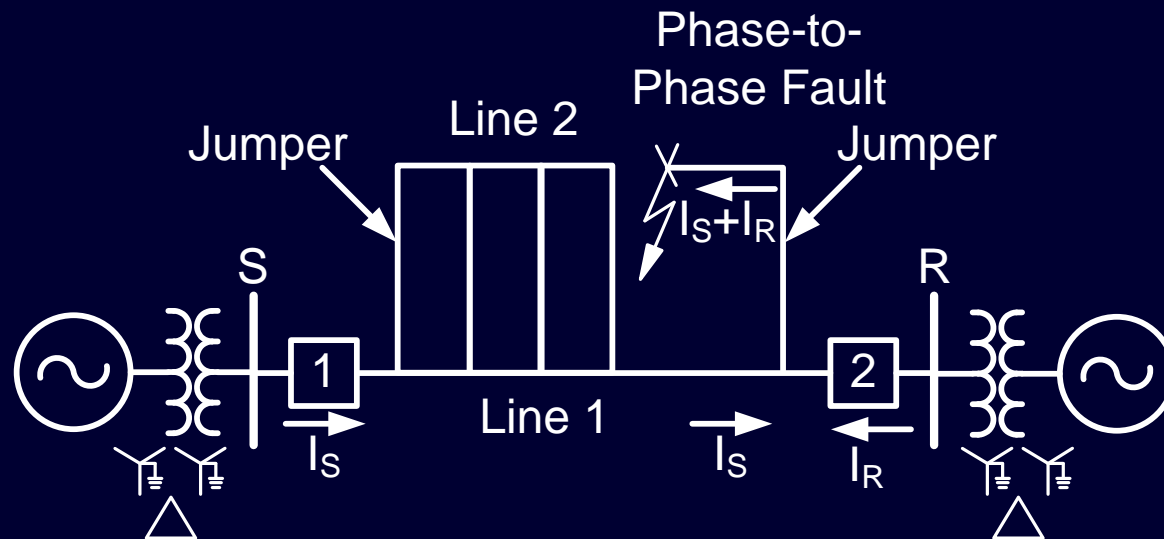
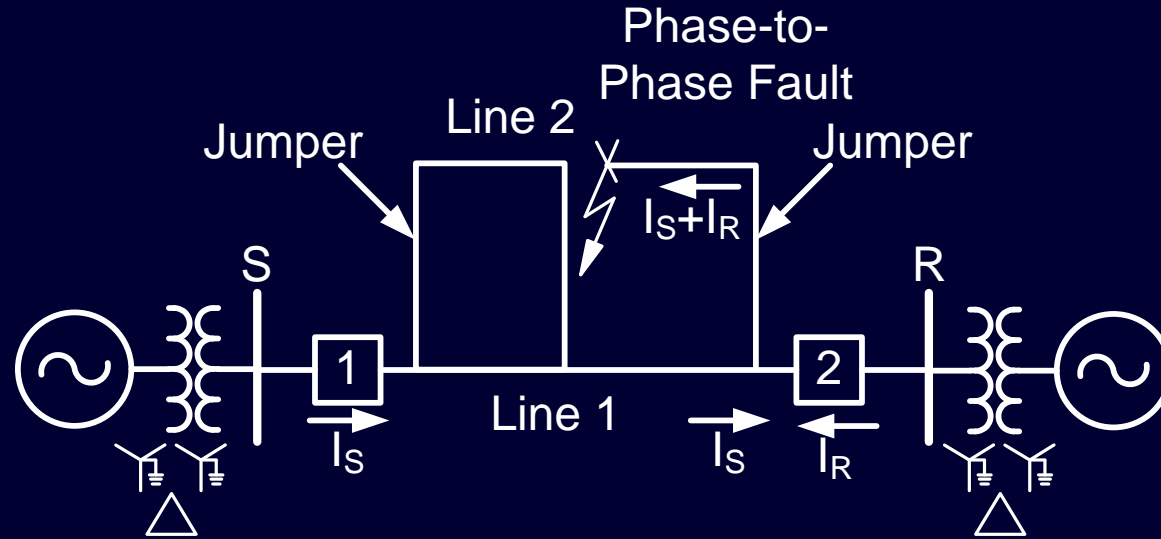
Distance From Bus R (% of Line Length)	Impedance at Bus S (Ohms)	Impedance at Bus R (Ohms)
100	0.0	19.55
90	4.24	25.22
85	6.31	33.22
80	8.35	26.22

$$Z_{1L}/2 = 19.5 \text{ ohms}$$

# A Challenging Fault for Analyzing Underreach



# Additional Jumpers Reduce Underreach



# Measured Impedances at Bus S

## $n$ Jumpers Placed at Equidistant Points Along the Lines

$$Z_{APP} = Z_{1L} \left( \frac{(n+4)}{2(n+1)} + \frac{2}{2(n+1)} \frac{I_R}{I_S} \right)$$

$$Z_{APP} = \frac{Z_{1L}}{2} \frac{(n+4)}{(n+1)}$$

# Conclusions

- Mutual coupling affects zero-sequence polarized ground directional elements
- Negative-sequence polarization is the solution
- Mutual coupling can cause ground distance element under- or overreach
- Distance element compensation methods are difficult to apply



# Conclusions

- Zero-sequence single-ended fault locating without  $I_{0M}$  information is not accurate
- Operating a double-circuit line as a single circuit with jumpers causes distance element underreach
- Current differential protection is the best solution for mutually coupled lines

**Questions?**